

Laser and Fourier Transform Spectroscopy of the $\tilde{A}^2\Pi-\tilde{X}^2\Sigma^+$ Transition of SrOH

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The combination of laser-induced fluorescence with Fourier transform spectroscopy has been used to analyze the 000-000 band of the $\tilde{A}^2\Pi-\tilde{X}^2\Sigma^+$ transition of SrOH. The rotational constants of both states have been determined. Relative intensities from the Fourier transform spectra provide information on rotational energy redistribution by collisions, and on the mixing of parallel character into the transition dipole moment. © 1985 Academic Press, Inc.

I. INTRODUCTION

The visible bands of SrOH have been known for a very long time, the first observations being made by Herschel in 1823 (1). The carrier was not identified as SrOH until 1955, when James and Sugden (2) recognized the similarity with the bands of the isoelectronic strontium fluoride molecule. The bands of SrOH (as for all the alkaline earth metal hydroxides) are so badly overlapped that rotational analysis was not possible before the development of the tunable dye laser. The first such analyses were by Harris and co-workers (3-6). Other analyses of alkaline earth metal hydroxides have also been carried out by Bernath and co-workers (7-9).

We report here the analysis of the $\tilde{A}^2\Pi-\tilde{X}^2\Sigma^+$ system of SrOH which occurs in the region 6700-6900 Å, recorded by laser-induced fluorescence. The spectrum was initially measured using the technique of selective laser excitation with selective fluorescence detection to resolve the overlapped lines. To complete the analysis, Fourier transform spectra of laser-induced fluorescence were recorded using the McMath FTS at Kitt Peak National Observatory. As well as additional transition frequencies, these spectra provide important information on relative line intensities due to the simultaneous observation of all the lines. The relative line intensities are interpreted by inclusion of a parallel contribution to what is nominally a perpendicular transition dipole moment.

II. METHOD

The SrOH molecule was produced in a Broida-type oven (10). Strontium metal was resistively heated in an alumina crucible and the vapor was entrained in a flow of argon carrier gas. The metal atoms then reacted with a few mTorr of water added to the system. Significant amounts of SrOH could only be produced by increasing the

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total pressure to around 9 Torr. The direct bimolecular reaction to produce $\tilde{X}^2\Sigma^+$ SrOH, $\text{Sr}(\text{g}) + \text{H}_2\text{O} \rightarrow \text{SrOH} + \text{H}$, is endothermic² by 0.8 eV (11); hence, this simple process is unlikely to contribute significantly. If, however, the Sr atoms are excited by pumping the $^3P_1-^1S$ transition at 6892 Å with a laser, then the bimolecular reaction becomes exothermic by 1.0 eV. Experimentally, we find that SrOH can be produced at much lower pressure (≈ 1 Torr) and in typically 1000 times higher concentrations when the atomic line is excited.

The output of a Coherent 699-29 computer-controlled ring dye laser was focused vertically into the flame. Typical laser power was 200–500 mW using DCM dye pumped with 7 W of the 4880-Å line of a Coherent Innova 20 argon ion laser. The resultant SrOH fluorescence was dispersed through a 0.65-m monochromator and detected with a cooled photomultiplier tube with photon-counting electronics.

The spectra were recorded by scanning the dye laser and recording the fluorescence through the monochromator. By scanning the laser in the *P* branch and monitoring fluorescence from the connecting *R* branch, the complexity of the spectrum was much reduced (Fig. 2) (12, 13). This also made assignment easy, as transitions with a common excited state could be identified, and ground state combination differences were available (4).

Three channels of data were recorded simultaneously and displayed on the screen before storing on floppy disks. These consisted of the resolved fluorescence spectrum together with either the total undispersed signal or an iodine fluorescence spectrum, and 6-GHz Fabry-Perot fringes from the Coherent 699-29 wavemeter. The fringes were recorded only to provide a check on scan continuity. The wavemeter provides relative wavenumber measurements accurate to $\pm 0.002 \text{ cm}^{-1}$, but the iodine spectrum (14) was needed to maintain the absolute accuracy to this same standard. The data were corrected by subtracting 0.0056 cm^{-1} from the observed lines (15).

Two Doppler-limited Fourier transform spectra of SrOH, produced in a Broida oven, were also recorded. About 1 W of radiation from a Coherent 599-01 broadband dye laser (1-cm^{-1} bandwidth) was passed horizontally through the oven, and the resultant fluorescence was imaged onto the entrance aperture of the FT spectrometer. For one spectrum the laser was tuned to the $P_1 + Q_{12}$ bandhead and 13 scans were coadded in $1 \frac{1}{2}$ hr. For the other the $^3P_1-^1S$ Sr atomic line, which lies very near to the P_{12} branch bandhead (see Fig. 3), was excited. In this case 14 scans were coadded in 1 hr of observation. The resolution of the Fourier transform spectrometer was 0.020 cm^{-1} .

III. RESULTS AND DISCUSSION

A. Vibrational Structure

The $\tilde{A}^2\Pi-\tilde{X}^2\Sigma^+$ system was initially recorded by scanning the dye laser broadband (1-cm^{-1} linewidth) and monitoring the total fluorescence; this spectrum is shown in Fig. 1. The spin-orbit splitting for SrOH is 260 cm^{-1} , so that the $^2\Pi_{3/2}$ and $^2\Pi_{1/2}$ components are well separated and the $^2\Pi$ state conforms to Hund's case (a) coupling. Each of the subbands consists of six branches spaced approximately by $-3B, -B, B,$

² $D_0^0(\text{SrOH}) = 92 \text{ kcal/mole}$ [Ref. (11)].

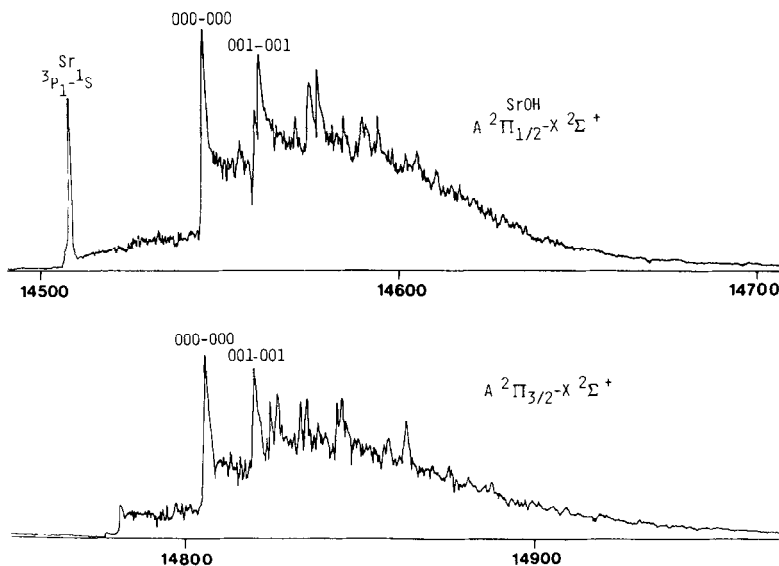


FIG. 1. The $\tilde{A}^2\Pi-\tilde{X}^2\Sigma^+$ system of SrOH recorded by scanning the dye laser (1-cm^{-1} bandwidth) and monitoring the total fluorescence. The approximate frequency scale is given in cm^{-1} .

$3B$, with the $-B$ and B branches doubled by the ground state spin-rotation interaction. The $-B$ branches reach bandheads at quite low J (20-30), giving rise to the prominent features in Fig. 1. The $-3B$ branches give rise to weak high- J bandheads (≈ 90), one of which can be seen at about 14780 cm^{-1} . Herzberg (16) provides notation, energy level diagrams, and a description of a case (a) $^2\Pi-^2\Sigma$ transition.

The transition involves promotion of an electron between two nonbonding metal-centered orbitals of Sr^+ ; this has little effect on the rest of the molecule. Thus the transitions which occur are highly diagonal and the small changes in vibrational frequencies cause the sequence structure to be badly overlapped. This is further complicated by the fact that two vibrations are of low frequency, Sr-O stretch at 522 cm^{-1} and the bend at 360 cm^{-1} , leading to population of many vibrational levels at 500 K.

The Q heads of the 000-000 vibrational band are easy to pick out as they are the most prominent features and lie at the low frequency side of each sequence. Some of the other features in Fig. 1 have been assigned on the basis of measured ground and excited state vibrational frequencies (Table I). These frequencies were measured by fixed frequency laser excitation and recording of the resolved fluorescence. A progression in the ground state Sr-O stretch is seen up to $\Delta\nu_3 = 3$. The excited state stretch (ν'_3) was found to be 544 cm^{-1} from a laser excitation scan. Note that the labeling of the vibrations has been brought into conformity with customary spectroscopic practice (17): ν_1 is the O-H stretch, ν_2 is the Sr-O-H bend and ν_3 is the Sr-O stretch. Previous papers (3-8) had interchanged ν_1 and ν_3 .

The bending vibration has Π character and hence the $\Delta\nu_2 = 1$ transition is formally forbidden (18). However, it is seen with about $1/8$ the intensity of the 000-02⁰ transition. The $\tilde{A}^2\Pi-\tilde{X}^2\Sigma^+$ 000-010 transition is allowed by vibronic coupling. The $\tilde{A}^2\Pi$

TABLE I

SrOH Vibrational Frequencies (in cm^{-1} ; estimated uncertainty $\pm 1 \text{ cm}^{-1}$)

| State | ν_2 | $2\nu_2$ | ν_3 | $2\nu_3$ | $3\nu_3$ |
|-----------------------|---------|----------|---------|----------|----------|
| $\tilde{X}^2\Sigma^+$ | 361 | 727 | 528 | 1048 | 1561 |
| $\tilde{A}^2\Pi$ | - | - | 544 | - | - |

000 (Π) vibronic level interacts with the $\tilde{B}^2\Sigma^+$ 010 (Π) vibronic level so that the $\tilde{A}-\tilde{X}$ 000-010 transition appears by intensity borrowing. There is a definite trend in the observation of ν_2 in the alkaline earth metal hydroxides. For MgOH (6) and CaOH (5, 7) only the $\Delta\nu_2 = 2$ transition is seen. For SrOH the $\Delta\nu_2 = 1$ band is seen weakly while for BaOH (9) it is as strong as the $\Delta\nu_2 = 2$ transition. This increase in 000-010 band intensity correlates with the increase in spin-orbit coupling and is probably due to "spin-orbit vibronic" coupling (19). Fischer's discussion (19) of the spin-orbit vibronic coupling of singlet and triplet states in aromatic molecules is directly applicable with only a change in notation.

The spin-orbit Hamiltonian [$H_{\text{SO}}(q, Q)$] is a function of both electronic (q) and vibrational (Q) coordinates, so the spin-orbit matrix element connecting Π and Σ vibronic states is

$$V_{\text{SO}}(Q) = \langle \Sigma | H_{\text{SO}}(q, Q) | \Pi \rangle \simeq V_{\text{SO}}(Q_0) + \sum_i \left(\frac{\partial V_{\text{SO}}}{\partial Q_i} \right)_{Q_0} Q_i,$$

where the integration is over electronic coordinates. Some manipulation (19) of $(\partial V_{\text{SO}}/\partial Q_i)_{Q_0}$ produces a term of the form

$$\sum_n \langle \Sigma | H_{\text{SO}} | n\Pi \rangle \left\langle n\Pi \left| \frac{\partial H_e}{\partial Q_i} \right| \Pi \right\rangle / (E_{\Pi} - E_{n\Pi})_{Q_0},$$

which contains both spin-orbit mixing ($\langle \Sigma | H_{\text{SO}} | n\Pi \rangle$) and vibronic coupling ($\langle n\Pi | \partial H_e / \partial Q_i | \Pi \rangle$). The diagonal spin-orbit coupling constant of the $\tilde{A}^2\Pi$ state increases from 67 cm^{-1} in CaOH to 635 cm^{-1} in BaOH. Thus, the growing strength of the spin-orbit interaction is probably responsible for the increasing 000-010 band intensity.

B. Rotational Structure

The $\Delta B = -3$ and -1 branches of the 000-000 band were easily discernable, and the other branches were found by adjusting the monochromator to observe fluorescence in one of the known branches while scanning the dye laser. A monochromator bandpass of 1 \AA was usually used for these measurements. All of the transitions were measured using the monochromator as a narrow-band filter to simplify the spectrum (12, 13). Ground state combination differences were obtained by reducing the bandpass to 0.2 \AA , allowing fluorescence from only one rotational line to be detected; and, from these measurements, definite rotational assignments could be made. The FTS mea-

measurements were made after the initial laser assignments had been completed so they were assigned by calculation.

The observed SrOH transition wavenumbers are listed in Table II. Only those lines which were used in the fit are given: low- J transitions with unresolved ground state spin-rotation splitting were not included. All the lines were weighted equally although some of the FTS measurements are of slightly lower accuracy. The average uncertainty as determined from the standard deviation of fit is 0.0025 cm^{-1} , which is consistent with the estimated measurement accuracy.

The observed transitions in Table II were fit to the $^2\Pi$ and $^2\Sigma^+$ energy level expressions of Zare *et al.* (20), using a nonlinear least-squares procedure. An explicit listing of these matrix elements can be found in Kotlar *et al.* (21). The molecular constants determined are given in Table III.

The ground state constants, while of higher precision, are in excellent agreement with those of Nakagawa *et al.* (4). It was found that the $^2\Pi$ state could be represented by only six constants (A , A_J , B , D , p , and q) and a transition energy. When additional higher-order terms such as H , p_D , and q_D were included, the quality of fit was only marginally improved, and these constants were not well determined; hence, they were excluded from the final fit.

The rotational constants B_0 and D_0 for the $\tilde{A}^2\Pi$ state are very similar to those for the $\tilde{B}^2\Sigma^+$ state (6). These two states form a unique perturber pair (20), with

$$\gamma_0 = -0.1667\text{ cm}^{-1} \quad \simeq p_0 \quad = -0.1432\text{ cm}^{-1}.$$

The pure precession value (22) is given by

$$\begin{aligned} p_0 \simeq \gamma_0 &= \frac{2A_0B_0l(l+1)}{E(A^2\Pi) - E(B^2\Sigma^+)} \\ &= -0.157\text{ cm}^{-1} \quad \text{for} \quad l = 1, \end{aligned}$$

which is in reasonable agreement with the experimental results. If the expression is assumed to be exact, then an effective value for l may be calculated: this gives $l_{\text{eff}} = 0.96$. This does not imply that the \tilde{A} and \tilde{B} states are nearly pure p states. A similar estimate can also be made for the other lambda-doubling parameter, q ,

$$\begin{aligned} q &= \frac{2B_0^2l(l+1)}{E(A^2\Pi) - E(B^2\Sigma^+)} \\ &= -1.51 \times 10^{-6}\text{ cm}^{-1} \quad \text{for} \quad l = 1. \end{aligned}$$

Again this is in reasonable agreement with the experimental result of $-1.91 \times 10^{-4}\text{ cm}^{-1}$.

A prediction of the ground state microwave spectrum of SrOH can be made using the constants obtained together with the energy level expressions for $^2\Sigma$ states (16). The strong lines have $\Delta N = \Delta J$; these are given in Table IV for N'' up to 9. Each transition consists of a doublet split by 73 MHz due to the spin-rotation interaction.

The error estimates for the fitted constants imply a precision of between 0.5 MHz for the low- N transitions and 5 MHz for the high- N ones. Due to the possibility of systematic errors, the predictions are probably only accurate to about 10 MHz. This is consistent with the small systematic trends in the residuals of Table II.

TABLE II

Observed Transitions in Wavenumbers in the 000-000 Band of the $\tilde{A}^2\Pi-\tilde{X}^2\Sigma^+$ Transition of SrOH

| J | $P_{12}(J)$ o-c ^a | $P_1(J)$ o-c | $Q_{12}(J)$ o-c | $Q_1(J)$ o-c | $R_{12}(J)$ o-c | $R_1(J)$ o-c |
|------|---------------------------------|--------------------|--------------------|--------------------|--------------------|--------------------|
| 3.5 | 14539.5929 0.0029 | | | | 14543.7270 -0.0021 | 14547.0736 0.0032 |
| 4.5 | 14538.8050 0.0028 | | | | 14543.2642 0.0032 | |
| 5.5 | 14538.0240 0.0029 | | | | 14544.2001 -0.0075 | 14548.8261 -0.0017 |
| 6.5 | 14537.2555 0.0029 | | | 14543.9520 0.0037 | 14544.4550 -0.0049 | 14549.7179 -0.0014 |
| 7.5 | 14536.4940 0.0029 | | | 14544.4390 -0.0002 | 14544.7187 -0.0021 | 14550.6218 0.0023 |
| 8.5 | 14535.7390 0.0008 | | | 14544.7001 0.0024 | 14544.9850 -0.0053 | 14551.5339 0.0056 |
| 9.5 | | | | 14544.9611 -0.0037 | | 14552.4492 0.0036 |
| 10.5 | 14534.2608 0.0021 | | | 14545.2371 -0.0035 | 14545.5530 -0.0024 | 14553.3734 0.0119 |
| 11.5 | 14533.5343 0.0022 | | | 14545.5233 -0.0017 | 14545.8491 -0.0018 | 14554.3092 0.0033 |
| 12.5 | 14532.8156 0.0014 | | | 14545.8241 0.0060 | 14546.1509 -0.0042 | 14555.2558 0.0069 |
| 13.5 | 14532.1066 0.0015 | | | 14546.1150 -0.0049 | 14546.4721 0.0042 | 14556.2046 0.0041 |
| 14.5 | 14531.4052 0.0013 | | | 14546.4267 -0.0035 | 14546.7894 0.0030 | 14557.1532 0.0026 |
| 15.5 | 14530.7163 0.0029 | | | 14546.7465 -0.0028 | 14547.1156 -0.0039 | 14558.1328 0.0037 |
| 16.5 | 14529.0302 -0.0005 | | | 14547.0798 0.0028 | 14547.4555 -0.0027 | 14559.1089 0.0027 |
| 17.5 | 14528.3648 -0.0021 | | | 14547.4109 -0.0024 | 14547.7978 -0.0028 | 14560.0943 0.0024 |
| 18.5 | 14528.6942 0.0023 | | | 14547.757 -0.0026 | 14548.1592 -0.0025 | 14561.0885 0.0025 |
| 19.5 | 14528.0393 0.0025 | | | 14548.1103 0.0016 | 14548.5245 -0.0019 | 14562.0920 0.0034 |
| 20.5 | 14527.3909 0.0024 | | | 14548.4722 -0.0020 | 14548.8944 -0.0054 | 14563.1027 0.0031 |
| 21.5 | 14526.7522 0.0022 | | | 14548.8452 0.0000 | 14549.2666 0.0048 | 14564.1228 0.0036 |
| 22.5 | | | | 14549.2265 0.0018 | 14549.6643 -0.0081 | 14565.1521 0.0049 |
| 23.5 | | | 14540.8077 -0.0027 | 14549.6129 -0.0004 | 14550.0693 -0.0024 | 14566.1838 0.0045 |
| 24.5 | | 14540.7469 -0.0016 | 14540.8523 -0.0035 | 14550.0086 -0.0012 | 14550.4767 -0.0029 | |
| 25.5 | | 14540.7902 -0.0012 | 14540.9078 -0.0020 | 14550.4156 0.0003 | 14550.8946 -0.0016 | 14568.2388 0.0019 |
| 26.5 | | 14540.8430 -0.0001 | 14540.9718 -0.0008 | 14550.8283 -0.0012 | 14551.3220 0.0006 | 14569.3455 0.0018 |
| 27.5 | | 14540.9029 -0.0005 | 14541.0450 0.0009 | 14551.2515 -0.0008 | 14551.7470 -0.0003 | 14570.4175 0.0036 |
| 28.5 | | 14540.9727 0.0002 | 14541.1257 0.0014 | 14551.6862 0.0025 | 14552.1973 -0.0005 | 14571.4961 0.0036 |
| 29.5 | | 14541.0487 -0.0016 | | 14552.1238 0.0000 | 14552.6507 0.0017 | 14572.5810 0.0014 |
| 30.5 | | | | 14552.5723 -0.0002 | 14553.1075 -0.0013 | 14573.6776 0.0026 |
| 31.5 | | | | 14553.0275 -0.0024 | 14553.5766 -0.0006 | 14574.7821 0.0033 |
| 32.5 | 14520.3207 0.0058 | | | 14553.4961 0.0002 | 14554.0527 -0.0016 | 14575.8942 0.0032 |
| 33.5 | 14519.7810 -0.0026 | 14541.3344 -0.0016 | 14541.5304 -0.0021 | 14553.9689 -0.0016 | 14554.5355 -0.0045 | 14577.0128 0.0012 |
| 34.5 | 14519.2631 0.0019 | 14541.4463 -0.0024 | 14541.6544 -0.0019 | 14554.4547 0.0004 | 14555.0313 -0.0030 | 14578.1423 0.0018 |
| 35.5 | 14518.7498 0.0019 | 14541.5681 0.0001 | 14541.7878 -0.0011 | 14554.9451 -0.0006 | 14555.5226 -0.0048 | |
| 36.5 | 14518.2459 0.0023 | 14541.6994 -0.0009 | 14541.9321 0.0018 | 14555.4448 -0.0015 | 14556.0612 0.0022 | |
| 37.5 | 14517.7482 -0.0001 | 14541.8395 0.0002 | 14542.0775 -0.0029 | 14555.9541 -0.0014 | 14556.5647 -0.0046 | 14581.5800 0.0025 |
| 38.5 | | 14541.9875 0.0006 | 14542.2407 0.0015 | 14556.4727 -0.0007 | 14557.0928 -0.0054 | 14582.7427 0.0029 |
| 39.5 | 14516.7836 -0.0012 | 14542.1424 -0.0009 | | 14556.9967 -0.0012 | 14557.6323 -0.0035 | 14583.9121 0.0016 |
| 40.5 | 14516.3130 -0.0037 | | 14542.5812 -0.0019 | 14557.5319 -0.0031 | 14558.1870 0.0050 | 14585.0925 0.0031 |
| 41.5 | 14515.8532 -0.0044 | 14542.4825 0.0001 | 14542.7679 -0.0003 | 14558.0767 -0.0021 | 14558.7399 0.0031 | 14586.2816 0.0049 |
| 42.5 | 14515.4075 -0.0001 | 14542.6641 -0.0009 | 14542.9614 -0.0006 | 14558.6296 -0.0016 | 14559.2977 -0.0026 | 14587.4757 0.0033 |
| 43.5 | 14514.9620 -0.0047 | 14542.8571 0.0007 | 14543.1643 -0.0003 | 14559.1898 -0.0025 | 14559.8667 -0.0020 | 14588.6701 0.0018 |
| 44.5 | 14514.5289 -0.0059 | 14543.0565 -0.0001 | 14543.3767 0.0008 | 14559.7609 -0.0011 | 14560.4500 -0.0032 | 14589.8907 0.0022 |
| 45.5 | 14514.1181 0.0060 | 14543.2635 -0.0020 | | 14560.3394 -0.0010 | 14561.0368 -0.0059 | 14591.1093 0.0004 |
| 46.5 | 14513.6995 0.0010 | | | 14560.9326 0.0052 | | 14592.3386 0.0009 |
| 47.5 | 14513.2901 -0.0039 | 14543.4701 0.0005 | 14544.0632 0.0006 | 14561.5236 0.0006 | | 14593.5772 0.0025 |
| 48.5 | 14512.8965 -0.0032 | 14543.9448 -0.0001 | 14544.3084 -0.0006 | | | 14594.8206 0.0006 |
| 49.5 | | 14544.1975 -0.0014 | 14544.5650 0.0008 | | | 14596.0759 0.0023 |
| 50.5 | | 14544.4418 0.0000 | 14544.8298 0.0015 | 14562.7378 -0.0024 | | 14597.3357 0.0004 |
| 51.5 | | 14544.7041 0.0009 | 14545.1045 0.0035 | | | 14598.6000 0.0006 |
| 52.5 | | 14544.9760 0.0025 | 14545.3830 0.0005 | | | 14599.8837 0.0001 |
| 53.5 | | 14545.2533 0.0006 | 14545.6743 0.0014 | | | 14601.1711 0.0010 |
| 54.5 | | 14545.5407 0.0001 | 14545.9716 -0.0004 | | | 14602.4642 0.0003 |
| 55.5 | | 14545.8385 0.0012 | | | | 14603.7698 0.0020 |
| 56.5 | | | 14546.9224 0.0002 | | | 14605.0777 -0.0012 |
| 57.5 | | 14546.7811 0.0009 | 14547.2574 0.0008 | | | 14606.3994 0.0012 |
| 58.5 | | 14547.1137 0.0015 | | | | 14607.7288 0.0010 |
| 59.5 | | 14547.4523 0.0006 | 14547.9500 -0.0017 | | | 14609.0617 0.0002 |
| 60.5 | | 14547.8002 -0.0022 | 14548.3134 0.0009 | | | 14602.0387 -0.0023 |
| 61.5 | | 14548.1604 -0.0004 | 14548.6825 0.0004 | | | 14622.8655 -0.0006 |
| 62.5 | | 14548.5255 -0.0025 | 14549.0593 -0.0013 | | | 14610.4063 0.0029 |
| 63.5 | | 14548.9030 -0.0010 | | | | 14611.7571 -0.0003 |
| 64.5 | | 14549.2866 -0.0023 | 14549.8440 0.0000 | | | 14613.1178 0.0002 |
| 65.5 | | 14549.6822 -0.0003 | 14550.2494 0.0005 | | | 14614.4895 -0.0006 |
| 66.5 | | 14550.0847 -0.0004 | 14550.6620 -0.0007 | 14574.4883 0.0057 | 14575.4188 0.0013 | 14617.2474 0.0002 |
| 67.5 | | 14550.4951 -0.0013 | 14551.0869 0.0016 | 14575.2535 0.0023 | 14576.2009 0.0037 | 14618.6384 -0.0017 |
| 68.5 | 14506.9275 -0.0004 | 14550.9166 -0.0000 | 14551.5159 -0.0009 | 14576.0312 0.0027 | 14576.9883 0.0028 | 14620.0387 -0.0023 |
| 69.5 | 14506.7281 0.0011 | 14551.3437 -0.0020 | 14551.9553 -0.0018 | 14576.8162 0.0019 | 14577.7840 0.0015 | 14621.4478 -0.0023 |
| 70.5 | 14506.5384 0.0009 | 14551.7807 -0.0029 | 14552.4052 -0.0011 | 14577.6110 0.0021 | 14578.5894 0.0013 | 14622.8655 -0.0006 |
| 71.5 | 14506.3661 0.0027 | 14552.2277 -0.0026 | 14552.8638 -0.0006 | 14577.4136 0.0015 | 14579.4041 0.0018 | 14624.2884 -0.0042 |
| 72.5 | 14506.1817 0.0010 | 14552.6843 -0.0017 | 14553.3300 -0.0013 | 14578.2260 0.0021 | 14580.2268 0.0015 | 14625.7244 -0.0016 |
| 73.5 | 14506.0174 0.0000 | 14553.1471 -0.0034 | 14553.8066 -0.0005 | 14579.0457 0.0012 | 14581.0585 0.0016 | 14627.1658 -0.0017 |
| 74.5 | 14505.8651 0.0026 | 14553.6218 -0.0020 | 14554.2906 -0.0011 | 14580.8761 0.0025 | 14581.8985 0.0013 | 14628.6171 0.0002 |
| 75.5 | 14505.7210 0.0020 | 14554.1038 -0.0022 | | 14581.7132 0.0017 | 14582.7468 0.0017 | 14629.0788 0.0002 |
| 76.5 | 14505.5878 0.0037 | | | 14582.5598 0.0018 | 14583.6053 0.0016 | 14629.5484 0.0002 |
| 77.5 | 14505.4612 0.0027 | | | 14583.4146 0.0015 | 14584.4671 -0.0028 | 14630.0387 -0.0023 |
| 78.5 | 14505.3465 0.0040 | | | 14584.2772 0.0003 | 14585.3415 -0.0032 | 14630.5387 -0.0023 |
| 79.5 | 14505.2362 0.0003 | | | 14585.1456 0.0002 | 14586.2297 0.0013 | 14631.0484 -0.0042 |
| 80.5 | 14505.1304 -0.0004 | | | 14586.0352 0.0046 | 14587.1163 -0.0043 | 14631.5684 -0.0042 |
| 81.5 | 14505.0472 -0.0040 | | | 14586.9188 -0.0016 | 14588.0223 0.0007 | 14632.0884 -0.0042 |
| 82.5 | 14504.9707 -0.0025 | | | 14587.8207 0.0018 | 14588.9296 -0.0015 | 14632.6184 -0.0042 |
| 83.5 | 14504.9031 -0.0016 | | | 14588.7299 0.0038 | 14589.8525 0.0031 | 14633.1484 -0.0042 |
| 84.5 | 14504.8428 -0.0029 | | | 14589.6340 -0.0078 | | 14633.6784 -0.0042 |
| 85.5 | | | | 14590.5680 0.0016 | | |

^a Observed-Calculated in wavenumbers.

There is also the possibility of proton hyperfine structure; this has been discussed for CaOH (8). The effect is likely to be similar in SrOH, with splittings of a few MHz at low N dropping to zero at higher N where both rotational levels show the same hyperfine splitting.

TABLE II—Continued

| J | $P_2(J)$ | | $P_{21}(J)$ | | $Q_2(J)$ | | $R_{21}(J)$ | |
|------|------------|---------|-------------|---------|------------|---------|-------------|---------|
| | | O-C | | O-C | | O-C | | O-C |
| 1.5 | | | | | | | 14807.3704 | 0.0013 |
| 2.5 | | | | | | | 14808.1504 | 0.0010 |
| 3.5 | | | | | | | | |
| 4.5 | | | | | | | | |
| 5.5 | 14801.4760 | 0.0005 | | | | | 14809.7375 | -0.0012 |
| 6.5 | 14800.7831 | 0.0006 | | | | | 14810.5452 | -0.0027 |
| 7.5 | 14800.0979 | -0.0012 | | | | | 14811.3659 | -0.0007 |
| 8.5 | 14799.4254 | -0.0001 | | | | | 14812.1936 | -0.0014 |
| 9.5 | 14798.7603 | -0.0013 | | | | | 14813.0308 | -0.0023 |
| 10.5 | 14798.1090 | 0.0016 | | | 14803.4380 | -0.0037 | 14814.7376 | -0.0004 |
| 11.5 | 14797.4618 | -0.0012 | 14803.4176 | 0.0036 | 14803.3546 | -0.0006 | 14815.6029 | -0.0019 |
| 12.5 | 14796.8283 | 0.0000 | 14803.2776 | 0.0028 | 14803.1784 | 0.0000 | 14816.4788 | -0.0024 |
| 13.5 | 14796.2054 | 0.0020 | 14803.1489 | 0.0033 | 14803.0508 | -0.0005 | | |
| 14.5 | 14795.5904 | 0.0022 | 14803.0279 | 0.0018 | 14802.9555 | 0.0015 | 14818.2591 | -0.0037 |
| 15.5 | 14794.9873 | 0.0045 | 14802.9178 | 0.0015 | 14802.8507 | 0.0024 | 14819.1665 | -0.0015 |
| 16.5 | 14794.3860 | -0.0012 | 14802.8172 | 0.0009 | 14802.7569 | 0.0004 | 14820.0816 | -0.0011 |
| 17.5 | 14793.8020 | -0.0016 | 14802.7286 | 0.0006 | 14802.6686 | -0.0019 | 14821.0078 | 0.0008 |
| 18.5 | 14793.2251 | -0.0002 | 14802.6416 | -0.0038 | 14802.6211 | -0.0008 | | |
| 19.5 | 14792.6607 | 0.0017 | 14802.5689 | -0.0057 | 14802.5641 | 0.0008 | 14822.9804 | -0.0038 |
| 20.5 | 14792.1023 | -0.0003 | 14802.5152 | 0.0017 | 14802.5161 | 0.0018 | | |
| 21.5 | 14791.5508 | 0.0049 | 14802.4680 | 0.0058 | 14802.4768 | 0.0016 | 14824.8005 | 0.0009 |
| 22.5 | 14791.0200 | 0.0000 | 14802.4246 | 0.0042 | 14802.4429 | -0.0029 | | |
| 23.5 | 14790.4938 | 0.0017 | 14802.3862 | -0.0025 | 14802.4243 | -0.0018 | 14826.7524 | -0.0006 |
| 24.5 | 14789.9748 | -0.0001 | 14802.3644 | -0.0023 | 14802.4183 | 0.0020 | 14827.7450 | 0.0010 |
| 25.5 | 14789.4669 | -0.0006 | 14802.3564 | 0.0020 | 14802.4179 | 0.0018 | 14828.7444 | -0.0001 |
| 26.5 | 14788.9682 | -0.0018 | 14802.3537 | 0.0019 | 14802.4265 | 0.0007 | 14829.7566 | 0.0021 |
| 27.5 | 14788.4829 | 0.0025 | 14802.3592 | 0.0002 | 14802.4425 | -0.0017 | 14830.7723 | -0.0017 |
| 28.5 | 14788.0052 | 0.0007 | 14802.3751 | -0.0009 | 14802.4737 | -0.0007 | 14831.8039 | 0.0009 |
| 29.5 | 14787.5389 | 0.0003 | 14802.3990 | -0.0038 | 14802.5142 | 0.0008 | 14832.8416 | 0.0006 |
| 30.5 | 14787.0785 | 0.0000 | 14802.4401 | 0.0037 | 14802.5631 | 0.0009 | 14833.8903 | 0.0009 |
| 31.5 | 14786.6305 | 0.0002 | 14802.4684 | 0.0026 | 14802.6191 | -0.0017 | 14834.9481 | 0.0013 |
| 32.5 | 14786.1937 | 0.0004 | 14802.5415 | -0.0003 | 14802.6846 | -0.0045 | 14836.0132 | 0.0026 |
| 33.5 | 14785.7650 | 0.0015 | 14802.6052 | -0.0026 | 14802.7646 | -0.0027 | 14837.0877 | -0.0022 |
| 34.5 | 14785.3471 | 0.0022 | 14802.6818 | -0.0018 | 14802.8546 | -0.0007 | 14838.1738 | -0.0018 |
| 35.5 | 14784.9370 | 0.0008 | 14802.7677 | -0.0014 | 14802.9517 | -0.0013 | 14839.2704 | -0.0004 |
| 36.5 | 14784.5373 | -0.0001 | 14802.8630 | -0.0014 | 14803.0593 | -0.0013 | 14840.3765 | 0.0011 |
| 37.5 | | | 14802.9666 | -0.0031 | 14803.1755 | -0.0025 | 14841.4895 | -0.0010 |
| 38.5 | | | 14803.0828 | -0.0017 | 14803.3035 | -0.0017 | 14842.6127 | -0.0002 |
| 39.5 | 14783.4011 | 0.0004 | 14803.2086 | -0.0007 | 14803.4375 | -0.0047 | 14843.7449 | -0.0009 |
| 40.5 | 14783.0430 | 0.0014 | 14803.3368 | -0.0051 | 14803.5844 | -0.0047 | 14844.8892 | 0.0012 |
| 41.5 | 14782.6963 | 0.0029 | 14803.4836 | -0.0047 | 14803.7464 | 0.0007 | 14846.0381 | -0.0016 |
| 42.5 | 14782.3547 | 0.0015 | 14803.6426 | 0.0000 | 14803.9118 | -0.0004 | 14847.1989 | -0.0018 |
| 43.5 | 14782.0260 | 0.0020 | 14803.8043 | -0.0023 | 14804.0860 | -0.0026 | 14848.3703 | -0.0009 |
| 44.5 | 14781.7077 | 0.0030 | 14803.9793 | -0.0012 | 14804.2752 | 0.0004 | 14849.5507 | -0.0003 |
| 45.5 | 14781.3982 | 0.0029 | 14804.1636 | -0.0007 | 14804.4702 | -0.0006 | 14850.7415 | 0.0014 |
| 46.5 | 14781.0972 | 0.0012 | 14804.3575 | -0.0004 | 14804.6737 | -0.0009 | 14851.9385 | -0.0002 |
| 47.5 | 14780.8118 | 0.0026 | 14804.5621 | 0.0006 | 14804.8913 | -0.0010 | 14853.1493 | 0.0026 |
| 48.5 | 14780.5282 | 0.0010 | 14804.7745 | -0.0001 | 14805.1189 | 0.0010 | 14854.3630 | -0.0008 |
| 49.5 | 14780.2597 | 0.0019 | 14804.9982 | 0.0005 | 14805.3548 | 0.0015 | 14855.5311 | 0.0007 |
| 50.5 | 14779.9995 | 0.0012 | 14805.2306 | -0.0001 | 14805.5999 | 0.0013 | 14856.7239 | -0.0009 |
| 51.5 | 14779.7499 | 0.0010 | 14805.4747 | 0.0011 | 14805.8555 | 0.0018 | 14858.0686 | -0.0029 |
| 52.5 | 14779.5095 | 0.0000 | 14805.7254 | -0.0009 | 14806.1187 | -0.0000 | 14859.3266 | 0.0005 |
| 53.5 | 14779.2814 | 0.0013 | 14805.9909 | 0.0020 | 14806.3935 | -0.0001 | 14860.5909 | 0.0010 |
| 54.5 | 14779.0601 | -0.0006 | 14806.2611 | -0.0002 | 14806.6781 | -0.0002 | 14861.8630 | -0.0001 |
| 55.5 | 14778.8541 | 0.0027 | 14806.5432 | -0.0004 | 14806.9752 | 0.0022 | 14863.1481 | 0.0025 |
| 56.5 | 14778.6529 | 0.0008 | 14806.8345 | -0.0013 | 14807.2787 | 0.0012 | 14864.4365 | -0.0009 |
| 57.5 | 14778.4647 | 0.0019 | 14807.1391 | 0.0012 | 14807.5934 | 0.0016 | 14865.7412 | 0.0028 |
| 58.5 | 14778.2861 | 0.0025 | 14807.4520 | 0.0022 | 14807.9196 | 0.0035 | 14867.0693 | 0.0005 |
| 59.5 | 14778.1167 | 0.0023 | 14807.7732 | 0.0015 | 14808.2393 | -0.0110 | 14868.3660 | -0.0024 |
| 60.5 | 14777.9585 | 0.0032 | 14808.1009 | -0.0025 | 14808.5940 | -0.0003 | 14869.6986 | 0.0014 |
| 61.5 | 14777.8079 | 0.0017 | 14808.4449 | -0.0002 | 14808.9465 | -0.0018 | 14871.0352 | -0.0002 |
| 62.5 | 14777.6672 | -0.0000 | 14808.7952 | -0.0014 | 14809.3119 | -0.0002 | 14872.3828 | 0.0001 |
| 63.5 | 14777.5401 | 0.0017 | 14809.1583 | 0.0003 | 14809.6889 | 0.0010 | 14873.7383 | -0.0001 |
| 64.5 | 14777.4232 | 0.0036 | 14809.5301 | 0.0007 | 14810.0672 | -0.0024 | 14875.1051 | -0.0001 |
| 65.5 | 14777.3163 | 0.0055 | 14809.9114 | 0.0008 | 14810.4657 | 0.0025 | 14876.4810 | 0.0007 |
| 66.5 | 14777.2170 | 0.0048 | 14810.3038 | 0.0020 | 14810.8664 | -0.0003 | | |
| 67.5 | 14777.1256 | 0.0019 | 14810.7018 | -0.0010 | 14811.2785 | -0.0016 | 14879.2588 | 0.0006 |
| 68.5 | | | 14811.1139 | 0.0001 | 14811.6984 | -0.0050 | 14880.6528 | 0.0019 |
| 69.5 | 14776.9795 | 0.0024 | 14811.5335 | -0.0012 | 14812.1337 | -0.0030 | 14882.0735 | 0.0007 |
| 70.5 | 14776.9197 | 0.0008 | 14811.9617 | -0.0039 | 14812.5782 | -0.0017 | 14883.4956 | 0.0016 |
| 71.5 | | | 14812.4033 | -0.0030 | 14813.0274 | -0.0056 | 14884.9246 | 0.0003 |
| 72.5 | | | 14812.8532 | -0.0038 | 14813.4949 | -0.0012 | 14886.3639 | 0.0001 |
| 73.5 | | | 14813.3158 | -0.0019 | 14813.9713 | 0.0022 | | |
| 74.5 | | | 14813.7852 | -0.0030 | | | | |

The dipole moment of SrOH has not been measured. However, the dipole moment for the isoelectronic molecule SrF was found to be 3.47 D (23). The value for SrOH is likely to be smaller, probably around 2–3 Debye. The calculated frequencies will aid in a search for the microwave spectrum in either the laboratory or in extraterrestrial sources.

C. Relative Intensities

The first FT spectrum was recorded with excitation at the P_1 , Q_{12} bandhead. The corresponding R_1 branch shows strong resonant lines between J of 10.5 and 32.5. The intensities of the P_{12} , Q_1 , and R_{12} branches which originate from the other lambda-

TABLE III

Molecular Constants for the 000-000 Band of the $\tilde{A}^2\Pi-\tilde{X}^2\Sigma^+$ Transition of SrOH
(in cm^{-1} ; one standard deviation in parentheses)

| Constant | $\tilde{X}^2\Sigma^+ 000$ | $\tilde{A}^2\Pi 000$ |
|------------------------|---------------------------|----------------------|
| T_0 | 0.0 | 14 674.332(2) |
| B_0 | 0.2492032(27) | 0.2538873(27) |
| $D_0 \times 10^7$ | 2.1801(30) | 2.1735(30) |
| $\gamma_0 \times 10^3$ | 2.4273(53) | - |
| P_0 | - | -0.1432006(86) |
| $q_0 \times 10^4$ | - | -2.0000(133) |
| A_0 | - | 263.51741(34) |
| $A_J \times 10^5$ | - | 7.0046(68) |

doubling component (f) show a Boltzmann distribution ($T \approx 500$ K) of population in the excited state f levels. The peak e/f population ratio is about 3/1, but the f levels could not have been populated directly by the laser. There is, however, no evidence of resonant ($\Delta J = 0$) transfer of population between the e and f levels since the distributions are different. However, the presence of a substantial Boltzmann population in the f component does suggest that the e and f levels communicate with each other.

The second FT spectrum was recorded with excitation of the $^3P_1-^1S_0$ Sr line at 6892 Å. There is no overlap of this line with the spectrum of SrOH. However, the P_{12} bandhead is only 0.4 cm^{-1} away so that it was excited by the 1-cm^{-1} -bandwidth dye laser. The lines with $J' = 83.5-96.5$ which could have been directly excited are not the strongest lines, however; instead, the maximum occurs at $J' = 71.5$, as can be seen in Fig. 3. The most reasonable explanation of this is that a partial relaxation of the population has occurred. In the limit of an infinite number of collisions, a Boltzmann

TABLE IV

Predicted Pure Rotational Transitions of SrOH (in MHz)

| Transition $N+1 \leftarrow N$ | Predicted Frequency | |
|----------------------------------|---------------------|------------------|
| | $F_1 - F_1(e-e)$ | $F_2 - F_2(f-f)$ |
| 1-0 | 14 979. | - |
| 2-1 | 29 921. | 29 846. |
| 3-2 | 44 862. | 44 787. |
| 4-3 | 59 803. | 59 728. |
| 5-4 | 74 743. | 74 669. |
| 6-5 | 89 683. | 89 608. |
| 7-6 | 104 621. | 104 547. |
| 8-7 | 119 559. | 119 484. |
| 9-8 | 134 494. | 134 420. |
| 10-9 | 149 430. | 149 355. |

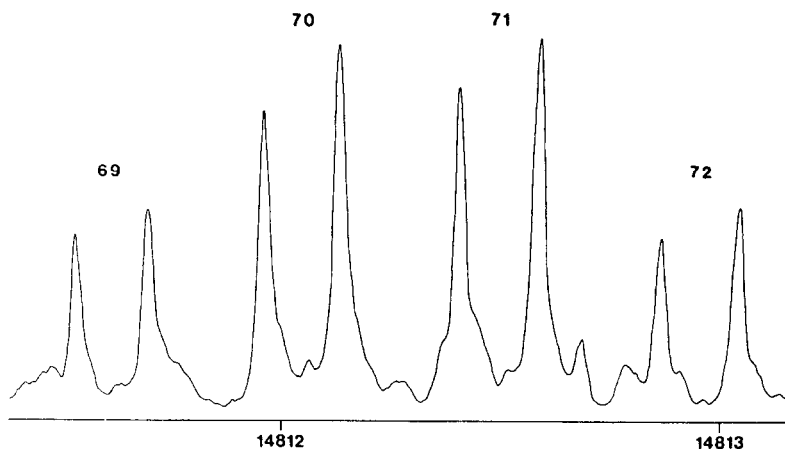


FIG. 2. A section of the Q_2 and P_{21} branches of SrOH recorded using resolved fluorescence detection. The numbers are N for the $^2\Sigma^+$ state, each transition being doubled by the ground state spin-rotation interaction.

distribution of population will occur. We appear to be looking at a situation part way between the fully relaxed and the initial laser-excited distributions. The high- J levels are well resolved in the Q_1 and R_{12} branches, shown in Fig. 4. The intensity of these transitions shows an additional maximum around $J = 88.5$ consistent with a small number of molecules emitting before undergoing collisions.

There is clear evidence in this spectrum of transfer to the e levels in the $^2\Pi$ state. In this case there is no strong Boltzmann background and the populations can be estimated fairly accurately, giving a value of 5:1 for the $f:e$ ratio. The chance of a single

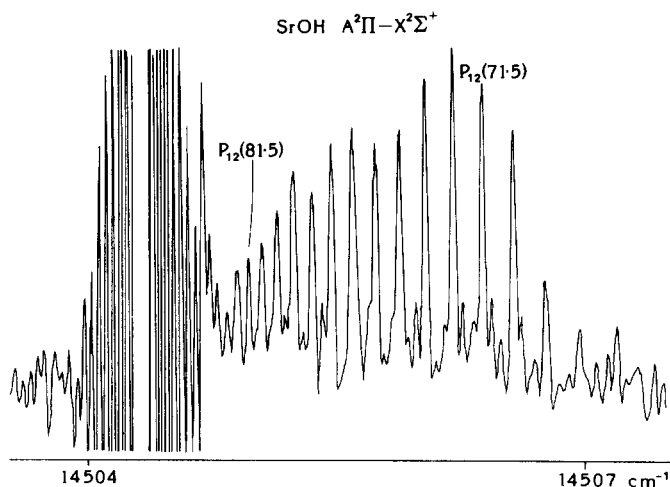


FIG. 3. Part of the Fourier transform spectrum of SrOH. Excitation is centered on the $^3P_1-^1S_0$ Sr atomic line, which is offscale by a factor of 100. The structure on this line is an instrumental artifact. At slightly higher frequency is seen the P_{12} bandhead, which is also excited by the laser. In addition there are several P_{12} lines which lie outside of the 1-cm^{-1} laser bandwidth.

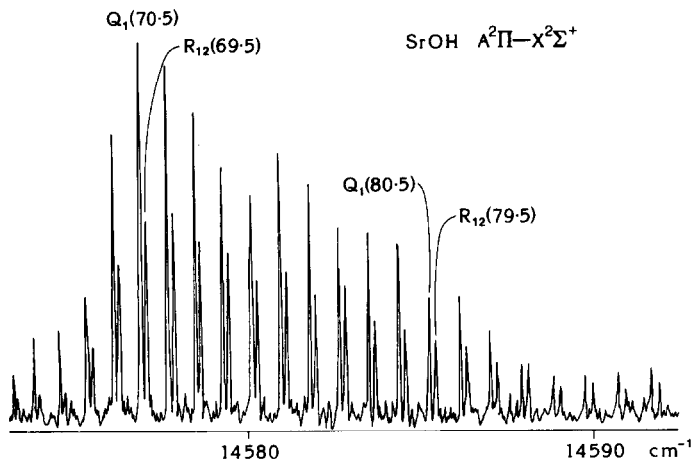


FIG. 4. A section of Fourier transform spectrum showing the Q_1 and R_{12} branches which originate from the same excited state rotational levels as shown in Fig. 3.

collision causing a change of parity must be less than this, however, as each molecule must have undergone several collisions at our pressure of 10 Torr before emitting.

There has been much interest recently in rotational energy transfer in $^2\Pi$ states of diatomic molecules (24–26), and this work represents the first observation of similar results in a triatomic species. The low propensity for e/f transfer is consistent with the qualitative explanation for other polar molecules given by Gottscho (26) and the quantitative work of Alexander (24).

It is also possible to make a comparison of the resonantly excited P_{12} , Q_1 , and R_{12} branches. For a pure case a $^2\Pi-^2\Sigma^+$ transition these should have a 1:2:1 intensity ratio. If spin–uncoupling is included in the intensity calculations (27), then the ratio becomes 1:2.6:1. The measured ratio is 1:2.6:1.6; the difference is thought to arise from a parallel contribution to the formally perpendicular transition dipole moment. Expressions for the relative intensities of $\Omega = \frac{1}{2}$ states including this effect have been derived by Kopp and Hougen (28). Their expressions do not include spin–uncoupling, but as the ratio of P/R does not change due to uncoupling, an estimate of μ_{\parallel} may be made from the relative intensities of these two branches. The calculation gives

$$\mu_{\perp}/\mu_{\parallel} = 9.3.$$

This contribution arises from contamination of the $^2\Pi_{1/2}$ state by spin–orbit mixing [$A(L_{-}S_{+} + L_{+}S_{-})$] with the $\tilde{B}^2\Sigma^+$ state. The wavefunction for the \tilde{A} state acquires a proportion of $^2\Sigma$ character and μ_{\parallel} can then make a contribution to the overall transition moment.

IV. CONCLUSION

The rotational analysis of the $\tilde{A}^2\Pi-\tilde{X}^2\Sigma^+$ system of SrOH has been performed by laser spectroscopic techniques. Laser-induced fluorescence from gas-phase free radicals has been detected by Fourier transform spectroscopy for the first time. The coupling of these two techniques gives the FT advantage of simultaneous recording of a large number of lines together with the simplification due to the selectivity of laser excitation.

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REFERENCES

1. J. F. W. HERSCHEL, *Trans. Roy. Soc. (Edinburgh)* **9**, 445-460 (1823).
2. C. G. JAMES AND T. M. SUGDEN, *Nature (London)* **175**, 333-334 (1955).
3. R. F. WORMSBECHER, M. TRKULA, C. MARTNER, R. E. PENN, AND D. O. HARRIS, *J. Mol. Spectrosc.* **97**, 29-36 (1983).
4. J. NAKAGAWA, R. F. WORMSBECHER, AND D. O. HARRIS, *J. Mol. Spectrosc.* **97**, 37-64 (1983).
5. R. C. HILBORN, ZHU QINGSHI, AND D. O. HARRIS, *J. Mol. Spectrosc.* **97**, 73-91 (1983).
6. YONG NI AND D. O. HARRIS, "The Structure of the Alkaline Earth Monohydroxides: MgOH and MgOD," in preparation.
7. P. F. BERNATH AND S. M. KINSEY-NIELSEN, *Chem. Phys. Lett.* **105**, 663-666 (1984).
8. P. F. BERNATH AND C. R. BRAZIER, *Astrophys. J.* **288**, 373-376 (1985).
9. S. M. KINSEY-NIELSEN, C. R. BRAZIER, AND P. F. BERNATH, "Rotational Analysis of the $\tilde{B}^2\Sigma^+-\tilde{X}^2\Sigma^+$ Transition of BaOH and BaOD," *J. Chem. Phys.*, accepted for publication.
10. J. B. WEST, R. S. BRADFORD, J. D. EVERSOLE, AND C. R. JONES, *Rev. Sci. Instrum.* **46**, 164-168 (1975).
11. E. MURAD, *J. Chem. Phys.* **75**, 4080-4085 (1981).
12. C. LINTON, *J. Mol. Spectrosc.* **69**, 351-364 (1978).
13. M. DULICK, P. F. BERNATH, AND R. W. FIELD, *Canad. J. Phys.* **58**, 703-712 (1980).
14. S. GERSTENKORN AND P. LUC, "Atlas du Spectre d'Absorption de la Molecule d'Iode." Laboratoire Amie-Cotton, CNRS 9145 Orsay, France.
15. S. GERSTENHORN AND P. LUC, *Rev. Phys. Appl.* **14**, 791-796 (1979).
16. G. HERZBERG, "Spectra of Diatomic Molecules," 2nd ed., p. 257, Van Nostrand-Reinhold, New York, 1950.
17. R. S. MULLIKEN, *J. Chem. Phys.* **23**, 1997-2011 (1955).
18. G. HERZBERG, "Electronic Spectra and Electronic Structure of Polyatomic Molecules," p. 152, Van Nostrand-Reinhold, New York, 1966.
19. G. FISCHER, "Vibronic Coupling," p. 136, Academic Press, New York, 1984.
20. R. N. ZARE, A. L. SCHMELTEKOPF, W. J. HARROP, AND D. L. ALBRITTON, *J. Mol. Spectrosc.* **46**, 37-66 (1970).
21. A. J. KOTLAR, R. W. FIELD, J. I. STEINFELD, AND J. A. COXON, *J. Mol. Spectrosc.* **80**, 86-108 (1980).
22. R. S. MULLIKEN AND A. CHRISTY, *Phys. Rev.* **38**, 87-119 (1931).
23. W. E. ERNST, J. KANDLER, S. KINDT, AND T. TORRING, *Chem. Phys. Lett.* **113**, 351-354 (1985).
24. M. H. ALEXANDER, *J. Chem. Phys.* **76**, 5974-5988 (1982).
25. O. NEDELEC AND J. DUFAYARD, *Chem. Phys.* **84**, 167-184 (1984).
26. R. A. GOTTSCHO, *Chem. Phys. Lett.* **81**, 66-69 (1981).
27. L. T. EARLS, *Phys. Rev.* **48**, 423-424 (1935).
28. I. KOPP AND J. T. HOUGEN, *Canad. J. Phys.* **45**, 2581-2596 (1967).