

# The Emission Spectrum of Hot Water in the Region between 370 and 930 $\text{cm}^{-1}$

Oleg L. Polyansky,\* Jennifer R. Busler,† Bujin Guo,† Keqing Zhang,† and Peter F. Bernath†‡

\*Physical Chemistry Institute, Justus Liebig University Giessen, Heinrich-Buff-Ring 58, D-35392 Giessen, Germany; †Departments of Chemistry and Physics, University of Waterloo, Waterloo, Ontario, Canada N2L 3G1; and ‡Department of Chemistry, University of Arizona, Tucson, Arizona 85721

Received September 6, 1995; in revised form December 5, 1995; accepted December 7, 1995

An emission spectrum of the water molecule at a temperature of 1550°C has been recorded in the range from 373 to 933  $\text{cm}^{-1}$ . More than 4000 pure rotational lines were observed with the strongest belonging to the ground state (000) and the first excited bending vibrational level (010). Transitions involving rotational quantum numbers  $J$  and  $K_a$  significantly higher than previously recorded have been assigned. © 1996 Academic Press, Inc.

## I. INTRODUCTION

The pure rotational spectrum of water at room temperature has been studied in the millimeter wave, submillimeter wave, and far infrared regions (1–9). Even more studies have been devoted to the rovibrational bands of water (10–21) including overtones with wavenumbers as high as 25 000  $\text{cm}^{-1}$ . Among the IR and near IR studies are the classic works by Flaud, Camy-Peyret, and co-workers (10, 11) on the oxyacetylene flame spectra of water at temperatures as high as 2900 K. Information on the energy levels for high values of the rotational quantum numbers  $J$  and  $K_a$  are derived mostly from the transitions in these flame spectra. The ground state energy levels up to  $J = 35$  and  $K_a = 20$  were derived in Ref. (10) and the levels of the first excited bending state (010) up to  $J = 32$  and  $K_a = 14$  were reported in Ref. (11). These energy levels were used for a comprehensive atlas of the water lines (22) and for the assignment of a hot water spectrum (9).

The energy levels derived from the flame spectra have been used in numerous theoretical papers, in which effective Hamiltonians were developed for the theoretical treatment of the highly excited rotational states of water molecule (3, 4, 23–27). Within the framework of the variational approach, the fitting of the potential energy surface of water was accomplished using these energy levels as the input data (28–34).

Experimental information on highly excited rotational levels of water in the ground and lower vibrational states is very important and is widely used in many applications. For example, the infrared spectrum of a sunspot (36, 37) contains thousands of molecular absorption features. Many of these lines belong to the water molecule but most of the lines do not have rovibrational assignments. This spectrum awaits detailed assignment and the obvious step toward this goal is the study of the high temperature water spectrum in the laboratory.

The present study of the hot water spectrum was motivated both by the desire to extend the rotational energy levels higher than those reported in the literature and by the necessity of understanding the sunspot spectrum in more detail.

## II. EXPERIMENTAL DETAILS

A high resolution emission spectrum of hot  $\text{H}_2\text{O}$  was recorded with the Bruker IFS 120 HR Fourier transform spectrometer located at the University of Waterloo. The spectrum was recorded using a KBr beamsplitter with a liquid helium cooled Si:B detector in the region 350–1000  $\text{cm}^{-1}$  with a resolution of 0.01  $\text{cm}^{-1}$ . The lower limit of the spectrum was set by the transmission of the KBr beamsplitter and the detector response, while the upper limit was determined by a cold filter.

Water vapor flowed continuously from a room temperature glass container into the hot cell. The cell was a 1.2 m long by 5 cm diameter mullite ( $3\text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2$ ) tube with KRS-5 windows attached at each end. The mullite tube was placed inside a commercial CM Rapid Temperature Furnace and the pressure maintained at approximately 15 Torr with a vacuum pump. The tube was slowly heated to a temperature of 1550°C. It was necessary to have a constant flow of water vapor since the water vapor reacted rapidly with the hot walls of the tube. Higher temperatures were not obtained because the mullite tube cracked at 1550°C.

## III. ANALYSIS

The spectrum was reduced by fitting the water lines with Voigt profiles to determine line position, width, and relative intensity using PC-DECOMP, an interactive spectral analysis program developed by J. W. Brault. The laboratory data were calibrated using J. W. C. Johns'  $\text{H}_2\text{O}$  measurements (8) and a calibration factor of 1.00 004 870 768 was applied to correct the observed line positions.

TABLE 1  
Assigned Line Frequencies of the Hot Water Spectrum with Intensities Higher than 0.1 r.u.

Wavenumber	Intensity	$J'$	$K'_a$	$J$	$K_a$	$K_c$	$(0v0)$	Wavenumber	Intensity	$J'$	$K'_c$	$J$	$K_a$	$K_c$	$(0v0)$	Wavenumber	Intensity	$J'$	$K'_c$	$J$	$K_a$	$K_c$	$(0v0)$
407.30521	0.0772	19	4	16	18	3	15 (000)	499.08242	0.2584	23	5	18	22	6	17 (000)	568.30274	0.4270	15	7	8	14	6	9 (010)
418.96138	0.1094	19	4	15	18	5	14 (000)	499.78570	0.1787						OH	568.94562	0.1504	30	3	28	29	2	27 (000)
423.23867	0.0754	20	3	17	19	4	16 (000)	502.19364	0.3375	13	6	7	12	5	8 (010)	571.28617	0.1647	13	4	9	12	3	10 (000)
423.75482	0.1107	20	4	17	19	3	16 (000)	502.61196	0.1098	24	4	20	23	5	19 (000)	572.88411	0.1932	32	0	32	31	1	31 (000)
424.87537	0.1083	23	0	23	22	1	22 (000)	502.93212	0.2643	10	10	0	9	1	(010)	572.94282	0.3620	16	7	9	15	6	10 (000)
425.16224	0.1165	22	1	21	21	2	20 (010)	503.21357	0.2593	24	5	20	23	4	19 (000)	573.32095	0.1837	31	2	30	30	1	29 (000)
425.43655	0.1074	22	2	21	21	1	20 (000)	503.97049	0.1396	9	3	7	8	0	(010)	574.53908	0.3161	14	10	5	13	9	4 (000)
432.46246	0.1046						OH	504.38274	0.1514	13	5	8	12	4	9 (000)	574.55568	0.2366	14	10	4	13	9	5 (000)
433.39106	0.1044						OH	504.61545	0.2658	25	3	22	24	4	21 (000)	575.15347	0.4192	12	12	0	11	11	1 (010)
435.35756	0.1177	11	5	6	10	4	7 (010)	504.64520	0.1340	25	4	22	24	3	21 (000)	575.56939	0.3121						art
436.95054	0.1184	20	4	16	19	5	15 (000)	506.68047	0.2714	26	3	24	25	2	23 (000)	575.58194	0.3326	13	12	1	12	11	2 (000)
438.07435	0.1290	24	0	24	23	1	23 (010)	506.74287	0.1175	23	6	18	22	5	17 (000)	576.69533	0.2298	17	7	11	16	6	10 (010)
438.12334	0.1026	21	6	15	20	7	14 (000)	507.92176	0.2117	14	7	8	13	6	7 (000)	577.23550	0.3603	16	8	9	15	7	8 (000)
439.88645	0.1673	21	3	18	20	4	17 (000)	508.56081	0.2445	28	1	28	27	0	27 (000)	577.73289	0.4783	13	10	4	12	9	3 (010)
440.17247	0.1031	21	4	18	20	3	17 (000)	509.04550	0.2584	27	1	26	26	2	25 (000)	580.21560	0.4751	15	9	7	14	8	6 (000)
441.21862	0.1404	22	2	20	21	3	19 (000)	510.58378	0.1248	12	4	8	11	3	9 (000)	580.22725	0.1264						art
441.22887	0.1535	22	3	20	21	2	19 (000)	513.39309	0.2377	11	9	2	10	8	3 (010)	580.43439	0.3818	15	9	6	14	8	7 (000)
441.70186	0.1050	22	3	20	21	2	19 (010)	514.76864	0.2043	13	5	8	12	4	9 (010)	580.73232	0.1318	12	3	9	11	2	10 (000)
441.87974	0.2018	24	0	24	23	1	23 (000)	514.91255	0.1692	14	6	8	13	5	9 (000)	580.84027*	0.2818	20	7	14	19	6	13 (010)
442.21655	0.2051	20	5	16	19	4	15 (000)	517.18934	0.1398	25	4	21	24	5	20 (000)	581.00694*	0.2796	20	7	14	19	6	13 (010)
442.25198	0.1257	23	1	22	22	2	21 (010)	517.78161	0.2005	13	7	7	12	6	6 (010)	581.14986	0.2195	30	4	27	29	3	26 (000)
442.42334	0.1552	23	2	22	22	1	21 (000)	518.41450	0.1591	14	7	7	13	6	8 (000)	581.25267	0.2889	18	7	12	17	6	11 (010)
446.12087	0.1307	9	8	1	8	7	2 (010)	518.78710	0.1481	24	6	19	23	5	18 (000)	581.61518	0.3224	13	4	9	12	3	10 (010)
447.41481	0.1008	13	6	8	12	5	7 (000)	519.14188	0.2550	12	8	5	11	7	4 (010)	583.38113	0.3781	16	8	8	15	7	9 (000)
449.27890	0.2260	23	7	16	22	8	15 (000)	519.20352	0.1916	12	8	4	11	7	5 (010)	584.20394	0.3717	13	13	0	12	12	1 (000)
449.69817	0.1511	10	7	4	9	6	3 (010)	520.13515	0.1825	12	4	8	11	3	9 (010)	584.25344	0.1079	11	4	8	10	1	9 (010)
449.79489	0.1385	10	7	3	9	6	4 (010)	520.35162	0.1501	26	4	23	25	3	22 (000)	584.70802	0.1298	12	5	8	11	2	9 (000)
454.08393	0.2339	21	4	17	20	5	16 (000)	520.58546	0.2056	13	7	6	12	6	7 (010)	585.25851	0.4978	14	9	6	13	8	5 (010)
456.34126	0.1663	22	3	19	21	4	18 (000)	522.58329	0.1798	27	2	25	26	3	24 (000)	585.29478	0.3545	14	9	5	13	8	6 (010)
456.50106	0.2446	22	4	19	21	3	18 (000)	522.74032	0.2001	15	7	9	14	6	8 (000)	586.62282	0.3378	15	8	8	14	7	7 (010)
457.14058	0.1132	21	5	17	20	4	16 (000)	524.87378	0.2413	29	0	29	28	1	28 (000)	588.13178	0.4402	15	8	7	14	7	8 (010)
457.83988	0.2792	23	3	21	22	2	20 (000)	525.34551	0.2087	28	2	27	27	1	26 (000)	588.77838	0.4158	14	11	4	13	10	3 (000)
458.03151	0.1137	23	2	21	22	3	20 (010)	528.29060	0.3110	11	10	1	10	9	2 (010)	588.99047	0.1433	32	2	31	31	1	30 (000)
458.04729	0.1342	23	3	21	22	2	20 (010)	529.67325	0.1457						OH	590.63946	0.5212	13	11	3	12	10	2 (010)
458.75505	0.2546	25	0	25	24	1	24 (000)	530.54049	0.1211						OH	592.05514	0.1154	10	6	5	9	3	6 (000)
459.25771	0.1533	24	1	23	23	2	22 (010)	531.06871	0.1713						OH	592.11412	0.1537	11	5	7	10	2	8 (010)
459.79574	0.1944	15	6	10	14	5	9 (000)	532.13805	0.1699						OH	592.75489	0.2084						OH
460.83250	0.1719	21	5	16	20	6	15 (000)	532.55170	0.2063	14	6	8	13	5	9 (010)	593.70280	0.1272						OH
461.64610	0.1903	16	6	11	15	5	10 (000)	533.19198	0.3359	16	7	10	15	6	9 (000)	593.80898	0.1318						OH
462.64262	0.2112	17	6	12	16	5	11 (000)	534.24968	0.2605	13	9	5	12	8	4 (000)	593.88832	0.4256	17	8	10	16	7	9 (000)
463.14425	0.1527	11	4	7	10	3	8 (010)	534.26268	0.2398						art	594.18763	0.2485	16	7	9	15	6	10 (010)
463.30281	0.1860	9	9	0	8	8	1 (010)	534.27895	0.2706	13	9	4	12	8	5 (000)	594.94996	0.1055						OH
463.38157	0.2292	12	6	7	11	5	6 (010)	535.85486	0.2487	27	3	24	26	4	23 (000)	597.87173	0.3210						art
464.35772	0.1881	18	6	13	17	5	12 (000)	536.46687	0.1768	10	4	7	9	1	8 (010)	597.88868	0.4747	15	10	6	14	9	5 (000)
464.75076	0.1533						OH	536.61132	0.2142	11	3	8	10	2	9 (010)	597.90376	0.3303	15	10	5	14	9	6 (000)
465.87552	0.1514						OH	536.94751	0.2873	14	8	7	13	7	6 (000)	600.45911	0.4495	14	12	3	13	11	2 (000)
								537.84470	0.3694	12	9	3	11	8	4 (010)	600.66240	0.4628	16	6	10	15	5	11 (000)



TABLE 1 — Continued

Wavenumber	Intensity	J'	K' <sub>a</sub>	K' <sub>c</sub>	J	K <sub>a</sub>	K <sub>c</sub>	(0v0)	Wavenumber	Intensity	J'	K' <sub>a</sub>	K' <sub>c</sub>	J	K <sub>a</sub>	K <sub>c</sub>	(0v0)
633.09023	0.1261	12	2	10	11	1	11	(000)	702.30630	0.3356	19	11	9	18	10	8	(000)
633.81065	0.5675	14	13	1	13	12	2	(010)	702.37810	0.4514	19	11	8	18	10	9	(000)
634.59131	0.5063	15	13	2	14	12	3	(000)	703.69963	0.4930	17	17	0	16	16	1	(000)
635.11455	0.2971	12	4	9	11	1	10	(010)	703.71594	0.1567	14	4	11	13	1	12	(000)
635.39734	0.1004	12	3	10	11	0	11	(000)	703.76382	0.2503	15	6	10	14	3	11	(000)
635.94640	0.5407	16	11	5	15	10	6	(000)	704.29680	0.4268	20	10	11	19	9	10	(000)
639.09858	0.5944	15	11	4	14	10	5	(010)	705.36109	0.1135	11	5	6	10	2	9	(000)
639.25833	0.5547	14	14	0	13	13	1	(010)	705.77654	0.4767	art						art
639.97283	0.2179	13	3	10	12	2	11	(000)	705.77643	0.4861	18	13	5	17	12	6	(000)
640.88868	0.3989	18	8	11	17	7	10	(010)	706.16387	0.2940	20	10	10	19	9	11	(000)
642.01050	0.5580	15	14	1	14	13	2	(000)	707.08304	0.4109	17	13	4	16	12	5	(010)
642.23218	0.2664	13	6	8	12	3	9	(000)	707.44311	0.3722	18	11	8	17	10	7	(010)
642.65853	0.6405	18	9	10	17	8	9	(000)	707.45721	0.1447	18	11	7	17	10	8	(010)
642.78348	0.5673	17	10	8	16	9	7	(000)	707.67042*	0.2445	20	9	12	19	8	11	(010)
642.91061	0.5273	17	10	7	16	9	8	(000)	708.26088	0.2546	14	5	10	13	2	11	(010)
644.18769	0.3768	18	7	11	17	6	12	(000)	708.33956	0.2448	18	6	12	17	5	13	(000)
645.51864	0.1442	14	4	10	13	3	11	(010)	709.75494	0.2825	15	4	11	14	3	12	(010)
646.09504	0.4727	18	9	9	17	8	10	(000)	712.57127	0.2118	19	10	10	18	9	9	(010)
647.04629	0.5352	15	15	0	14	14	1	(000)	712.97183	0.3603	19	10	9	18	9	10	(010)
648.02989	0.4940	16	10	7	15	9	6	(010)	713.05216	0.4932	21	9	12	20	8	13	(000)
648.05219	0.2888	16	10	6	15	9	7	(010)	713.79192	0.2222	12	7	6	11	4	7	(000)
648.62802	0.5403	16	12	4	15	11	5	(000)	714.40047	0.4915	17	14	3	16	13	4	(010)
650.26380	0.5349	15	12	3	14	11	4	(010)	714.81549	0.6264	18	14	4	17	13	5	(000)
651.50878	0.2383	17	9	9	16	8	8	(010)	716.55537	0.6760	19	12	7	18	11	8	(000)
651.58078	0.2059	13	4	10	12	1	11	(000)	718.65746	0.3193	15	5	11	14	2	12	(000)
652.30117	0.4796	17	9	8	16	8	9	(010)	719.49361	0.4805	17	15	2	16	14	3	(010)
652.36965	0.4983	17	6	11	16	5	12	(000)	720.10263	0.4903	18	12	7	17	11	6	(010)
653.79697	0.1258							OH	721.23345	0.2598	14	6	9	13	3	10	(010)
655.47558	0.3429	17	6	11	16	5	12	(010)	721.42276	0.1431	13	7	7	12	4	8	(000)
658.69005	0.6255	17	11	6	16	10	7	(000)	721.75104	0.6394	18	15	3	17	14	4	(000)
658.87174	0.6582	19	8	11	18	7	12	(000)	722.37214	0.4364	17	17	0	16	16	1	(010)
658.87174	0.6582	15	13	2	14	12	3	(010)	722.48368	0.2880	21	10	12	20	9	11	(000)
658.91865	0.5117	16	13	3	15	12	4	(000)	722.91670	0.4218	17	16	1	16	15	2	(010)
660.42037	0.3966	19	9	11	18	8	10	(000)	723.10053	0.6088	20	11	10	19	10	9	(000)
661.48313	0.3112	20	8	13	19	7	12	(010)	723.28313	0.3919	20	11	9	19	10	10	(000)
662.48822	0.5839	16	11	5	15	10	6	(010)	726.00050	0.4869	21	8	13	20	7	14	(000)
664.19669	0.5926	18	10	9	17	9	8	(000)	726.39964	0.5578	21	10	11	20	9	12	(000)
664.53574	0.4585	18	10	8	17	9	9	(000)	726.62928	0.6715	18	16	2	17	15	3	(000)
664.77462	0.1175							art	728.28407	0.6706	19	13	6	18	12	7	(000)
664.78334	0.1161	13	5	9	12	2	10	(010)	728.56502	0.1129	14	3	11	13	2	12	(010)
665.00942	0.5423	15	14	1	14	13	2	(010)	728.95342	0.1838	19	11	9	18	10	8	(010)
666.43201	0.3017	13	3	10	12	2	11	(010)	728.99050	0.3976	19	11	8	18	10	9	(010)
666.92459	0.5867	16	14	2	15	13	3	(000)	729.41598	0.6410	18	17	1	17	16	2	(000)
667.65486	0.5083	19	9	10	18	8	11	(000)	729.94740	0.6295	18	18	0	17	17	1	(000)
668.67687	0.5493	15	15	0	14	14	1	(010)	730.22320	0.4921	18	13	6	17	12	5	(010)
670.11273	0.4234	14	6	9	13	3	10	(000)	730.54469	0.3868	14	7	8	13	4	9	(000)
670.25455	0.2865	17	10	8	16	9	7	(010)	732.44626	0.3347	20	10	11	19	9	10	(010)
763.26527	0.1852	22	11	11	21	10	12	(000)	763.26527	0.1852	22	11	11	21	10	12	(000)
763.49275	0.2520	20	12	9	19	11	8	(010)	763.49275	0.2520	20	12	9	19	11	8	(010)
763.78639	0.2249	24	10	15	23	9	14	(000)	766.73727	0.3414	19	6	13	18	5	14	(000)
766.73727	0.3414	19	6	13	18	5	14	(000)	767.14864	0.2933	23	10	13	22	9	14	(000)
767.14864	0.2933	23	10	13	22	9	14	(000)	767.20415	0.2580	19	15	5	18	14	4	(010)
767.20415	0.2580	19	15	5	18	14	4	(010)	767.26388	0.3629	16	5	12	15	2	13	(000)
767.26388	0.3629	16	5	12	15	2	13	(000)	767.30775	0.2556	23	9	14	22	8	15	(000)
767.30775	0.2556	23	9	14	22	8	15	(000)	768.02110	0.4484	20	15	5	19	14	6	(000)
768.02110	0.4484	20	15	5	19	14	6	(000)	770.08621	0.1778	19	19	1	18	18	0	(010)
770.08621	0.1778	19	19	1	18	18	0	(010)	771.40923	0.6035	21	13	8	20	12	9	(000)
771.40923	0.6035	21	13	8	20	12	9	(000)	771.75382	0.1903	19	16	4	18	15	3	(010)
771.75382	0.1903	19	16	4	18	15	3	(010)	772.57363	0.1004	16	4	12	15	3	13	(010)
772.57363	0.1004	16	4	12	15	3	13	(010)	773.63854	0.2553	19	18	2	18	17	1	(010)
773.63854	0.2553	19	18	2	18	17	1	(010)	773.83385	0.2216	19	17	3	18	16	2	(010)
773.83385	0.2216	19	17	3	18	16	2	(010)	774.00120	0.5466	20	16	4	19	15	5	(000)
774.00120	0.5466	20	16	4	19	15	5	(000)	774.53229	0.3054	20	13	8	19	12	7	(010)
774.53229	0.3054	20	13	8	19	12	7	(010)	774.53229	0.3054	20	13	8	19	12	7	(010)
774.53229	0.3054	20	13	8	19	12	7	(010)	778.11966	0.5172	20	17	3	19	16	4	(000)
778.11966	0.5172	20	17	3	19	16	4	(000)	778.70499	0.3984	20	20	1	19	19	0	(000)
778.70499	0.3984	20	20	1	19	19	0	(000)	778.77158	0.4053	22	12	11	21	11	10	(000)
778.77158	0.4053	22	12	11	21	11	10	(000)	778.88644	0.2152	22	12	10	21	11	11	(000)
778.88644	0.2152	22	12	10	21	11	11	(000)	780.37298	0.4918	20	18	2	19	17	3	(000)
780.37298	0.4918	20	18	2	19	17	3	(000)	780.66034	0.4359	20	19	2	19	18	1	(000)
780.66034	0.4359	20	19	2	19	18	1	(000)	781.79343	0.5054	21	14	7	20	13	8	(000)
781.79343	0.5054	21	14	7	20	13	8	(000)	782.44360	0.3227	23	11	12	22	10	13	(000)
782.44360	0.3227	23	11	12	22	10	13	(000)	783.29377	0.1945	21	12	9	20	11	10	(010)
783.29377	0.1945	21	12	9	20	11	10	(010)	783.48504	0.1349	20	14	7	19	13	6	(010)
783.48504	0.1349	20	14	7	19	13	6	(010)	783.76246	0.2464	17	6	12	16	3	13	(000)
783.76246	0.2464	17	6	12	16	3	13	(000)	785.57960	0.2157	16	6	11	15	3	12	(010)
785.57960	0.2157	16	6	11	15	3	12	(010)	788.38963	0.2196	15	3	12	14	2	13	(010)
788.38963	0.2196	15	3	12	14	2	13	(010)	789.94558	0.2435	20	15	6	19	14	5	(010)
789.94558	0.2435	20	15	6	19	14	5	(010)	790.12837	0.4959	21	15	6	20	14	7	(000)
790.12837	0.4959	21	15	6	20	14	7	(000)	791.49878	0.1025	0	0	0	0	0	0	art
791.49878	0.1025	0	0	0	0</												

670.31846	0.5213	17	10	7	16	9	8	(010)	732.51092	0.1988	13	2	11	12	1	12	(010)	798.36530	0.2892	23	12	11	22	11	12	(000)
671.36049	0.3754	14	5	10	13	2	11	(000)	733.38132	0.1280	20	10	10	19	9	11	(010)	798.56397	0.1383	20	18	3	19	17	2	(010)
671.75283	0.4293	18	9	10	17	8	9	(010)	734.98112	0.5245	17	5	12	16	4	13	(000)	798.75874	0.2254	15	2	13	14	1	14	(000)
671.86728	0.5751	17	12	5	16	11	6	(000)	737.79052	0.6404	19	14	5	18	13	6	(000)	799.06573	0.1118	15	3	13	14	0	14	(000)
672.67373	0.6014	16	15	1	15	14	2	(000)	737.85031	0.2445	20	7	13	19	6	14	(000)	801.21981	0.3439	21	17	4	20	16	5	(000)
673.57662	0.2120	18	9	9	17	8	10	(010)	737.95872	0.6405	20	12	9	19	11	8	(000)	801.36109	0.2363	21	21	0	20	20	1	(000)
674.15507	0.5165	16	12	4	15	11	5	(010)	737.97236	0.3222	20	12	8	19	11	9	(000)	802.81730	0.3852	22	14	8	21	13	9	(000)
674.53197	0.2964	16	5	11	15	4	12	(000)	738.04973	0.4628	18	14	5	17	13	4	(010)	802.98999	0.1725	13	7	6	12	4	9	(000)
675.62922	0.4858	20	9	12	19	8	11	(000)	738.45629	0.2110	22	9	13	21	8	14	(000)	803.50603	0.2252	16	5	12	15	2	13	(010)
676.09636	0.5364	16	16	0	15	15	1	(000)	738.47926	0.4915	22	10	13	21	9	12	(000)	804.11311	0.3531	21	18	3	20	17	4	(000)
676.55000	0.1517	12	3	10	11	0	11	(010)	740.56995	0.1629	11	7	4	10	4	7	(010)	804.19000*	0.1302	21	14	7	20	13	8	(010)
679.24772	0.1172	16	5	11	15	4	12	(010)	741.20236	0.2949	17	5	12	16	4	13	(010)	804.42324	0.3070	21	20	1	20	19	2	(000)
679.77495	0.3179	19	8	11	18	7	12	(010)	742.00289	0.2901	14	4	11	13	1	12	(010)	804.58205*	0.1103	21	14	7	20	13	8	(010)
680.81836	0.5320	18	11	8	17	10	7	(000)	742.06775	0.4951	16	6	11	15	3	12	(000)	805.22471	0.3552	21	19	2	20	18	3	(000)
680.84398	0.4064	18	11	7	17	10	8	(000)	742.12768	0.4469	19	12	8	18	11	7	(010)	805.99389	0.2177	16	3	13	15	2	14	(000)
682.24652	0.1567	12	6	7	11	3	8	(010)	742.43352	0.1039	12	6	6	11	3	9	(000)	806.69581	0.4440	17	4	13	16	3	14	(000)
682.65079	0.4845	17	13	4	16	12	5	(000)	743.12339	0.3231	21	11	11	20	10	10	(000)	808.03805	0.4137	16	4	13	15	1	14	(000)
683.29582	0.4766	16	13	3	15	12	4	(010)	743.34735	0.2416	15	7	9	14	4	10	(000)	811.55952	0.4627	22	15	7	21	14	8	(000)
684.77335	0.3801	19	10	10	18	9	9	(000)	743.57704	0.5860	21	11	10	20	10	11	(000)	811.93309	0.2835	23	13	11	22	12	10	(000)
685.28085	0.4680	17	11	6	16	10	7	(010)	743.72649	0.4309	18	15	4	17	14	3	(010)	811.96458	0.3843	23	13	10	22	12	11	(000)
685.59269	0.5134	19	10	9	18	9	10	(000)	744.21132	0.1628	14	2	12	13	1	13	(000)	811.97965	0.1856	21	15	6	20	14	7	(010)
687.47605	0.2254	21	9	13	20	8	12	(000)	744.81380	0.2705	14	3	12	13	0	13	(000)	813.75067	0.2746	23	8	15	22	7	16	(000)
687.98667	0.1086	13	4	10	12	1	11	(010)	745.23143	0.6514	19	15	4	18	14	5	(000)	814.51706	0.1330	12	8	5	11	5	6	(000)
688.33863	0.4757	19	7	12	18	6	13	(000)	746.58395	0.2422	22	10	12	21	9	13	(000)	815.30059	0.4788	18	7	12	17	4	13	(000)
689.03754	0.1578	13	2	11	12	1	12	(000)	747.31583	0.3938	18	16	3	17	15	2	(010)	816.15525	0.1429	21	16	5	20	15	6	(010)
689.72957	0.3166	20	9	11	19	8	12	(000)	747.96251	0.3273	18	18	1	17	17	0	(010)	816.45026	0.2785	17	5	13	16	2	14	(000)
690.02014	0.2722	20	8	12	19	7	13	(000)	748.78707	0.3674	18	17	2	17	16	1	(010)	816.68703	0.2957	24	12	13	23	11	12	(000)
690.05509	0.4528	16	14	3	15	13	2	(010)	749.74284	0.1273	15	6	10	14	3	11	(010)	817.15695	0.1864	24	12	12	23	11	13	(000)
690.22063	0.1359	13	3	11	12	0	12	(000)	749.77536	0.3139	20	11	10	19	10	9	(010)	817.20881*	0.1125	21	20	1	20	19	2	(010)
691.19311	0.5173	17	14	3	16	13	4	(000)	749.86908	0.1269	19	11	9	19	10	10	(010)	818.42382	0.4359	22	16	6	21	15	7	(000)
691.37971	0.1349	19	9	11	18	8	10	(010)	750.16491	0.6721	20	13	7	19	12	8	(000)	819.93233*	0.2082	21	17	4	20	16	5	(010)
691.79103	0.4157	18	10	9	17	9	8	(010)	750.69458	0.6660	19	16	3	18	15	4	(000)	822.18246*	0.1162	21	19	2	20	18	3	(010)
691.95960	0.1955	18	10	8	17	9	9	(010)	751.18495	0.3086	16	4	12	15	3	13	(000)	822.26460*	0.1341	21	18	3	20	17	4	(010)
693.11754	0.3870	15	4	11	14	3	12	(000)	752.26512	0.4034	15	3	12	14	2	13	(000)	822.95571	0.2227	22	22	0	21	1	1	(000)
693.52831	0.2483	19	7	12	18	6	13	(010)	752.71128	0.4227	19	13	7	19	12	8	(010)	823.18909	0.3983	23	14	9	22	13	10	(000)
694.48554	0.4650	16	15	2	15	14	1	(010)	752.88465	0.2351	23	10	14	22	9	13	(000)	823.53731	0.3860	22	17	5	21	16	6	(000)
694.51611	0.5792	18	12	6	17	11	7	(000)	754.20060	0.6575	19	17	2	18	16	3	(000)	825.63552	0.1842	20	6	14	19	5	15	(000)
695.28114	0.3893	22	9	14	21	8	13	(000)	754.86499	0.1329	15	5	11	14	2	12	(010)	826.13343	0.1538	16	7	10	15	4	11	(010)
696.52345	0.4286	16	16	1	15	15	0	(010)	754.92380	0.5795	19	19	0	18	18	1	(000)	826.97402	0.3396	22	18	4	21	17	5	(000)
697.05479	0.2115	14	3	11	13	2	12	(000)	755.68307	0.6026	19	18	1	18	17	2	(000)	827.04029	0.2362	22	21	1	21	20	2	(000)
697.44090	0.4530	17	12	5	16	11	6	(010)	755.98181	0.2605	15	4	12	14	1	13	(000)	827.70865	0.4713	18	6	13	17	3	14	(000)
697.56964	0.5178	17	15	3	16	14	2	(000)	758.71268	0.3065	21	12	10	20	11	9	(000)	828.75481	0.2857	22	19	3	21	18	4	(000)
697.91839	0.1411	11	6	5	10	3	8	(000)	758.73833	0.5374	21	12	9	20	11	10	(000)	828.83165	0.2512	22	20	2	21	19	3	(000)
698.46870	0.1818	23	9	15	22	8	14	(000)	760.11674	0.6202	14	6	19	13	7	(000)	831.19402	0.2332	24	13	12	23	12	11	(000)	
698.77006*	0.1111	24	9	16	23	8	15	(000)	761.00294	0.3462	19	14	6	18	13	5	(010)	832.31968	0.3132	23	15	8	22	14	9	(000)
699.65764*	0.1152	24	9	16	23	8	15	(000)	761.47289	0.4148	16	7	10	15	4	11	(000)	832.92807	0.2104	17	4	13	16	3	14	(010)
701.77622	0.4661	17	16	1	16	15	2	(000)	762.27571	0.4249	22	11	12	21	10	11	(000)	835.45046	0.1785	25	12	13	24	11	14	(000)

TABLE 1—Continued

Wavenumber	Intensity	$J'$	$K'_a$	$K'_c$	$J$	$K_a$	$K_c$	(0v0)	Wavenumber	Intensity	$J'$	$K'_a$	$K'_c$	$J$	$K_a$	$K_c$	(0v0)
835.55331	0.1698	14	8	7	13	5	8	(000)	866.17192*	0.1237	24	17	7	23	16	8	(000)
839.57208	0.2469	23	16	7	22	15	8	(000)	870.24464	0.1431	24	18	6	23	17	7	(000)
842.89688	0.1814	24	14	10	23	13	11	(000)	871.84116	0.1465	25	15	10	24	14	11	(000)
843.54665*	0.0990	23	23	0	22	22	1	(000)	872.97092*	0.1659	19	6	14	18	3	15	(000)
845.10003	0.2290	23	17	6	22	16	7	(000)	872.97092*	0.1659	24	19	5	23	18	6	(000)
845.73149	0.2045	16	8	9	15	5	10	(000)	873.05353	0.1227	24	22	2	23	21	3	(000)
848.57312	0.1310	23	22	1	22	21	2	(000)	874.39734	0.1094	24	20	4	23	19	5	(000)
849.00507	0.2276	23	18	5	22	17	6	(000)	874.93458	0.1001	19	8	12	18	5	13	(000)
849.63800	0.1830	19	7	13	18	4	14	(000)	879.79967	0.1237	25	16	9	24	15	10	(000)
849.89257	0.1712	25	13	12	24	12	13	(000)	883.07297	0.1501	15	7	8	14	4	11	(000)
850.81073	0.3964	19	5	14	18	4	15	(000)	883.31545	0.2428	21	6	15	20	5	16	(000)
850.97520	0.1951	16	4	13	15	1	14	(010)	886.04332	0.1060	25	17	8	24	16	9	(000)
851.24837	0.1203	15	2	13	14	1	14	(010)	887.40891	0.2749	20	7	14	19	4	15	(000)
851.25820	0.1511	23	21	2	22	20	3	(000)	894.63740	0.2332	20	8	13	19	5	14	(000)
851.34264	0.1973	23	19	4	22	18	5	(000)	902.29342	0.1563	17	3	14	16	2	15	(010)
851.62563	0.1010	17	8	10	16	5	11	(000)	903.53332	0.1797	18	5	14	17	2	15	(010)
852.11657	0.1721	23	20	3	22	19	4	(000)	904.62103	0.1895	23	7	16	22	6	17	(000)
852.41199	0.2496	24	15	9	23	14	10	(000)	904.67827	0.1510	20	5	15	19	4	16	(000)
852.48943	0.1386	13	8	5	12	5	8	(000)	906.22841	0.2622	17	2	15	16	1	16	(000)
852.75443	0.1181	16	2	14	15	1	15	(000)	906.30980	0.1082	17	3	15	16	0	16	(000)
852.91156	0.2601	16	3	14	15	0	15	(000)	906.75378	0.1767	15	8	7	14	5	10	(000)
858.54341	0.3281	17	3	14	16	2	15	(000)	910.05108	0.1386	16	3	14	15	0	15	(010)
859.66033	0.1621	17	4	14	16	1	15	(000)	910.09980	0.1896	18	3	15	17	2	16	(000)
859.91051	0.1718	18	4	14	17	3	15	(000)	910.71027	0.4266	18	4	15	17	1	16	(000)
860.02730	0.1827	24	16	8	23	15	9	(000)	911.23428	0.4688	19	4	15	18	3	16	(000)
860.83946	0.2427	18	8	11	17	5	12	(000)	913.98373	0.1064	13	9	4	12	6	7	(000)
861.96455	0.1274	25	14	11	24	13	12	(000)	914.60786	0.2387	19	5	15	18	2	16	(000)
864.04819	0.1623	18	6	14	17	3	14	(010)	918.82257	0.4750	20	6	15	19	3	16	(000)
864.62304*	0.1437	24	24	0	23	23	1	(000)	919.87598	0.1199	21	8	14	20	5	15	(000)
865.68669	0.3539	18	5	14	17	2	15	(000)	921.39854	0.1148	15	6	9	14	3	12	(000)
865.92987*	0.1614	24	17	7	23	16	8	(000)									

The strongest lines belong to the pure rotational spectrum of the ground (000) and first excited bending level (010). Except for some OH lines, the rest of the transitions belong to the pure rotational spectrum of higher excited vibrational levels such as (100), (020), (001) and to the rovibrational bands  $\nu_2$ ,  $2\nu_2 - \nu_2$ . About 250 lines belong to the pure rotational spectrum of water in the ground and (010) vibrational states. These lines have an intensity between 0.7 and 0.3 in relative units (r.u.). At least half of the approximately 1000 lines with an intensity between 0.3 and 0.1 also belong to these states. The lowest observable intensity was about 0.003 relative units. Some of the more than 3000 lines with intensity between 0.1 and 0.003 r.u. also belong to the ground and (010) states, but the majority of them are due to the pure rotational transitions of higher vibrational states and rovibrational bands.

Lines with  $J$  rotational quantum numbers between 9 and 13, which are quite strong in room temperature spectra, suffered from self absorption caused by cooler water at the ends of the cell, atmospheric water and trace amounts of water in the spectrometer. Because of the Doppler effect, the high temperature emission lines are broader than the cooler absorption lines. The cooler water thus removes the line center

from the emission lines, resulting in doublet line artifacts. As a rule, the line centers of these doublets were found to be shifted to the right and to the left by approximately  $0.005 \text{ cm}^{-1}$  from the line center of the room temperature transition. For completeness they are listed in Table 1 and the weaker components of such artifact doublets are marked by the letters "art."

A comprehensive analysis of the present spectrum would require a reliable calculation of the energy levels for the first few vibrational states up to very high values of the rotational quantum numbers. This could be done using variational calculations, since this approach allows the simultaneous calculation of energy levels and intensities of the lines. The only problem is the accuracy of the potential energy and dipole moment surfaces. Recently (34) a potential energy surface good enough to reliably predict highly excited rotational states has been obtained. Reliable dipole moment surfaces are also available (35). Work on the comprehensive assignment of all the lines in the present spectrum is underway.

Nevertheless, the assignment of the strongest lines of the spectrum, belonging to the ground and (010) states, can be achieved using both the available experimental energy levels

TABLE 2

Energy Levels of Water (in cm<sup>-1</sup>) Obtained from the Wavenumbers of the Hot Water Spectrum for the Ground Vibrational State

<i>J</i>	<i>K<sub>a</sub></i>	<i>K<sub>c</sub></i>	Position		<i>J</i>	<i>K<sub>a</sub></i>	<i>K<sub>c</sub></i>	Position		<i>J</i>	<i>K<sub>a</sub></i>	<i>K<sub>c</sub></i>	Position		<i>J</i>	<i>K<sub>a</sub></i>	<i>K<sub>c</sub></i>	Position	
14	0	14	2073.5180	a	16	5	11	3758.4050		18	6	12	4735.8490		20	3	17	5031.7959	d
14	1	14	2073.5187	a	16	6	11	3822.2508		18	7	12	4833.2126		20	4	17	5031.9799	
14	1	13	2327.8912	a	16	6	10	3870.2046		18	7	11	4865.2257		20	4	16	5292.1024	
14	2	13	2327.9141	a	16	7	10	4006.0755		18	8	11	5035.1322		20	5	16	5294.0407	
14	2	12	2550.8847		16	7	9	4016.1333		18	8	10	5040.8622		20	5	15	5513.2355	
14	3	12	2551.4857		16	8	9	4206.3336		18	9	10	5255.4518		20	6	15	5527.0467	
14	3	11	2739.4293		16	8	8	4207.5526		18	9	9	5256.1166		20	6	14	5680.7874	d
14	4	11	2746.0276		16	9	8	4427.1244		18	10	9	5495.0933		20	7	14	5739.2347	
14	4	10	2880.8372		16	9	7	4427.2339		18	10	8	5495.1411		20	7	13	5812.0743	d
14	5	10	2918.2482		16	10	7	4665.9732		18	11	8	5750.8534		20	8	13	5947.3100	
14	5	9	2983.3948		16	10	6	4665.9822		18	11	7	5750.8614		20	8	12	5966.8266	d
14	6	9	3084.8380		16	11	6	4919.2577	c	18	12	7	6019.1794	c	20	9	12	6167.7135	
14	6	8	3101.4312		16	11	5	4919.2577	c	18	12	6	6019.1794	c	20	9	11	6170.8317	
14	7	8	3264.3393		16	12	5	5183.5801	c	18	13	6	6296.9014	c	20	10	11	6407.0839	d
14	7	7	3266.5204		16	12	4	5183.5801	c	18	13	5	6296.9014	c	20	10	10	6407.4464	d
14	8	7	3464.8864		16	13	4	5455.8871	c	18	14	5	6581.0464	c	20	11	10	6664.1450	
14	8	6	3465.0711		16	13	3	5455.8871	c	18	14	4	6581.0464	c	20	11	9	6664.1731	
14	9	6	3685.4075		16	14	3	5733.1485	c	18	15	4	6868.8312	c	20	12	9	6935.4198	
14	9	5	3685.4245		16	14	2	5733.1485	c	18	15	3	6868.8312	c	20	12	8	6935.4301	
14	10	5	3922.3192		16	15	2	6012.3464	c	18	16	3	7157.3474	c	20	13	8	7217.5737	c
14	10	4	3922.3324		16	15	1	6012.3464	c	18	16	2	7157.3474	c	20	13	7	7217.5737	c
14	11	4	4172.1503	c	16	16	1	6290.1968	c	18	17	2	7443.5386	c	20	14	7	7507.5802	c
14	11	3	4172.1503	c	16	16	0	6290.1968	c	18	17	1	7443.5386	c	20	14	6	7507.5802	c
14	12	3	4431.6326	c	17	0	17	2981.3630	a	18	18	1	7723.8438	c	20	15	6	7802.7130	c
14	12	2	4431.6326	c	17	1	17	2981.3631	a	18	18	0	7723.8438	c	20	15	5	7802.7130	c
14	13	2	4697.6622	c	17	1	16	3291.1485	a	19	0	19	3675.1160	a	20	16	5	8100.2790	c
14	13	1	4697.6622	c	17	2	16	3291.1522	a	19	1	19	3675.1160	a	20	16	4	8100.2790	c
14	14	1	4967.0541	c	17	2	15	3567.1783		19	1	18	4021.2177	a	20	17	4	8397.6455	c
14	14	0	4967.0541	c	17	3	15	3567.2595		19	2	18	4021.2187	a	20	17	3	8397.6455	c
15	0	15	2358.3044	a	17	3	14	3810.9396		19	2	17	4331.0723	a	20	18	3	8691.9210	c
15	1	15	2358.3047	a	17	4	14	3812.0493		19	3	17	4331.0930	a	20	18	2	8691.9210	c
15	1	14	2631.2718	a	17	4	13	4017.9118		19	3	16	4608.2251	a	20	19	2	8979.8820	c
15	2	14	2631.2816	a	17	5	13	4027.5094		19	4	16	4608.5572	d	20	19	1	8979.8820	c
15	2	13	2872.2774		17	5	12	4174.2910		19	4	15	4851.8241		20	20	1	9257.4726	c
15	3	13	2872.5837		17	6	12	4221.0380		19	5	15	4855.1519		20	20	0	9257.4726	c
15	3	12	3080.1792		17	6	11	4291.9110		19	5	14	5052.6696		21	0	21	4438.7499	a
15	4	12	3083.8730		17	7	11	4409.3477		19	6	14	5074.2243	d	21	1	21	4438.7499	a
15	4	11	3244.6032		17	7	10	4428.1191		19	6	13	5199.6023		21	1	20	4820.6444	a
15	5	11	3269.5422		17	8	10	4610.0216		19	7	13	5276.8065	d	21	2	20	4820.6447	a
15	5	10	3360.6047		17	8	9	4612.7933		19	7	12	5326.9873		21	2	19	5163.0830	a
15	6	10	3443.1905		17	9	9	4830.6054		19	8	12	5481.1021	d	21	3	19	5163.0891	a
15	6	9	3472.8835		17	9	8	4830.8966		19	8	11	5492.0843		21	3	18	5471.8634	
15	7	9	3624.1715		17	10	8	5070.0174		19	9	11	5701.2826	d	21	4	18	5471.9684	d
15	7	8	3629.0981		17	10	7	5070.0350		19	9	10	5702.7871		21	4	17	5748.1247	
15	8	8	3824.5048		17	11	7	5324.6633	c	19	10	10	5940.8900	d	21	5	17	5749.2430	d
15	8	7	3825.0000		17	11	6	5324.6633	c	19	10	9	5941.0445		21	5	16	5987.8792	
15	9	7	4045.2867		17	12	6	5591.1250	c	19	11	9	6197.4474		21	6	16	5996.5192	d
15	9	6	4045.3208		17	12	5	5591.1250	c	19	11	8	6197.4714		21	6	15	6177.3580	
15	10	6	4283.3113		17	13	5	5866.2309	c	19	12	8	6467.4088	c	21	7	15	6219.6224	d
15	10	5	4283.3132		17	13	4	5866.2309	c	19	12	7	6467.4088	c	21	7	14	6318.5564	
15	11	5	4534.9521	c	17	14	4	6147.0802	c	19	13	7	6747.4635	c	21	8	14	6433.1124	d
15	11	4	4534.9521	c	17	14	3	6147.0802	c	19	13	6	6747.4635	c	21	8	13	6465.2352	d
15	12	4	4796.9684	c	17	15	3	6430.7181	c	19	14	6	7034.6919	c	21	9	13	6654.3026	d
15	12	3	4796.9684	c	17	15	2	6430.7181	c	19	14	5	7034.6919	c	21	9	12	6660.3621	d
15	13	3	5066.2239	c	17	16	2	6714.1226	c	19	15	5	7326.2778	c	21	10	12	6893.2154	d
15	13	2	5066.2239	c	17	16	1	6714.1226	c	19	15	4	7326.2778	c	21	10	11	6894.1131	d
15	14	2	5339.6727	c	17	17	1	6993.8964	c	19	16	4	7619.5258	c	21	11	11	7150.5698	d
15	14	1	5339.6727	c	17	17	0	6993.8964	c	19	16	3	7619.5258	c	21	11	10	7150.6609	d
15	15	1	5614.1004	c	18	0	18	3319.4512	a	19	17	3	7911.5480	c	21	12	10	7422.8833	c
15	15	0	5614.1004	c	18	1	18	3319.4512	a	19	17	2	7911.5480	c	21	12	9	7422.8858	c
16	0	16	2660.9497	a	18	1	17	3647.4632	a	19	18	2	8199.2217	c	21	13	9	7706.8290	c
16	1	16	2660.9499	a	18	2	17	3647.4651	a	19	18	1	8199.2217	c	21	13	8	7706.8290	c
16	1	15	2952.3890	a	18	2	16	3940.5440	a	19	19	1	8478.7676	c	21	14	8	7999.3671	c
16	2	15	2952.3962	a	18	3	16	3940.5898	a	19	19	0	8478.7676	c	21	14	7	7999.3671	c
16	2	14	3211.0591		18	3	15	4201.2520		20	0	20	4048.2524	a	21	15	7	8297.7086	c
16	3	14	3211.2160		18	4	15	4201.8588		20	1	20	4048.2524	a	21	15	6	8297.7086	c
16	3	13	3437.2755		18	4	14	4427.1700		20	1	19	4412.3168	a	21	16	6	8599.2846	c
16	4	13	3439.3099		18	5	14	4432.8650		20	2	19	4412.3173	a	21	16	5	8599.2846	c
16	4	12	3623.7687		18	5	13	4606.1709		20	2	18	4738.6237	a	21	17	5	8901.4988	c
16	5	12	3639.5413		18	6	13	4638.6487		20	3	18	4738.6359	a	21	17	4	8901.4988	c

TABLE 2—Continued

$J$	$K_a$	$K_c$	Position		$J$	$K_a$	$K_c$	Position	
21	18	4	9201.7586	c	23	9	15		
21	18	3	9201.7586	c	23	9	14	7704.7196	d
21	19	3	9497.1457	c,d	23	10	14	7924.4534	d
21	19	2	9497.1457	c,d	23	10	13	7927.6649	d
21	20	2	9784.3052	c,d	23	11	13		
21	20	1	9784.3052	c,d	23	11	12	8181.6850	d
21	21	1	10058.8367	c,d	23	12	12	8454.6036	d
21	21	0	10058.8367	c,d	23	12	11	8454.7541	d
22	0	22	4846.4961	a	23	13	11	8741.3893	d
22	1	22	4846.4961	a	23	13	10	8741.3971	d
22	1	21	5246.0810		23	14	10	9038.0521	c
22	2	21	5246.0810		23	14	9	9038.0521	c
22	2	20	5604.3077		23	15	9	9341.9660	c
22	3	20	5604.3119		23	15	8	9341.9660	c
22	3	19	5928.3096	d	23	16	8	9650.4987	c
22	4	19	5928.3645		23	16	7	9650.4987	c
22	4	18	6219.8886		23	17	7	9961.2324	c
22	5	18	6220.5425		23	17	6	9961.2324	c
22	5	17	6476.8335	d	23	18	6	10271.8270	c
22	6	17	6482.1609	d	23	18	5	10271.8270	c
22	6	16			23	19	5	10579.8154	c,d
22	7	16	6717.1790	d	23	19	4	10579.8154	c,d
22	7	15			23	20	4	10882.6300	c,d
22	8	15	6937.4118	d	23	20	3	10882.6300	c,d
22	8	14			23	21	3	11177.2356	c,d
22	9	14	7160.5163	d	23	21	2	11177.2356	c,d
22	9	13	7171.5687	d	23	22	2	11459.9186	c,d
22	10	13	7399.2414	d	23	22	1	11459.9186	c,d
22	10	12	7400.8866	d	23	23	1	11725.3390	c,d
22	11	12	7656.3888	d	23	23	0	11725.3390	c,d
22	11	11	7656.4807	d	24	0	24	5713.2512	
22	12	11	7929.4325		24	1	24	5713.2512	
22	12	10	7929.4562		24	1	23	6147.7603	
22	13	10	8214.8630		24	2	23	6147.7603	
22	13	9	8214.9012		24	2	22	6536.4428	
22	14	9	8509.6463	c	24	3	22	6536.4428	
22	14	8	8509.6463	c	24	3	21	6889.7206	d
22	15	8	8810.9266	c	24	4	21	6889.7365	d
22	15	7	8810.9266	c	24	4	20	7210.3312	d
22	16	7	9116.1324	c	24	5	20	7210.5562	
22	16	6	9116.1324	c	24	5	19		
22	17	6	9422.8219	c	24	6	19		
22	17	5	9422.8219	c	24	6	18		
22	18	5	9728.4728	c	24	7	18		
22	18	4	9728.4728	c	24	7	17		
22	19	4	10030.5134	c,d	24	8	17		
22	19	3	10030.5134	c,d	24	8	16		
22	20	3	10325.9774	c,d	24	9	16		
22	20	2	10325.9774	c,d	24	9	15		
22	21	2	10611.3455	c,d	24	10	15	8468.5060	d
22	21	1	10611.3455	c,d	24	10	14		
22	22	1	10881.7924	c,d	24	11	14	8724.8531	d
22	22	0	10881.7924	c,d	24	11	13		
23	0	23	5271.3715		24	12	13	8998.3720	d
23	1	23	5271.3715		24	12	12		
23	1	22	5688.5026		24	13	12	9285.9481	d
23	2	22	5688.5026		24	13	11		
23	2	21	6062.1467		24	14	11	9584.2862	c
23	3	21	6062.1467		24	14	10	9584.2862	c
23	3	20	6400.9785		24	15	10	9890.4641	c
23	4	20	6401.0138	d	24	15	9	9890.4641	c
23	4	19	6707.3426		24	16	9	10201.9933	c
23	5	19	6707.7192	d	24	16	8	10201.9933	c
23	5	18	6980.3242	d	24	17	8	10516.4286	c,d
23	6	18	6983.5764	d	24	17	7	10516.4286	c,d
23	6	17	7211.3501	d	24	18	7	10831.4770	c,d
23	7	17			24	18	6	10831.4770	c,d
23	7	16			24	19	6	11144.7979	c,d
23	8	16			24	19	5	11144.7979	c,d
23	8	15	7530.9297	d	24	20	5	11454.2127	c,d

<sup>a</sup> Energy levels taken from Ref. 10. <sup>c</sup> Energy levels obtained using unresolved doublets. <sup>d</sup> Energy levels which were not known previously.

(10, 11) and by extrapolation these levels and other available experimental data (I–II) using an effective Hamiltonian model.

In this work, the Padé–Borel (4, 24) method for the summation of the divergent perturbative effective Hamiltonian of the water molecule has been employed. A model with 30 parameters for fitting the available ground state data and 24 parameters for the (010) data was used. Recently very accurate fits to the available data on the ground and (010) states of water were achieved by Coudert (27). Accuracy close to the experimental error was obtained using a modified, exactly solvable model by Makarevich (38) with 36 parameters for the (000) state and 31 for (010) state respectively. Our use of a 30 (000) and 24 (010) constant Padé–Borel model resulted in somewhat lower accuracy—up to a few wave-numbers for the calculation of the highest rotational quantum numbers levels obtained in this work. One of the reasons for this is the smaller number of fitted parameters. However, in most cases, this accuracy was enough for the assignment of the lines. Only in a few cases, involving the highest  $J$  and  $K_a$  quantum numbers, was the assignment ambiguous (see below). The transitions involving the rotational levels of the (000) and (010) vibrational states with rotational quantum numbers significantly higher than previously observed (10, 11) were assigned. In particular, transitions involving high  $J$  and high  $K_a$  ( $\approx J$ ) were assigned up to  $J = 25$  for the (000) state and for  $J = 21$  for the (010) state. Levels up to  $K_a = 20$  (000) and  $K_a = 14$  (010) were previously known (10, 11). Some higher  $J$ ,  $K_a$  transitions were also assigned; however, their intensities are lower than 0.1 r.u. and their assignment is less certain.

The measured values of the most intense (down to 0.1 r.u.) transition frequencies, together with their rotational quantum numbers, are presented in Table 1.<sup>1</sup> In a few cases, indicated by an asterisk, there is more than one candidate line for an assignment. More accurate variational calculations and/or the measurement of lines in other spectral regions will lead to the elimination of the ambiguity in the assignment as well as to the assignment of the weaker lines in the spectrum. The assignment of the lines of the (020) state and of the  $\nu_2$  vibration–rotation lines was made using the available literature data (22). These lines and the additional lines of the (000) and (010) levels weaker than 0.1 r.u. will be presented in a separate publication.

The water energy levels derived from the new transitions of Table 1 are presented in Tables 2 and 3. These energy levels were obtained from the observed lines by the addition of the lower state energy levels either taken from the work of Flaud *et al.* (10) for the 000 vibrational level and Camy-Peyret *et al.* (11) for the 010 level or, if available, from the energy levels obtained in this work. We do not list the lower  $J$  energy levels since they are

<sup>1</sup> The full line list is available from the Depository of Unpublished Data and from the authors on request.



**TABLE 3**  
**Energy Levels of Water (in cm<sup>-1</sup>) Obtained from the Wavenumbers of the Hot Water Spectrum for the**  
**Excited Vibrational State (010)**

<i>J</i>	<i>K<sub>a</sub></i>	<i>K<sub>c</sub></i>	Position		<i>J</i>	<i>K<sub>a</sub></i>	<i>K<sub>c</sub></i>	Position		<i>J</i>	<i>K<sub>a</sub></i>	<i>K<sub>c</sub></i>	Position	
12	0	12	3144.5732	a	14	10	5	5721.1016	c	18	18	1	9695.4142	c,d
12	1	12	3144.5794	a	14	10	4	5721.1016	c	18	18	0	9695.4142	c,d
12	1	11	3386.0534	a	14	11	4	5996.6928	c	19	0	19	5241.7443	a
12	2	11	3386.3820	a	14	11	3	5996.6928	c	19	1	19	5241.7443	a
12	2	10	3587.6693	a	14	12	3	6280.5557	c	19	1	18	5632.0440	a
12	3	10	3592.4256	a	14	12	2	6280.5557	c	19	2	18	5632.0475	a
12	3	9	3738.5437	a	14	13	2	6569.4213	c,d	19	2	17	5970.9398	a
12	4	9	3770.8807	a	14	13	1	6569.4213	c,d	19	3	17	5970.9971	a
12	4	8	3843.4063	a	14	14	1	6859.8792	c	19	3	16		
12	5	8	3940.5212	a	14	14	0	6859.8792	c	19	4	16		
12	5	7	3959.2550	a	15	0	15	3937.5753	a	19	4	15	6525.0581	a
12	6	7	4123.2876	a	15	1	15	3937.5753	a	19	5	15		
12	6	6	4125.5965	a	15	1	14	4243.1121	a	19	5	14		
12	7	6	4329.3258	a	15	2	14	4243.1622	a	19	6	14		
12	7	5	4329.4988	a	15	2	13	4506.7671	a	19	6	13		
12	8	5	4557.5457	a	15	3	13	4507.5223	a	19	7	13		
12	8	4	4557.5585	a	15	3	12	4728.3037	a	19	7	12	7023.9820	d
12	9	4	4803.8217	c	15	4	12			19	8	12		
12	9	3	4803.8217	c	15	4	11	4894.5909	a	19	8	11	7226.7763	d
12	10	3	5064.1338	c	15	5	11	4938.2569	a	19	9	11		
12	10	2	5064.1338	c	15	5	10	5015.7065	a	19	9	10		
12	11	2	5334.8713	c	15	6	10	5132.5025	a	19	10	10	7738.0462	d
12	11	1	5334.8713	c	15	6	9	5152.9667	a	19	10	9	7738.1306	d
12	12	1	5612.4869	c	15	7	9	5339.4931	a	19	11	9	8022.2966	d
12	12	0	5612.4869	c	15	7	8	5342.3487	a	19	11	8	8022.3013	d
13	0	13	3391.1305	a	15	8	8	5568.0938	a	19	12	8	8318.4672	c,d
13	1	13	3391.1349	a	15	8	7	5568.3568	a	19	12	7	8318.4672	c,d
13	1	12	3654.0504	a	15	9	7	5817.0792	a	19	12	6	8623.2247	c,d
13	2	12	3654.2181	a	15	9	6	5817.1001	a	19	13	7	8623.2247	c,d
13	2	11	3877.0903	a	15	10	6	6082.4127	c	19	13	6	8933.5679	c,d
13	3	11	3879.7199	a	15	10	5	6082.4127	c	19	14	5	8933.5679	c,d
13	3	10	4052.8140	a	15	11	5	6360.2002	c	19	15	4	9246.6922	c,d
13	4	10	4074.0401	a	15	11	4	6360.2002	c	19	15	3	9246.6922	c,d
13	4	9	4174.0408	a	15	12	4	6646.9566	c	19	16	2	9560.1332	c,d
13	5	9	4252.4526	a	15	12	3	6646.9566	c,d	19	16	1	9560.1332	c,d
13	5	8	4285.6493	a	15	13	3	6939.4274	c,d	19	16	0	9870.1257	c,d
13	6	8	4437.4014	d	15	13	2	6939.4274	c,d	19	17	2	9870.1257	c,d
13	6	7	4442.7148	d	15	14	2	7234.4307	c,d	19	17	1	10174.2585	c,d
13	7	7	4643.3781	d	15	14	1	7234.4307	c,d	19	18	2	10174.2585	c,d
13	7	6	4643.8731	d	15	15	1	7528.5561	c,d	19	18	1	10174.2585	c,d
13	8	6	4871.9516	d	15	15	0	7528.5561	c,d	19	19	0	10465.5004	c,d
13	8	5	4871.9807	d	15	15	0	7528.5561	c,d	19	19	0	10465.5004	c,d
13	9	5	5119.3779	c	16	0	16	4237.3240	a	18	2	17	5611.3316	a
13	9	4	5119.3779	c	16	1	16	4237.3245	a	18	2	16	5611.3316	a
13	10	4	5381.5546	c	16	1	15	4564.0860	a	18	3	16	6022.7991	a
13	10	3	5381.5546	c	16	2	15	4564.1140	a	18	3	15	6022.8011	a
13	11	3	5654.7733	c	16	2	14	4847.1880	a	18	4	15	6379.3666	a
13	11	2	5654.7733	c	16	3	14	4847.6264	a	18	4	14	6379.4036	a
13	12	2	5935.6106	c	16	3	13	5089.3832	a	18	5	14		
13	12	1	5935.6106	c	16	4	13	5094.0873	a	18	5	13		
13	13	1	6220.6209	c	16	4	12	5280.0959	a	18	6	13	6330.4537	d
13	13	0	6220.6209	c	16	5	12	5310.2731	a	18	6	12		
14	0	14	3655.5180	a	16	5	11			18	7	12	6547.0014	d
14	1	14	3655.5187	a	16	6	11	5512.0169	a	18	7	11		
14	1	13	3939.8912	a	16	6	10	5546.7429	d	18	8	11	6775.7904	d
14	2	13	3939.9141	a	16	7	10	5720.7217	d	18	8	10		
14	2	12	4183.3919	a	16	7	9	5726.6901	d	18	9	10	7025.1588	d
14	3	12	4184.8360	a	16	8	9	5949.2186	d	18	9	9	7025.4749	d
14	3	11	4382.7831	a	16	8	8	5949.8748	d	18	10	9	7293.3108	d
14	4	11	4396.0533	a	16	9	8	6198.5747	d	18	10	8	7293.3432	d
14	4	10	4525.2385	a	16	9	7	6198.6277	d	18	11	8	7576.3363	d
14	5	10	4585.3512	a	16	10	7	6465.1300	d	18	11	7	7576.3395	d
14	5	9	4638.3524	a	16	10	6	6465.1314	c,d	18	12	7	7870.5134	c,d
14	6	9	4774.0460	a	16	11	6	6744.9009	c	18	12	6	7870.5134	c,d
14	6	8	4785.0043	a	16	11	5	6744.9009	c	18	13	6	8172.5650	c,d
14	7	8	4980.2250	d	16	12	5	7034.3553	c	18	13	5	8172.5650	c,d
14	7	7	4981.4710	d	16	12	4	7034.3553	c	18	14	5	8479.4880	c,d
14	8	7	5208.8984	d	16	13	4	7330.2524	c,d	18	14	4	8479.4880	c,d
14	8	6	5208.9907	d	16	13	3	7330.2524	c,d	18	15	4	8788.3794	c,d
14	9	6	5457.2392	d	16	14	3	7629.4825	c,d	18	15	3	8788.3794	c,d
14	9	5	5457.2464	d	16	14	2	7629.4825	c,d	18	16	3	9096.2919	c,d
					16	15	2	7928.9162	c,d	18	16	2	9096.2919	c,d
										18	17	2	9400.6200	c,d
										18	17	1	9400.6200	c,d

TABLE 3—Continued

<i>J</i>	<i>K<sub>a</sub></i>	<i>K<sub>c</sub></i>	Position	<i>J</i>	<i>K<sub>a</sub></i>	<i>K<sub>c</sub></i>	Position
20	14	6	9406.7097	c,d	21	7	14
20	15	6	9723.5135	c,d	21	8	14
20	15	5	9723.5135	c,d	21	8	13
20	16	5	10041.3674	c,d	21	9	13
20	16	4	10041.3674	c,d	21	9	12
20	17	4	10357.6841	c,d	21	10	12
20	17	3	10357.6841	c,d	21	10	11
20	18	3	10668.4944	c,d	21	11	11
20	18	2	10668.4944	c,d	21	11	10
20	19	2	10972.0620	c,d	21	12	10
20	19	1	10972.0620	c,d	21	12	9
20	20	1			21	13	9
20	20	0			21	13	8
21	0	21	5998.1661	a	21	14	8
21	1	21	5998.1661	a	21	14	7
21	1	20	6430.7950	a	21	15	7
21	2	20	6430.7950	a	21	15	6
21	2	19	6804.4702	a	21	16	6
21	3	19	6804.4900	a	21	16	5
21	3	18			21	17	5
21	4	18			21	17	4
21	4	17			21	18	4
21	5	17			21	18	3
21	5	16			21	19	3
21	6	16			21	19	2
21	6	15			21	20	2
21	7	15			21	20	1

<sup>a</sup> Energy levels taken from Ref. 11.

<sup>c</sup> Energy levels obtained using unresolved doublets.

<sup>d</sup> Energy levels which were not known previously.

well known and, moreover, they are poorly determined from our emission spectra. For completeness we have added all known high *J* energy levels to Tables 2 and 3, even when our spectra do not provide new values. Note that possible confusion in the assignment of lines in Table 1 leads to ambiguities in the energy levels with the highest rotational quantum numbers of Tables 2 and 3.

#### IV. CONCLUSION

The emission spectrum of hot water (1550°C) was observed in the spectral region between 373 and 931 cm<sup>-1</sup>. The wavenumbers of more than 4000 lines with an intensity from 0.7 down to 0.003 relative units were measured. More than 600 of the strongest lines belonging to the pure rotational spectrum in the ground (000) and first excited bending (010) vibrational levels were assigned. From the line positions, energy levels of the (000) and (010) states were derived with significantly higher rotational quantum numbers than previously available.

#### ACKNOWLEDGMENTS

O.L.P. gratefully acknowledges a Humboldt Fellowship for 1993–1995, and he is grateful to the Institute of Physical Chemistry at the Justus Liebig

University Giessen, and particularly to B. P. Winnewisser and M. Winnewisser, for hospitality. The work of O.L.P. was supported in part by the Russian Fund for Fundamental Studies. This work was supported by the Natural Sciences and Engineering Research Council of Canada (NSERC). Acknowledgment is made to the Petroleum Research Fund for partial support of this work. Some support was also provided by the NASA Laboratory Astrophysics Program.

#### REFERENCES

1. F. C. DeLucia, P. Helminger, R. L. Cook, and W. Gordy, *Phys. Rev. A* **5**, 487–490 (1972).
2. P. Helminger, J. K. Messer, and F. C. De Lucia, *Appl. Phys. Lett.* **42**, 309–310 (1988).
3. A. V. Burenin, T. M. Fevral'skikh, E. N. Karyakin, O. L. Polyansky, and S. M. Shapin, *J. Mol. Spectrosc.* **100**, 182–192 (1983).
4. S. P. Belov, I. N. Kozin, O. L. Polyansky, M. Yu. Tretyakov, and N. F. Zobov, *J. Mol. Spectrosc.* **126**, 113–117 (1988).
5. J. C. Pearson, T. Anderson, E. Herbst, F. C. De Lucia, and P. Helminger, *Astrophys. J. Lett.* **379**, L41–L43 (1991).
6. J. Kauppinen, T. Karkkainen, and E. Kyrö, *J. Mol. Spectrosc.* **71**, 14–45 (1978).
7. J. Kauppinen, K. Jolma, and V.-M. Horneman, *Appl. Opt.* **21**, 3322–3336 (1982).
8. J. W. C. Johns, *J. Opt. Soc. Am. B* **2**, 1340–1354 (1985).
9. J.-Y. Mandin, V. Dana, J.-M. Flaud, and C. Camy-Peyret, *J. Mol. Spectrosc.* **152**, 179–184 (1992).
10. J.-M. Flaud, C. Camy-Peyret, and J.-P. Maillard, *Mol. Phys.* **32**, 499–521 (1976).
11. C. Camy-Peyret, J.-M. Flaud, J. P. Maillard, and G. Guelachvili, *Mol. Phys.* **33**, 1641–1650 (1977).
12. R. A. Toth, *J. Opt. Soc. Am. B* **8**, 2236–2255 (1991).
13. R. A. Toth, *J. Opt. Soc. Am. B* **10**, 1526–1544 (1993).
14. R. A. Toth, *J. Opt. Soc. Am. B* **10**, 2006–2030 (1993).
15. J.-M. Flaud, C. Camy-Peyret, J.-P. Maillard, and G. Guelachvili, *J. Mol. Spectrosc.* **65**, 219–228 (1977).
16. C. Camy-Peyret and J.-M. Flaud, Thèse de doctorat des sciences. Université Pierre et Marie Curie, Paris, 1975.
17. C. Camy-Peyret, J.-M. Flaud, and J.-P. Maillard, *J. Phys. Lett.* **41**, L23–L26 (1980).
18. J.-Y. Mandin, J.-P. Chevillard, J.-M. Flaud, and C. Camy-Peyret, *Can. J. Phys.* **66**, 997–1011 (1988).
19. J.-P. Chevillard, J.-Y. Mandin, J.-M. Flaud, and C. Camy-Peyret, *Can. J. Phys.* **67**, 1065–1084 (1989).
20. K. Nakamo, A. Saito, and N. Ohashi, *J. Mol. Spectrosc.* **131**, 405–406 (1988).
21. L. S. Rothman, R. R. Gamache, R. H. Tipping, C. P. Rinsland, M. A. H. Smith, D. C. Benner, V. Malathy Devi, J.-M. Flaud, C. Camy-Peyret, A. Perrin, A. Goldman, S. T. Massie, L. R. Brown, and R. A. Toth, *J. Quant. Spectrosc. Radiat. Transfer* **48**, 469–507 (1992).
22. J.-M. Flaud, C. Camy-Peyret, and R. A. Toth, "Water Vapor Line Parameters from Microwave to Medium Infrared." Pergamon, Elmsford, NY, 1981.
23. A. V. Burenin and V. I. Tyuterev, *J. Mol. Spectrosc.* **108**, 153–154 (1984).
24. O. L. Polyansky, *J. Mol. Spectrosc.* **112**, 79–87 (1985).
25. V. I. Tyuterev, *J. Mol. Spectrosc.* **151**, 97–129 (1992).
26. L. H. Coudert, *J. Mol. Spectrosc.* **154**, 427–442 (1992).
27. L. H. Coudert, *J. Mol. Spectrosc.* **165**, 406–425 (1994).
28. S. Carter and N. C. Handy, *J. Chem. Phys.* **87**, 4294–4301 (1987).
29. L. Halonen and T. Carrington, Jr., *J. Chem. Phys.* **88**, 4171–4185 (1988).

30. P. Jensen, *J. Mol. Spectrosc.* **133**, 438–460 (1989).
31. E. Kauppi and L. Halonen, *J. Phys. Chem.* **94**, 5779–5785 (1990).
32. C. D. Paulse and J. Tennyson, *J. Mol. Spectrosc.* **168**, 313–322 (1994).
33. P. Jensen, S. A. Tashkun, and V. I. G. Tyuterev, *J. Mol. Spectrosc.* **168**, 271–289 (1994).
34. O. L. Polyansky, P. Jensen, and J. Tennyson, *J. Chem. Phys.* **101**, 7651–7657 (1994).
35. A. E. Lynas-Gray, S. Miller, and J. Tennyson, *J. Mol. Spectrosc.* **169**, 458–467 (1995).
36. L. Wallace, W. Livingston, and P. Bernath, “An Atlas of the Sunspot Spectrum from 470 to 1233 cm<sup>-1</sup> (8.1 to 21 μm) and the Photospheric Spectrum from 460 to 630 cm<sup>-1</sup> (16 to 22 μm).” NSO Technical Report 1994-01, Tucson, AZ, 1994.
37. L. Wallace, P. Bernath, W. Livingston, K. Hinkle, J. Busler, B. Guo, and K. Zhang, *Science* **268**, 1155–1158 (1995).
38. J. Makarewicz, *J. Phys. B* **21**, 3633–3651 (1988).