# Infrared emission spectroscopy at $100 \mu \mathrm{~m}$. Vibration-rotation spectrum of CsI 

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#### Abstract

The vibration-rotation emission spectrum of CsI was recorded in the $110-130 \mathrm{~cm}^{-1}$ region of the spectrum. Although individual rotational lines were not resolved, we measured the positions of 29 band heads involving the vibrational bands from 1-0 to $30-29$. These vibrational data when combined with previously measured microwave and millimeter-wave pure rotational transitions yielded improved Dunham constants. In addition, an experimentally derived Born-Oppenheimer potential is also reported and compared with the purely ionic internuclear potential of the Rittner model. The results reported here demonstrate that far-infrared emission spectroscopy is a very sensitive technique for detecting high-temperature molecules, even at wavelengths around $100 \mu \mathrm{~m}$.


## 1. Introduction

Cesium iodide, a crystalline solid at room temperature, is an extremely volatile substance at elevated temperatures. Because of its volatility, attention recently has been directed toward CsI as a prime candidate in the transport of radioactive iodine from fission products produced in nuclear reactors [1].

Previous spectroscopic work on the alkali halides has included microwave absorption experiments. CsI is an ionic molecule with a large dipole moment of 11.69 D [2]. Pure rotational spectra have been obtained for most of the diatomic alkali halides in the centimeter-wave region $[3,4]$, and for alkali bromides and iodides in the millimeter-wave region [5]. The hyperfine structure of CsI was measured for the $J=2 \rightarrow 3$ rotational transition by Hoeft et al. [6]. The most recent work was carried out by Honerjäger and Tischer [7], who obtained the rotational spectra of
cesium halides in the 1 cm wavelength region and combined their results with the millimeter-wave data of Rusk and Gordy [5] to yield an improved set of Dunham Y constants.
Additional work included electron diffraction studies on CsI in the gas phase [8]. Oldenberg et al. [9] obtained the CsI ultraviolet chemiluminescence spectrum from the reaction $\mathrm{Cs}_{2}+\mathrm{I}_{2}$. Rounding out these type of investigations on CsI in the gas phase are photodissociation [10-12], collision-induced dissociation [13-17], and mass spectrometric [1820] studies.

In contrast, only a limited amount of infrared spectroscopic work has been reported for CsI. The far-IR absorption spectrum of CsI isolated in solid argon has been reported [21]. Rice and Klemperer [22] measured IR spectra of several lighter alkali halides and performed an extrapolation to determine the vibrational frequency of CsI. Konings et al. [1] recorded
a $0.1 \mathrm{~cm}^{-1}$ low-resolution IR absorption spectrum in the gas phase. They assigned the broad double-peaked feature, centered at $113.9 \mathrm{~cm}^{-1}$, to the fundamental vibrational band of CsI but were unable to resolve any rotational structure.
In this Letter, we report on the analysis of the farIR emission spectrum of CsI recorded with a Fourier transform spectrometer. Band head positions were measured consecutively from 1-0 to $30-29$, with the exception of the 17-16 band which was not measured. The infrared data were then combined with pure rotational lines from the literature to yield improved spectroscopic constants for the $X^{1} \Sigma^{+}$ground state.

## 2. Experimental

The experimental procedures followed were similar to those described in a previous paper on AlCl [23]. A 10 g sample of CsI was gradually heated to $900^{\circ} \mathrm{C}$ in a carbon boat placed in the center of a carbon liner that was housed inside of a Mullite $\left(3 \mathrm{Al}_{2} \mathrm{O}_{3} \cdot 2 \mathrm{SiO}_{2}\right)$ tube. The tube was pressurized with 10 Torr of argon gas to prevent condensation of CsI on the polyethylene windows. The central 50 cm portion of the Mullite tube, 1.2 m in length and with an outside diameter of 5 cm , was heated by a commer-
cial CM Rapid Temp furnace. The ends of the Mullite tube were water cooled and the window holders were attached with $O$ rings.
The infrared radiation from the furnace was directed through the emission port of a Bruker IFS 120 HR Fourier transform spectrometer at the University of Waterloo. The far-IR emission spectrum was recorded with a liquid-helium cooled Si bolometer from Infrared Laboratories and a $12 \mu \mathrm{~m}$ Mylar beamsplitter.
At $900^{\circ} \mathrm{C}$ where the vapor pressure of CsI is estimated to be 30 Torr [24], 90 scans were coadded at a resolution of $0.01 \mathrm{~cm}^{-1}$ in the $50-200 \mathrm{~cm}^{-1}$ spectral range.
Fig. 1 shows a compressed view of the far-infrared emission spectrum of CsI. The sharp lines, labelled in Fig. 1 with leader lines, are actually rovibrational band heads where rotational lines from each vibrational band form heads at $J \approx 300$ in the R branch. The positions of 29 band heads were measured for the 1-0 to 30-29 bands, with the exception of 17-16, which was not measured due to the presence of a strong $\mathrm{H}_{2} \mathrm{O}$ absorption band. Actual measurement of band head positions was accomplished by using Brault's computer program PC-DECOMP and proceeded by calibration with respect to impurity' $\mathrm{H}_{2} \mathrm{O}$ lines also present in the spectrum [25].


Fig. 1. A portion of the vibration-rotation emission spectrum of CsI with the band heads marked above.

Table 1
Pure rotational transitions of CsI（in $\mathrm{cm}^{-1}$ ）

| $v$ | $J^{\prime} \leftarrow J^{\prime \prime}$ | Observed | $\begin{aligned} & \text { Obs.-calc. } \\ & \left(\times 10^{-7}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| 0 | 3ヶ2 | $0.1415587^{*}$ | －9 |
| 0 | $16 \leftarrow 15$ | $0.7549309{ }^{\text {b }}$ | 52 |
| 0 | $17 \leftarrow 16$ | $0.8021016^{\text {b }}$ | 13 |
| 0 | $18 \leftarrow 17$ | $0.8492719^{\circ}$ | －14 |
| 0 | 20ヶ－19 | $0.9436108{ }^{\text {c }}$ | －36 |
| 0 | 104－103 | $4.8906551{ }^{\text {d }}$ | －6 |
| 0 | $111 \leftarrow 110$ | $5.2173437{ }^{\text {d }}$ | －10 |
| 0 | $128 \leftarrow 127$ | $6.0086465{ }^{\text {d }}$ | 10 |
| 0 | 135－134 | $6.3335389{ }^{\text {d }}$ | 9 |
| 0 | 1394－138 | $6.5189272{ }^{\text {d }}$ | 13 |
| 1 | 3ヶ2 | $0.1411499{ }^{\text {a }}$ | －7 |
| 1 | $16 \leftarrow 15$ | $0.7527548{ }^{\text {b }}$ | 106 |
| 1 | $17 \leftarrow 16$ | $0.7997853^{\text {b }}$ | 30 |
| 1 | 18＋17 | $0.8468205^{\circ}$ | 16 |
| 1 | $20 \leftarrow 19$ | $0.9408855^{\text {c }}$ | －17 |
| 1 | 111－110 | $5.2021936{ }^{\text {d }}$ | －52 |
| 1 | 128＋127 | $5.9911771{ }^{\text {d }}$ | 14 |
| 1 | 129＊－128 | $6.0374874{ }^{\text {d }}$ | 2 |
| 1 | 139＋138 | $6.4999507{ }^{\text {d }}$ | －19 |
| 2 | 3＋－2 | 0.1407419 ＊ | －3 |
| 2 | $17+16$ | $0.7974750{ }^{\text {b }}$ | 74 |
| 2 | $18 \leftarrow 17$ | $0.8443728^{\text {b }}$ | 47 |
| 2 | 20ヶ－19 | $0.9381615^{\circ}$ | －27 |
| 2 | 111－110 | $5.1870788{ }^{\text {d }}$ | 39 |
| 2 | 128－127 | $5.9737340{ }^{\text {d }}$ | 27 |
| 2 | 139－138 | $6.4810056{ }^{\text {d }}$ | －2 |
| 3 | 3－2 | 0.1403339 ＊ | －4 |
| 3 | 17－16 | $0.7951658{ }^{\text {b }}$ | 93 |
| 3 | 20ヶ19 | $0.9354428{ }^{\text {c }}$ | －23 |
| 3 | $128 \leftarrow 127$ | $5.9563113^{\text {d }}$ | －12 |
| 3 | 140ヶ－139 | $6.5079926^{\text {d }}$ | －6 |
| 4 | 3¢2 | $0.1399250^{\text {＊}}$ | －20 |
| 4 | $20 \leftarrow 19$ | $0.9327278{ }^{\text {c }}$ | －22 |
| 5 | 20ヶ－19 | $0.9300161^{\text {c }}$ | －29 |
| 6 | 20－19 | $0.9273111^{\text {c }}$ | －9 |
| 7 | 20ヶ－19 | $0.9246076{ }^{\text {c }}$ | －16 |
| 8 | 20ヶ19 | $0.9219096{ }^{\text {c }}$ | －9 |
| 9 | 20ヶ19 | $0.9192160^{\text {c }}$ | 1 |
| 10 | 20ヶ19 | $0.9165264^{\text {c }}$ | 8 |
| 11 | $20 \leftarrow 19$ | $0.9138398^{\text {c }}$ | 3 |
| 12 | $20 \leftarrow 19$ | $0.9111574{ }^{\text {c }}$ | －4 |
| 13 | 20ヶ19 | $0.9084881^{\circ}$ | 7 |
| 14 | $20 \leftarrow 19$ | $0.9058086^{\text {c }}$ | 15 |
| 15 | $20 \leftarrow 19$ | $0.9031394^{\text {c }}$ | 12 |
| 16 | $20 \leftarrow 19$ | $0.9004728{ }^{\text {c }}$ | －9 |
| 17 | $20 \leftarrow 19$ | $0.8978143^{\text {c }}$ | 6 |
| 18 | 20ヶ19 | $0.8954561^{\circ}$ | －20 |
| 19 | 20ヶ19 | $0.8925062^{\text {c }}$ | －8 |
| 20 | 20ヶ19 | $0.8898625^{\circ}$ | 21 |
| 21 | $20 \leftarrow 19$ | $0.8872187^{\circ}$ | 4 |
| 23 | $20 \leftarrow 19$ | $0.8819450{ }^{\circ}$ | －28 |
| 24 | $20 \leftarrow 19$ | $0.8793212^{\text {c }}$ | 17 |

## 3．Results and discussion

## 3．1．Dunham fits

All of the available microwave and millimeter－wave absorption data published so far on CsI［3，5－7］are displayed in Table 1．With the exception of the Hoeft et al．data［6］，all of the reported data corresponds to pure rotational line frequencies with no resolved hyperfine structure．In order to incorporate the Hoeft et al．data set into our fits（where individual hyper－ fine lines for the $J=2 \rightarrow 3$ transitions of $v=0-3$ were reported instead）line centers for these pure rota－ tional transitions were calculated using their re－ ported eqQ constants．A fit of the combined micro－ wave and millimeter－wave data to the Dunham energy levels yielded a standard deviation of 0.675 with re－ siduals given in Table 1.

The Dunham Ys obtained from this preliminary fit were then used in conjunction with the solutions of

$$
\begin{align*}
& \frac{\mathrm{d}}{\mathrm{~d} J} \sum_{i j}\left(Y _ { i j } ( v + \frac { 1 } { 2 } ) ^ { i } \left\{[(J+1)(J+2)]^{j}\right.\right. \\
& \left.\left.-[J(J+1)]^{j}\right\}\right)=0, \tag{1}
\end{align*}
$$

to obtain $\mathbf{R}(J)$ assignments for the band heads．
Two separate fits were then performed with a data set that combined the band head data with the micro－ wave and millimeter－wave data．In the first fit，des－ ignated unconstrained，all Dunham Ys were treated as adjustable parameters．The second fit，designated constrained，involved treating the $Y_{i 0}$ and $Y_{i 1}$ as ad－ justable parameters and fixing all remaining $Y_{i j}$ for $j>1$ to constraints imposed by the Dunham model ［23，26］．The standard deviations for the uncon－ strained and constrained fits were 0.674 and 0.802 ， respectively．Other pertinent results from these fits reported here are the band head residuals from the constrained fit（Table 2）and the Dunham $Y$ values along with their uncertainties quoted to 1 standard deviation（Table 3）．

Previous Dunham constants reported by Honerjä－ ger and Tischer are also listed in Table 3 for compar－ ison purposes．Note that they also used Dunham re－ lations similar to ours in determining the constants $Y_{10}, Y_{20}, Y_{03}$ ，and $Y_{04}$ ．Strictly speaking，the Dunham relation constraints are valid for only isotopically in－ variant Dunham $U$ constants，i．e．constants that con－

[^0]Table 2
Band head position in $\mathrm{cm}^{-1}$

| Band | Band origin | Band head | Obs.-calc. |
| :---: | :--- | :--- | ---: |
| $1-0$ | 118.6587 | 126.2504 | -0.0016 |
| $2-1$ | 118.1630 | 125.7216 | 0.0007 |
| $3-2$ | 117.6672 | 125.1928 | 0.0011 |
| $4-3$ | 117.1711 | 124.6640 | -0.0004 |
| $5-4$ | 116.6827 | 124.1430 | 0.0041 |
| $6-5$ | 116.1878 | 123.6157 | 0.0004 |
| $7-6$ | 115.6975 | 123.0932 | -0.0004 |
| $8-7$ | 115.2109 | 122.5745 | 0.0007 |
| $9-8$ | 114.7234 | 122.0551 | -0.0007 |
| $10-9$ | 114.2380 | 121.5380 | -0.0018 |
| $11-10$ | 113.7563 | 121.0248 | -0.0008 |
| $12-11$ | 113.2686 | 120.5057 | -0.0075 |
| $13-12$ | 112.7968 | 120.0027 | -0.0001 |
| $14-13$ | 112.3195 | 119.4943 | 0.0001 |
| $15-14$ | 111.8435 | 118.9874 | -0.0001 |
| $16-15$ | 111.3706 | 118.4838 | 0.0011 |
| $18-17$ | 110.4266 | 117.4788 | 0.0002 |
| $19-18$ | 109.9552 | 116.9772 | -0.0022 |
| $20-19$ | 109.4915 | 116.4834 | 0.0014 |
| $21-20$ | 109.0238 | 115.9858 | -0.0008 |
| $22-21$ | 108.5606 | 115.4929 | -0.0001 |
| $23-22$ | 108.0994 | 115.0021 | 0.0008 |
| $24-23$ | 107.6389 | 114.5122 | 0.0008 |
| $25-24$ | 107.1798 | 114.0239 | 0.0005 |
| $26-25$ | 106.7247 | 113.5397 | 0.0024 |
| $27-26$ | 106.2679 | 113.0540 | 0.0009 |
| $28-27$ | 105.8107 | 112.5681 | -0.0026 |
| $29-28$ | 105.3587 | 112.0875 | -0.0027 |
| $30-29$ | 104.9127 | 111.6131 | 0.0016 |

The observed-calculated values correspond to residuals obtained from the combined fit of band heads, microwave, and mil-limeter-wave data to the Dunham model with constraints. Estimates of band origins are based on the parameters listed in the second column of Table 3.
vey information solely about the mechanical effects of nuclear motion with the reduced mass explicitly factored out. However, since
$2 B_{\mathrm{e}} / \omega_{\mathrm{e}} \approx 0.0004$,
it can be safely assumed that Born-Oppenheimer breakdown, implicitly absorbed in the $Y \mathrm{~S}$ and of or$\operatorname{der} 2 B_{e} / \omega_{e}$, is negligible. Therefore, applying these relations to the $Y_{S}$ is justified.

Finally, with the $Y_{01}$ value obtained from the constrained fit along with the atomic masses taken from Mills et al. [27], we calculated the equilibrium internuclear separation $R_{\mathrm{e}}$ to be $3.31519042(40) \AA$.

### 3.2. Born-Oppenheimer potential

The results in Tables 2 and 3 are quite astonishing in view of the fact that the vibrational constants, $Y_{10}$, $Y_{20}$, and $Y_{30}$, were determined to such high degrees of precision from fits containing band head data. Moreover, the agreement between observed and calculated band head positions is in most cases considerably better than the assigned statistical weight of $0.002 \mathrm{~cm}^{-1}$. Clearly the incorporation of microwave and millimeter-wave lines to the data set together with Dunham constraints enhance the precision of these constants. But the question remains as to whether this statistical information is providing a realistic estimate as to how accurate one can expect to predict $\Delta v=+1$ rotational line frequencies with these constants.

In contrast to the flexibility of the Dunham model, a more rigid model was also tried, similar to the one used in the analysis of AIF and AlCl [23]. Specifically, this involved fitting the data directly to the eigenvalues of the radial Schrödinger equation,

$$
\begin{align*}
& \left(\frac{\hbar^{2}}{2 \mu} \nabla^{2}-U^{\mathrm{BO}}(R)+E(v, J)\right. \\
& \left.\quad-\frac{\hbar^{2}}{2 \mu}[1+q(R)] J(J+1) / R^{2}\right) \\
& \quad \times \psi(r, v, J)=0 \tag{3}
\end{align*}
$$

with the parameterized Born-Oppenheimer potential,
$U^{\mathrm{BO}}=D_{\mathrm{c}} \frac{\{1-\exp [-\beta(R)]\}^{2}}{\{1-\exp [-\beta(\infty)]\}^{2}}$,
where
$\beta(R)=z \sum_{i=0} \beta_{i} z^{i}$,
and
$z=\left(R-R_{\mathrm{e}}\right) /\left(R+R_{\mathrm{e}}\right)$.
Potential parameters obtained from this fit are displayed in Table 4 where the dissociation energy $D_{e}$ was fixed to the value given in Ref. [28]. The standard deviation was now significantly higher, 60.4, with the largest increase in the residuals contributed by the band head data with a root-mean-square deviation of $0.197 \mathrm{~cm}^{-1}$. It is also important to note that the statistical weights used in the Dunham $Y$ fits,

Table 3
Dunham $Y$ constants for CsI (in $\mathrm{cm}^{-1}$ )

| Constant | This work |  | Ref. [7] |
| :---: | :---: | :---: | :---: |
|  | unconstrained | constrained ${ }^{\text {a }}$ |  |
| $Y_{10}$ | 119.16002(144) | 119.165242(975) | 119.1776(76) |
| $Y_{20}$ | -0.250285(116) | -0.2505696(750) | -0.2505(7) |
| $10^{3} Y_{30}$ | 0.28453(293) | 0.28573(197) | - |
| $10^{2} Y_{01}$ | $2.36274612(245)$ | 2.36273842 (58) | 2.3627357 (15) |
| $10^{3} Y_{11}$ | -0.06827322(967) | -0.06826443(377) | -0.0682626(70) |
| $10^{6} Y_{21}$ | 0.048969(991) | 0.048780(533) | 0.04893(80) |
| $10^{9} Y_{31}$ | 0.1255(281) | 0.1224(187) | $0.114(25)$ |
| $10^{9} Y_{02}$ | -3.72237(141) | -3.71541832 | -3.71464(47) |
| ${ }_{10} 0^{12} Y_{12}$ | -2.028(196) | -2.30881029 | -2.30 (50) |
| ${ }^{10} 0^{13} Y_{22}$ | - | 0.253353610 | - |
| ${ }_{10} 0^{15} Y_{03}$ | -0.0714(321) | -0.250428337 | -0.25043(13) |
| ${ }_{10} 0^{19} Y_{13}$ | - | -0.981502746 | - |
| ${ }^{10} 0^{20} Y_{23}$ | - | 0.798064841 | - |
| $10^{22} Y_{04}$ | - | -0.889215827 | -0.8876(17) |
| ${ }_{10} 0^{24} \mathrm{Y}_{14}$ | - | 0.152376355 | -0.886(17) |
| ${ }^{10} 0^{28} Y_{05}$ | - | -0.257041566 | - |
| ${ }_{10} 0^{31} Y_{15}$ | - | 0.820852269 | _ |
| ${ }_{10} 0^{35} Y_{06}$ | - | -0.875800401 | - |
| ${ }^{1041} Y_{07}$ | - | -0.315840421 | - |

${ }^{-}$See text.

Table 4
Born-Oppenheimer potential parameters

| $D_{e}\left(\mathrm{~cm}^{-1}\right)$ | 28710 |
| :--- | :---: |
| $R_{e}(\AA)$ | $3.3150949(177)$ |
| $\beta_{0}$ | $4.404121(304)$ |
| $\beta_{1}$ | $-1.0409(190)$ |

$3 \times 10^{-6} \mathrm{~cm}^{-1}$ for the microwave and millimeterwave lines and $0.002 \mathrm{~cm}^{-1}$ for the band head positions, were also used in this fit. Therefore, a fit of the data to this more rigid model places a conservative upper limit of $0.2 \mathrm{~cm}^{-1}$ on the accuracy of predicted $\Delta v=+1$ rotational line positions.

In addition to representing the Born-Oppenheimer potential by Eq. (4), we also obtained the Dunham form by expanding Eq. (4) in a power series about $R=R_{e}$. The Dunham potential constants derived in this manner are given in Table 5. For the purpose of comparison, the as derived from the $Y$ s of the constrained fit are also listed.

Table 5
Dunham potential constants

|  | BO potential | Dunham $Y \mathrm{~s}$ |
| :--- | :---: | :---: |
| $a_{0}\left(\mathrm{~cm}^{-1}\right)$ | $149382(267)$ | $150253(477)$ |
| $a_{1}$ | $-3.43841(452)$ | $-3.4286(154)$ |
| $a_{2}$ | $8.0309(220)$ | $7.624(110)$ |
| $a_{3}$ | $-15.5029(657)$ | $-12.960(514)$ |
| $a_{4}$ | $26.508(153)$ | $17.42(206)$ |
| $a_{5}$ | $-41.552(306)$ | $-18.61(790)$ |

### 3.3. Rittner model

One additional model that we used in analyzing the data was the Rittner potential,

$$
\begin{align*}
& U(R)=-e^{2}\left(\frac{1}{R}+\frac{\left(\alpha_{+}+\alpha_{-}\right)}{2 R^{4}}+\frac{2 \alpha_{+} \alpha_{-}}{R^{7}}\right) \\
& -\frac{C_{6}}{R^{6}}+A \exp (-R / \rho)+U_{0} \tag{7}
\end{align*}
$$

In Eq. (7) $\alpha_{+}$and $\alpha_{-}$are the atomic polarizabilities for $\mathrm{Cs}^{+}$and $\mathrm{I}^{-}, C_{6}$ is a measure of the van der Waals attraction between ions, $A$ and $\rho$ are constants that

Table 6
Rittner parameters and potential constants

|  | BO potential |  | Dunham $Y$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | B-K | S-A | B-K | S-A |
| $\alpha_{+}\left(\dot{A}^{3}\right)$ | 2.880 | 2.935 | 2.880 | 2.935 |
| $\alpha_{-}\left(\dot{A}^{3}\right)$ | 5.866 | 5.409 | 5.866 | 5.409 |
| $10^{5} C_{6}\left(\mathrm{~cm}^{-1} \dot{A}^{6}\right)$ | 5.579 | 5.242 | 5.579 | 5.242 |
| $10^{7} A\left(\mathrm{~cm}^{-1}\right)$ | 3.785 | 3.886 | 3.882 | 3.989 |
| $\rho(\AA)$ | 0.3861 | 0.3836 | 0.3848 | 0.3823 |
| $R_{\mathrm{e}}(\AA)$ | 3.3150949 |  | 3.31519042 |  |
| $r_{0}\left(\mathrm{~cm}^{-1}\right)$ | 149382 |  | 150253 |  |
| $r_{1}$ | -3.530 | -3.551 | -3.543 | -3.564 |
| $r_{2}$ | 7.877 | 7.991 | 7.940 | 8.054 |
| $r_{3}$ | -13.11 | -13.46 | -13.28 | -13.63 |
| $r_{4}$ | 16.90 | 17.68 | 17.25 | 18.03 |
| $r_{s}$ | -16.19 | -17.63 | -16.75 | -18.20 |

Table 7
Rittner $Y$ constants in $\mathrm{cm}^{-1}$

| $Y_{10}$ | 119.165 |
| :--- | :---: |
| $Y_{20}$ | -0.2758 |
| $10^{4} Y_{30}$ | 2.981 |
| $10^{2} Y_{01}$ | 2.36273842 |
| $10^{5} Y_{11}$ | -7.176 |
| $10^{8} Y_{21}$ | 3.268 |
| $10^{10} Y_{31}$ | 2.388 |
| $10^{9} Y_{02}$ | -3.715 |
| $10^{12} Y_{12}$ | -5.176 |
| $10^{14} Y_{22}$ | 2.559 |
| $10^{16} Y_{03}$ | -3.231 |
| $10^{18} Y_{13}$ | -1.403 |
| $10^{20} Y_{23}$ | 1.821 |
| $10^{22} Y_{04}$ | -1.313 |
| $10^{25} Y_{14}$ | -3.775 |
| $10^{29} Y_{05}$ | -4.992 |
| $10^{33} Y_{15}$ | 1.366 |
| $10^{35} Y_{06}$ | -2.210 |
| $10^{41} Y_{07}$ | -1.014 |

correspond to the Born-Mayer form for repulsion, and $U_{0}$ is the dissociation energy [29].
A particular form of the Rittner potential conducive to the analysis of spectroscopic data is the power series expansion [3],
$U(\xi)=U(0)+r_{0} \xi^{2}\left(1+r_{1} \xi+r_{2} \xi^{2}+r_{3} \xi^{3}+\ldots\right)$,
where
$\xi \equiv\left(R-R_{\mathrm{e}}\right) / R_{\mathrm{e}}$
and the minimum of $U(\xi)$ is constrained to lie at $\xi=0$.
By equating $r_{0}$ to the Dunham $a_{0}$, the remaining $r_{i}$ are only functions of the Rittner parameters and $R_{e}$. Expressions for $r_{i}$ have already been given by Honig et al. [3] and, therefore, are not reproduced here.
In the process of calculating $r_{i}$, Brumer-Karplus [30] and Shanker-Agrawal [31] polarizabilities for $\mathrm{Cs}^{+}$and $\mathrm{I}^{-}$were chosen as representative values [32], while $C_{6}$ was estimated using London's formula [30],
$C_{6}=-\frac{3}{2} \frac{I_{\mathrm{Cs}} I_{\mathrm{I}}}{I_{\mathrm{Cs}}+I_{\mathrm{I}}} \alpha_{+} \alpha_{-}$,
where $I_{\text {Cs }}$ is the ionization energy of atomic $\mathrm{Cs}, 3.893$ eV [33], and $I_{\mathrm{I}}$ is the electron affinity of iodine, 3.063 eV [34]. The $A$ and $\rho$ repulsion constants were obtained by numerically solving
$\left(\frac{\mathrm{d} U(\xi)}{\mathrm{d} \xi}\right)_{\xi=0}=0$
and
$\left(\frac{\mathrm{d}^{2} U(\xi)}{\mathrm{d} \xi^{2}}\right)_{\xi=0}=2 a_{0}$.
Values of Rittner parameters and $r_{i}$ calculated from $B-K$ and S-A polarizabilities are tabulated in Table 6.

Comparison of $a_{i}$ in Table 5 with $r_{i}$ in Table 6 in-
dicates excellent agreement between the $r_{i}$ and $a_{i}$ obtained from the Dunham $Y \mathrm{~s}$. On the other hand, for $a_{i}$ from the potential fit, good agreement is exhibited only between the lowest $r_{i}$ and $a_{i}$ and becomes progressively worse for the higher $r_{i}$ and $a_{i}$.

The fact that $a_{i}$ from the Dunham $Y \mathrm{~s}$ rather than $a_{i}$ from the potential fit agree with the Rittner $r_{i}$ to $\leqslant 5 \%$ seems to signify that the Rittner model is capable of predicting the spectrum much more accurately than the Born-Oppenheimer potential given by Eq. (4). To demonstrate that this was not the case, a set of $Y \mathrm{~s}$ was computed by averaging the Rittner $r_{i}$ appearing in the last two columns of Table 6. Generating a spectrum with these Rittner Ys (Table 7) gave a root-mean-square deviation of $1.2 \mathrm{~cm}^{-1}$ for the ob-served-calculated band-head positions ( $0.002 \mathrm{~cm}^{-1}$ for pure rotation transitions) as compared to 0.2 $\mathrm{cm}^{-1}$ for the Born-Oppenheimer potential fit. Thus, it appears that the Rittner model is capable of predicting the rovibrational spectrum to no better than $\approx 1 \mathrm{~cm}^{-1}$. Obviously, a more refined treatment must await the analysis of resolved rotational structure in the far-IR spectrum before any final conclusion can be reached.

## 4. Conclusion

Infrared emission spectroscopy is a remarkably sensitive technique for the detection of high-temperature molecules, even at the longer wavelength end of the spectrum ( $100 \mu \mathrm{~m}$ ). Although individual rotational lines could not be resolved because of the small rotational constant, $B \approx 0.02 \mathrm{~cm}^{-1}$, it was still possible to improve the vibrational constants by using band-head positions. The availability of high-precision microwave and millimeter-wave data allowed the separation between the band heads and band origins to be calculated reliably for the first time. Emission spectroscopy at very long wavelengths is not only feasible but is also a useful technique for elucidating molecular structure and monitoring the concentrations of molecules at high temperatures.

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[^0]:    ${ }^{\mathbf{a}}$ See text，Ref．［6］．${ }^{\text {b }}$ Ref．［3］．
    ${ }^{\text {c }}$ See text，Ref．［7］．${ }^{d}$ Ref．［5］．

