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# High-resolution investigation of the excited electronic states of CaSH and SrSH by laser excitation spectroscopy 

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#### Abstract

A laser ablation/pulsed molecular jet system has been used to record high-resolution laser excitation spectra of the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition of CaSH and the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$, and $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transitions of SrSH . The rotationally-resolved data were analysed using an asymmetric top Hamiltonian ( $A$-reduction) to determine rotational and fine structure parameters. A combined fit of all the newly measured and the previously recorded spectroscopic data for both CaSH and SrSH was performed. In the excited states observed in this study, both species were found to have a bent geometry. The spin-rotation parameters were analysed in terms of the pure precession and unique perturber approximations. In the excited electronic states of SrSH , the large spin-rotation interaction was found to cause perturbations between the $K_{a}=0$ and 1 levels within each state. In the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states of both species, the metal-sulfur bond length was found to decrease relative to the ground state, which is consistent with previous observations of other calcium and strontium radicals.


## 1. Introduction

Among the small metal-containing molecules bonded to a single polyatomic ligand, the metal monohydroxides (MOH) have been the most investigated, both experimentally and theoretically [1, 2]. Extension of these studies to other polyatomic ligands, particularly those of lower symmetry, has been limited due to the complicated nature of their rotational energy level patterns and the difficulties associated with synthesizing them in sufficient quantities. One such species, the metal monohydrosulfides (MSH), is of interest because it is the sulfur analogue of the metal monohydroxides and therefore allows for comparison of the geometric and electronic properties between these two groups of molecules. For example, calcium, strontium, and barium monohydroxides have been found to possess linear geometries in their ground and low-lying electronic states [1]. This molecular structure has been attributed to the mostly ionic character of the metal-oxygen bond [3, 4].

[^0]In contrast, their hydrosulfide counterparts have not been found to share this characteristic. Limited spectroscopic data on the ground and low-lying excited electronic states of several of these species have shown that they are bent, with an $\mathrm{M}-\mathrm{S}-\mathrm{H}$ bond angle of $\sim 90^{\circ}$ [5]. This change in geometry is an indication of an increased covalent character in the metal-ligand bond [5]. Also, the reduced molecular symmetry of the metal hydrosulfides allows for additional interactions within and between their excited electronic states that are not possible for the metal hydroxides, making them of further interest [6].

The metal hydrosulfides were first observed in the gas phase by the Bernath group in their study of calcium and strontium monohydrosulfide and monothiolate derivatives [7]. Their low-resolution spectra suggested that CaSH and SrSH were non-linear in their four lowest energy electronic states. Subsequent high-resolution investigations of the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}[6]$ and $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ [8] transitions of CaSH showed that this molecule was indeed bent in these states, in agreement with theoretical predictions [9, 10]. This work was followed by studies of the ground states of LiSH, NaSH, MgSH, $\mathrm{CaSH}, \mathrm{SrSH}$, $\mathrm{BaSH}, \mathrm{AlSH}$, and CuSH [5, 11-17] using pure rotational spectroscopic techniques. Again each of these molecules was found to possess a bent geometry in their ground state. Unfortunately, high-resolution studies of the


Figure 1. Overview of the spectra recorded for the $\tilde{A}^{2} A^{\prime}-$ $\tilde{X}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$, and $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transitions of SrSH. Each subgroup of lines is labelled by the notation ( $K_{a}^{\prime}-K_{a}^{\prime \prime}$ ). In the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transitions, multiple $K_{a}$ subbands $((0-0)$ and $(1-0))$ were observed and each subband has the appearance of a perpendicular transition. In the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition only one subband ( $0-0$ ) was observed, which has the structure of a parallel transition.
excited electronic states of the metal hydrosulfides have been limited to CaSH and to a recent report of the $\tilde{A}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transition of CuSH [18].

In order to further examine the excited electronic states of the metal hydrosulfides, we have recorded highresolution laser excitation spectra of the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition of CaSH along with the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}-$ $\tilde{X}^{2} A^{\prime}$, and $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transitions of SrSH . The rotation-ally-resolved spectra were analysed using an asymmetric top ( $A$-reduction) Hamiltonian. Rotational and fine structure parameters were derived from a least-squares fit of the newly measured and the previously recorded spectroscopic data. CaSH and SrSH were both found to exhibit a bent geometry in each of the electronic states observed in this study. Evidence for electronic state mixing, an examination of the measured spin-rotation constants in terms of a pure precession model, and a comparison of excited state structural parameters for CaSH and SrSH will be presented.

## 2. Experimental

Laser excitation spectra of CaSH and SrSH were obtained using the laser ablation/pulsed molecular jet system of the Bernath group [19]. Ca and Sr vapour were produced by the ablation of a metal target rod ( Ca or Sr ) using the 3 rd harmonic ( 355 nm ) of a pulsed ( 10 Hz ) Nd:YAG laser ( $10 \mathrm{~mJ} / \mathrm{pulse}$ ). The metal atoms reacted with a gas mixture of $7 \% \mathrm{H}_{2} \mathrm{~S}$ in argon ( 100 psi backing pressure). The molecules then exited the pulsed nozzle assembly in a free jet expansion ( $T_{\text {rot }} \sim 4-6 \mathrm{~K}$ ) and were interrogated $\sim 15 \mathrm{~cm}$ downstream by a probe laser. A photomultiplier tube (PMT) was used to detect the laser-induced fluorescence and band pass filters $( \pm 20 \mathrm{~nm})$ were employed to attenuate the plasma radiation. The output of the PMT was sent through a preamplifier ( $100 \times$ current) and then to a boxcar integrator for processing.
High-resolution laser excitation spectra of CaSH and SrSH were recorded using a Coherent ring dye (DCM laser dye) laser system. The band centres from previous low-resolution work [7] were used as the approximate starting positions for recording high-resolution spectra of each electronic transition. Rotationally resolved spectra were obtained in $5 \mathrm{~cm}^{-1}$ segments, at a data sampling interval of 10 MHz and scan speeds of $1-3$ minutes per wavenumber, over the range of each transition. The slower scan speeds, and in some cases the averaging of several $5 \mathrm{~cm}^{-1}$ segments together, were necessary to increase the signal-to-noise ratio of the spectra. Line widths of approximately 350 MHz were observed and are the result of residual Doppler broadening in the molecular jet. The $\mathrm{I}_{2}$ spectrum was recorded simultaneously by laser excitation spectroscopy with fluorescence detection and used to calibrate the spectra [20]. The estimated uncertainty of the spectral line positions is $0.003 \mathrm{~cm}^{-1}$.

## 3. Results

The molecular geometry of CaSH and SrSH is bent. As a result these molecules can be classified as near prolate asymmetric tops belonging to the $C_{s}$ point group. The electronic states of these species are ordered in energy as $\tilde{X}^{2} A^{\prime}, \tilde{A}^{2} A^{\prime}, \tilde{B}_{2}^{2} A^{\prime \prime}$, and $\tilde{C}^{2} A^{\prime}[7,10]$. In the linear limit, the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ terms correlate to a ${ }^{2} \Pi$ state while the $\tilde{X}^{2} A^{\prime}$ and $\tilde{C}^{2} A^{\prime}$ terms correlate to ${ }^{2} \Sigma^{+}$states [7]. Figure 1 shows an overview of the spectra recorded for the $\tilde{A}^{2} A^{\prime}-$ $\tilde{X}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$, and $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transitions of SrSH. In the spectra of the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transitions, features arising from two ( $K_{a}^{\prime}-K_{a}^{\prime \prime}$ ) subbands were observed. Both of these subbands, ( $0-0$ ) and (1-0), have the appearance of perpendicular transitions.


Figure 2. Energy level diagram of the $K_{a}^{\prime}=1-K_{a}^{\prime \prime}=0$ subband of the $\mathscr{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition of CaSH and SrSH . Each rotational energy level is labelled by the quantities $N, J$, $K_{a}$, and $K_{c}$. The allowed transitions are determined by $b$-dipole type selections rules ( $\Delta K_{a}= \pm 1$ and $\Delta K_{c}= \pm 1, \pm 3$ ) as well as $\Delta N=0, \pm 1, \pm 2$ and $\Delta J=0, \pm 1$. The rotational energy levels of the $\tilde{X}^{2} A^{\prime}$ state have the appearance of a Hund's case (b) ${ }^{2} \Sigma$ state and those of the $\tilde{A}^{2} A^{\prime}$ state resemble a Hund's case (a) ${ }^{2} \Pi$ (regular) state. A total of twelve branches are possible in this subband, labelled by the notation ${ }^{\Delta N} \Delta J_{F_{i}^{\prime} F_{j}^{\prime \prime}}(i=1,2 ; j=1,2)$.

For the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transitions of CaSH and SrSH only the (0-0) subband was observed, which has the appearance of a parallel transition.

The rotational energy levels of CaSH and SrSH can be labelled using the asymmetric top molecule quantities $K_{a}$ and $K_{c}$, which are the projections of the rotational angular momentum $\mathbf{N}$ onto the corresponding $a$ and $c$ inertial axes, respectively [21]. Because the metal hydrosulfides are near prolate asymmetric tops, their rotational energy levels can be grouped by the value of $K_{a}$. The rotational energy levels within each $K_{a}$ group are split into two by asymmetry splitting and labelled by $K_{c}$, where $K_{c}=N-K_{a}$ or $N-K_{a}+1$. In addition, CaSH and $\operatorname{SrSH}$ each possess an unpaired electron located primarily on the metal atom. Consequently, each asymmetry component of every rotational level is further split into two by the interaction of the
unpaired electron spin (S) and the rotational angular momenta, and are labelled by $\mathbf{J}$, where $\mathbf{J}=\mathbf{N}+\mathbf{S}$. Because CaSH and SrSH do not possess an axis of rotational symmetry and each has only a single hydrogen atom, proton nuclear spin statistics do not affect the $K_{a}$ levels in these molecules [21]. Therefore, unlike in our previous study of $\mathrm{SrNH}_{2}$ [22], only the rotational levels of the $K_{a}=0$ component of the $\tilde{X}^{2} A^{\prime}$ ground state are expected to be populated in our rotationally cold molecular jet.
An energy level diagram for the $K_{a}^{\prime}=1-K_{a}^{\prime \prime}=0$ subband of the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition of SrSH is shown in figure 2. Each energy level is identified by the quantum numbers $N$ and $J$, as well as the asymmetric top labels $K_{a}$ and $K_{c}$. The rotational energy levels of the $\tilde{X}^{2} A^{\prime}$ ground state ( $K_{a}=0$ ) resemble a Hund's case (b) ${ }^{2} \Sigma$ state. The spin-rotation parameters $\varepsilon_{b b}$ and $\varepsilon_{c c}$ ( $\varepsilon_{a a}$ is essentially zero) in this state are smaller than the rotational constants ( $B$ and $C$ ); therefore, the spin components ( $\mathrm{F}_{1}$ and $\mathrm{F}_{2}$ ) can be grouped together by their value of $N$. For the $\tilde{A}^{2} A^{\prime}$ state $\left(K_{a}=1\right)$ the rotational energy levels have the appearance of a Hund's case (a) ${ }^{2} \Pi$ (regular) state. The splitting of the spin components in this state is much larger than in the ground state. In the $\tilde{A}^{2} \Pi$ state of the linear analogue SrOH , the $\mathrm{F}_{1}$ and $\mathrm{F}_{2}$ levels are separated by the spin-orbit coupling parameter $A_{s o}\left(\sim 266 \mathrm{~cm}^{-1}\right)$ [23]. Because the $\tilde{A}^{2} A^{\prime}$ state of SrSH is not orbitallydegenerate, the first-order contribution to this interaction is quenched. However, second-order spin-orbit coupling is possible. This effect can be significant and contributes to the $\varepsilon_{a a}$ spin-rotation constant $\left(\sim 8.85 \mathrm{~cm}^{-1}\right)$, which is primarily responsible for the large splitting of the $\mathrm{F}_{1}$ and $\mathrm{F}_{2}$ components in the $\tilde{A}^{2} A^{\prime}$ state. In this state, $\mathrm{F}_{1}$ and $\mathrm{F}_{2}$ designate the $\Sigma=-1 / 2$ and $+1 / 2$ spin components ( $\Sigma$ is the projection of $\mathbf{S}$ onto the symmetry axis in the linear limit), respectively. Because the inertial axis in SrSH is rotated by only $0.43^{\circ}$ from the $\mathrm{Sr}-\mathrm{S}$ bond, an approximate picture of the orbital character of the $\tilde{A}^{2} A^{\prime}$ state can be extrapolated from species with higher molecular symmetry such as CaF and $\mathrm{CaNH}_{2}$ [1]. The unpaired electron in the $\tilde{A}^{2} A^{\prime}$ state resides in the in-plane component of a $\pi$ orbital, which lies nearly along the molecular $b$-axis [6]. As a result, $b$-dipole type transitions ( $\Delta K_{a}= \pm 1$ and $\Delta K_{c}= \pm 1, \pm 3$ ) are expected to be the most intense. The selection rules $\Delta N=0, \pm 1, \pm 2$ and $\Delta J=0, \pm 1$ give rise to twelve branches in the (1-0) subband, labelled by the notation ${ }^{\Delta N} \Delta J_{F_{i}^{\prime} F_{i}^{\prime \prime}}(i=1,2$; $j=1,2$ ).

For the $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transition, an energy level diagram of the $K_{a}^{\prime}=1-K_{a}^{\prime \prime}=0$ subband is shown in figure 3. The ( $K_{a}=1$ ) rotational energy levels in the $\tilde{B}^{2} A^{\prime \prime}$ state have the appearance of a Hund's case (a) ${ }^{2} \Pi$ (inverted) state due to the negative value of $\varepsilon_{a a}$. As a result, $\mathrm{F}_{1}$ and $\mathrm{F}_{2}$ now designate the $\Sigma=+1 / 2$ and $-1 / 2$ spin


Figure 3. Energy level diagram of the $K_{a}^{\prime}=1-K_{a}^{\prime \prime}=0$ subband of the $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transition of CaSH and SrSH . The quantities $N, J, K_{a}$, and $K_{c}$ are used to label each rotational energy level. The allowed transitions are determined by $c$-dipole type selections rules $\tilde{B} \Delta K_{a}= \pm 1$ and $\Delta K_{c}=0, \pm 2$ ) as well as $\Delta N=0, \pm 1, \pm 2$ and $\Delta J=0, \pm 1$. In the $\tilde{X}^{2} A^{\prime}$ state, the rotational energy levels resemble a Hund's case (b) ${ }^{2} \Sigma$ state while those of the $\tilde{B}^{2} A^{\prime}$ state have the appearance of a Hund's case (a) ${ }^{2} \Pi$ (inverted) state. In this subband a total of twelve branches are possible and are labeled by the notation ${ }^{\Delta N} \Delta J_{F_{i}^{\prime} F_{j}^{\prime \prime}}(i=1,2 ; j=1,2)$.
components, respectively. In the $\tilde{B}^{2} A^{\prime \prime}$ state, the unpaired electron (approximately) resides in a $\pi$ orbital perpendicular to the plane of the molecule (molecular $c$-axis) [6]; therefore, $c$-dipole type transitions ( $\Delta K_{a}= \pm 1$ and $\left.\Delta K_{c}=0, \pm 2\right)$ are expected to be the most intense. Twelve branches are possible in the (1-0) subband ( $\Delta N=0, \pm 1, \pm 2$ and $\Delta J=0, \pm 1$ ) and are labelled by the notation ${ }^{\Delta N} \Delta J_{F_{i}^{\prime} F_{i}^{\prime}}(i=1,2 ; j=1,2)$.

In the $\tilde{C}^{2} A^{\prime}$ state, the unpaired electron resides in a $\sigma$-type molecular orbital. As a result, the most intense transitions expected between the $\tilde{C}^{2} A^{\prime}$ and $\tilde{X}^{2} A^{\prime}$ states of CaSH and SrSH are $a$-dipole type ( $\Delta K_{a}=0 ; \Delta K_{c}= \pm 1$, $\pm 3$ ). Only transitions in the $K_{a}^{\prime}=0-K_{a}^{\prime \prime}=0$ subband, which has the appearance of a parallel type transition [22], are expected to be observed. Interestingly, features arising from the $(0-0)$ subband were also observed in the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transitions of SrSH . This was surprising given the small degree of rotation
of the inertial axes from the $\mathrm{Sr}-\mathrm{S}$ bond. The presence of these subbands is due to the off-diagonal spin-rotation term in the Hamiltonian $\left(\left(\varepsilon_{a b}+\varepsilon_{b a}\right) / 2\right)$, which can mix the rotational energy levels of the $K_{a}=0$ and $K_{a}=1$ levels [14, 16, 24]. In the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states of SrSH, this parameter is the same order of magnitude as the $\varepsilon_{b b}$ and $\varepsilon_{c c}$ spin-rotation constants; therefore, the $K_{a}=0$ levels have sufficient $K_{a}=1$ character to make the ( $0-0$ ) subband observable. Because the $\varepsilon_{b b}$ and $\varepsilon_{c c}$ spinrotation parameters are larger than the rotational constants in the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states of SrSH , the $K_{a}=0$ rotational energy levels have the structure of a Hund's case (a) ${ }^{2} \Pi$ state. As a result, the ( $0-0$ ) subbands for the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transitions have the appearance of perpendicular transitions. Interestingly, we did not observe the (1-0) subbands in the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transitions of CaSH and SrSH .

Quantum number assignments ( $J$ ) for each transition of CaSH and SrSH were made using combination differences available from the ( $K_{a}=0$ ) ground state millimetre-wave data $[14,15]$. Determination of the upper state $K_{a}$ values for the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states was more complex, because, as mentioned previously, each group of lines has the appearance of a perpendicular transition. For the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition, the origin gap of the $(1-0) \mathrm{F}_{2}$ subband is $\sim 4 B$; therefore, the group of lines located at higher wavenumbers (see figure 1) was assigned to this subband. The remaining subbands $\left((1-0) \mathrm{F}_{1}\right.$ and $\left.(0-0)\right)$ both have an origin gap of $\sim 2 B$. However, the energy separation of the ( $0-0$ ) band from the centre of the (1-0) $\mathrm{F}_{1}$ and (1-0) $\mathrm{F}_{2}$ spin components is given by the quantity $A^{\prime} K_{a}^{\prime}$. Using the value of the ground state $A$ rotational constant as an estimate gives an energy separation of $\sim 10 \mathrm{~cm}^{-1}$. This condition is satisfied only if the group of lines on the lower wavenumber side of the spectrum is assigned as the $(0-0)$ subband and those lines in the centre of the spectrum are assigned as the $(1-0) \mathrm{F}_{1}$ subband. For the $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transition, the ( $1-0$ ) $\mathrm{F}_{1}$ subband has an origin gap of $\sim 4 B$; therefore, the middle group of lines (see figure 1) could be assigned to this subband. Because the $K_{a}^{\prime}=0$ level lies lower in energy than the $K_{a}^{\prime}=1\left(\mathrm{~F}_{2}\right)$ level, the only plausible assignment for the weaker group of lines at lower wavenumbers is the ( $0-0$ ) subband. The remaining stronger features at higher wavenumbers are the (1-0) $\mathrm{F}_{2}$ subband. In addition, the similar intensity of the (1-0) $F_{1}$ and (1-0) $F_{2}$ spincomponents in each electronic transition suggests that they share a common upper and lower $K_{a}$ value.

In figure 4, a subsection of the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ spectrum of SrSH is presented with $J$ assignments. In the top and bottom panels, the six branches observed for the (1-0) $F_{1}$ subband and the six branches of the (1-0) $F_{2}$ subband are shown, respectively. The overall appearance of the


Figure 4. Expanded view of the $(1-0)$ subbands of the $\tilde{A}^{2} A^{\prime}-$ $\tilde{X}^{2} A^{\prime}$ transition of SrSH . Transitions involving the $K_{a}^{\prime}=1, \mathrm{~F}_{1}$ and $F_{2}$ spin components are shown in the top and bottom panels, respectively. In each spectrum, transitions arising from the six possible branches are presented and labelled by their $J$ values. In the top panel the origin gap is $\sim 2 B$, while in the bottom panel the origin gap is $\sim 4 B$. Each spectrum has the appearance of a perpendicular transition with $\sim 1 B$ and $\sim 3 B$ spaced branches present.
spectra, with $\sim 1 B$ and $\sim 3 B$ spaced branches, is similar to a Hund's case (a) ${ }^{2} \Pi$-Hund's case (b) ${ }^{2} \Sigma$ transition. A portion of the $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ spectrum of SrSH is displayed in figure 5, with quantum number assignments. In the top panel, transitions from three branches of the $(0-0)$ subband (labelled in italics) are shown progressing through the six branches observed for the $(1-0) F_{1}$ subband. In the bottom panel, lines from the six branches of the $(1-0) F_{2}$ subband are presented. In each subband, a pattern of $\sim 1 B$ and $\sim 3 B$ spaced lines is present. Figure 6 shows a spectrum, with rotational assignments, of the $(0-0)$ subband of the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition of SrSH . A total of six branches were observed in this subband, which exhibits the pattern of a Hund's case (b) ${ }^{2} \Sigma-$ Hund's case (b) ${ }^{2} \Sigma$ transition. The $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition of CaSH , which is not shown, has a very similar appearance to that of SrSH .


Figure 5. Expanded view of the $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transition of SrSH . In the top panel, the six branches of the $(1-0) \mathrm{F}_{1}$ subband are shown along with three of the branches of the $(0-0)$ subband (labelled in italics). In the bottom panel, the six branches observed for the (1-0) $\mathrm{F}_{2}$ subband are shown. The origin gap of the (1-0) $\mathrm{F}_{1}$ subband in the upper panel is $\sim 4 B$, while in the lower panel the origin gap of the $(1-0) F_{2}$ subband is $\sim 2 B$. The presence of $\sim 1 B$ and $\sim 3 B$ spaced branches in all three subbands gives each the appearance of a perpendicular transition.

## 4. Analysis

The rotational transitions recorded for the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$, $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$, and $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transitions of SrSH and CaSH were fitted using a non-linear least-squares fitting program that contained the appropriate effective Hamiltonian in a Hund's case (b) basis. For the molecular rotation $(A, B$, and $C)$ and its centrifugal distortion corrections ( $\Delta_{N}, \Delta_{N K}$, higher order terms), matrix elements derived using Watson's asymmetric top Hamiltonian ( $A$ reduction) were used [25]. The spin-rotation interaction ( $A$-reduction [26]) was modelled using the matrix elements given by Hirota [24]. For a molecule with $C_{s}$ symmetry, there are four possible spin-rotation parameters: $\varepsilon_{a a}, \varepsilon_{b b}$, and $\varepsilon_{c c}$ (diagonal) and the off-diagonal contribution $\left(\left(\varepsilon_{a b}+\varepsilon_{b a}\right) / 2\right)$ [26].


Figure 6. Expanded view of the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition of SrSH. The six branches of the $(0-0)$ subband are shown with J values. This subband has the structure of a parallel type transition, with $\sim 2 B$ spaced branches present. The $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition of CaSH , which is not shown, has a similar appearance.

For CaSH 52 lines in the $(0-0)$ subband of the $\tilde{C}^{2} A^{\prime}-$ $\tilde{X}^{2} A^{\prime}$ transition were recorded. These data are available as supplemental material from the journal. A combined (weighted) fit of the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ data, in addition to the previous millimetre-wave data of the $\tilde{X}^{2} A^{\prime}$ state $\left(0.0000015 \mathrm{~cm}^{-1}\right)$ [14] and $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}\left(0.005 \mathrm{~cm}^{-1}\right)$ [6] and $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}\left(0.004 \mathrm{~cm}^{-1}\right)$ [8] transitions was performed and the results are shown in table 1. The estimated errors for the lines used in the fits are given in parenthesis. Because of the limited data set for the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition, only the average values for the rotation $((B+C) / 2)$ and spin-rotation $\left(\left(\varepsilon_{b b}+\varepsilon_{c c}\right) / 2\right)$ parameters could be determined. In the $\tilde{C}^{2} A^{\prime}$ state, the $A$ rotational constant was fixed to the ground state value [14] and the $\varepsilon_{a a}$ parameter was fixed to zero.

For $\mathrm{SrSH}, 195,204$, and 67 lines were measured for the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$, and $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transitions, respectively. These data are available from the journal as supplemental material. A combined (weighted) fit of this data $\left(0.003 \mathrm{~cm}^{-1}\right)$ with the previously published millimetre wave data $\left(0.0000017 \mathrm{~cm}^{-1}\right)$ [15] was performed and the results are given in table 2. Because transitions involving both the $(1-0)$ and ( $0-0$ ) subbands were observed for the $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ transitions of SrSH , all three rotational constants along with the four spin-rotation parameters could be determined individually for the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states. Centrifugal distortion corrections to the rotational constants were not required for the $\tilde{A}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}$, and $\tilde{C}^{2} A^{\prime}$ states due to the low $J$ values observed in
this work. For the $\tilde{B}^{2} A^{\prime \prime}$ state, however, the $\Delta_{K N}^{s}$ spin-rotation centrifugal distortion correction was found to improve the quality of the fit, suggesting a perturbation in the rotational energy levels of the $\tilde{B}^{2} A^{\prime \prime}$ state. For the $\tilde{C}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}$ transition of SrSH , again a limited data set was measured; therefore, only the average values of $((B+C) / 2)$ and $\left(\left(\varepsilon_{b b}+\varepsilon_{c c}\right) / 2\right)$ could be determined. Again, the $A$ rotational parameter was fixed to the ground state value [15] and the $\varepsilon_{a a}$ constant was fixed to zero.

## 5. Discussion

Calcium and strontium monohydrosulfide each possess an unpaired electron located on the metal atom. Because of the low molecular symmetry of these species, the resulting fine structure is modelled only as spin-rotation coupling. For heavy molecules, the first-order contribution to this interaction is generally negligible and second-order spin-orbit coupling effects tend to dominate [27]. The $\tilde{A}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}$, and $\tilde{C}^{2} A^{\prime}$ states of calcium and strontium monohydrosulfide can be viewed, in the linear limit, as an interacting $p(\pi) / p(\sigma)$ complex. Therefore, using perturbation theory and the pure precession approximation, the second order contribution can be expressed as [28, 29]:

$$
\begin{equation*}
\varepsilon_{\alpha \alpha}^{(2)}=\sum_{n \neq 0} \frac{4 B_{\alpha}\left\langle\psi_{0}\right| \hat{\ell}_{\alpha}\left|\psi_{n}\right\rangle\left\langle\psi_{n}\right| \zeta_{4 p} \hat{\ell}_{\alpha}\left|\psi_{0}\right\rangle}{E_{n}^{0}-E_{0}^{0}} \tag{1}
\end{equation*}
$$

where $\alpha$ represents the principal axis system of the molecule $\left(B_{a}=A, B_{b}=B, B_{c}=C\right), \zeta_{4 p}$ is the atomic spin-orbit constant for the $4 p$ orbital of strontium ( $3 p$ in the case of calcium), and $E_{n}$ and $E_{0}$ represent the energies $(\mathrm{v}=0)$ of the interacting electronic states. Because the $\tilde{A}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}$, and $\tilde{C}^{2} A^{\prime}$ states are sufficiently isolated from other interacting states, the unique perturber approximation can be utilized and the summation over n connecting states can be removed. Equation (1) can then be cyclically applied to obtain expressions for $\varepsilon_{\alpha \alpha}^{(2)}$ by considering which electronic states can interact as a result of a rotation of the molecule about the $\alpha$ axis. For $\mathrm{CaNH}_{2}$, an asymmetric top molecule, expressions for each spin-rotation parameter in the three lowest-lying excited electronic states have been derived [29]. It is of interest to examine how well these equations apply to the excited states of the lower symmetry metal hydrosulfides.

The calculated second order spin-orbit contributions to the spin-rotation constants of CaSH and SrSH are presented in table 3. The measured values are also listed for comparison. In the $\tilde{A}^{2} A^{\prime}$ state of CaSH , the

Table 1. Spectroscopic parameters (in $\mathrm{cm}^{-1}$ ) for $\mathrm{CaSH}^{\mathrm{a}}{ }^{\text {a }}$

| Parameter $^{\mathrm{b}}$ | $\tilde{X}^{2} A^{\prime}$ | $\tilde{A}^{2} A^{\prime}$ | $\tilde{B}^{2} A^{\prime \prime}$ | $\tilde{C}^{2} A^{\prime}$ |
| :--- | :---: | :---: | :---: | :---: |
| $T$ | 0.0 | $15380.29079(23)$ | $15859.46277(73)$ | $16075.12884(65)$ |
| $A$ | $9.693540(45)$ | $9.090954(77)$ | $10.43552(78)$ | $9.693540^{\mathrm{c}}$ |
| $(B+C) / 2$ | $0.140741287(30)$ | $0.14614820(33)$ | $0.142292(13)$ | $0.144783(15)$ |
| $(B-C) / 2$ | $0.00116479(14)$ | $0.0013285(10)$ | $0.001151(75)$ |  |
| $\Delta_{K}$ | $8.880(16) \times 10^{-4}$ | $4.630(36) \times 10^{-4}$ |  |  |
| $\Delta_{N K}$ | $1.20491(84) \times 10^{-5}$ | $2.0039(21) \times 10^{-5}$ |  |  |
| $\Delta_{N}$ | $1.00155(10) \times 10^{-7}$ | $1.2974(13) \times 10^{-7}$ |  |  |
| $\delta_{K}$ | $9.216(55) \times 10^{-6}$ |  |  |  |
| $\delta_{N}$ | $1.834(12) \times 10^{-9}$ |  |  |  |
| $\Phi_{K N}$ | $4.77(11) \times 10^{-9}$ |  |  |  |
| $\Phi_{N K}$ | $7.41(24) \times 10^{-11}$ |  | $-5.77951(93)$ | $0.0^{\mathrm{d}}$ |
| $\varepsilon_{a a}$ | $-0.000583(99)$ | $3.44584(26)$ | $-0.05097(14)$ |  |
| $\left(\varepsilon_{b b}+\varepsilon_{c c}\right) / 2$ | $0.00139806(49)$ | $0.051688(16)$ | $0.03751(36)$ |  |
| $\left(\varepsilon_{b b}-\varepsilon_{c c}\right) / 2$ | $0.0001234(13)$ | $-0.026603(29)$ |  |  |
| $\left(\varepsilon_{a b}+\varepsilon_{b a}\right) / 2$ | $-0.00011281(53)$ | $0.065929(46)$ |  |  |
| $\Delta_{N K}^{s}$ |  | $3.48(58) \times 10^{-5}$ |  |  |
| $\Delta_{K N}^{s}$ | $\Delta_{S}^{s}$ | $-2.93(76) \times 10^{-4}$ |  |  |

${ }^{\text {a }}$ Combined fit includes previously recorded millimetre-wave [14], $\tilde{A}^{2} A^{\prime}-\tilde{X}^{2} A^{\prime}[6]$, and $\tilde{B}^{2} A^{\prime \prime}-\tilde{X}^{2} A^{\prime}$ [8] transition data.
${ }^{\mathrm{b}}$ Values in parenthesis are $1 \sigma$ standard deviations, in units of the last significant digits.
${ }^{\mathrm{c}}$ Fixed to the $\tilde{X}^{2} A^{\prime}$ state value.
${ }^{\mathrm{d}}$ Fixed to zero.

Table 2. Spectroscopic parameters (in $\mathrm{cm}^{-1}$ ) for $\mathrm{SrSH}_{.}{ }^{\mathrm{a}}$

| Parameter $^{\mathrm{b}}$ | $\tilde{X}^{2} A^{\prime}$ | $\tilde{A}^{2} A^{\prime}$ | $\tilde{B}^{2} A^{\prime \prime}$ | $\tilde{C}^{2} A^{\prime}$ |
| :--- | :--- | :---: | :---: | :---: |
| $T$ | 0.0 | $14275.69327(64)$ | $14809.61225(62)$ | $15003.14682(60)$ |
| $A$ | $9.7179(19)$ | $9.23006(79)$ | $9.7334(30)$ | $9.7179^{\mathrm{c}}$ |
| $(B+C) / 2$ | $0.095448499(22)$ | $0.0984682(40)$ | $0.0969202(35)$ | $0.0970991(87)$ |
| $(B-C) / 2$ | $0.00054170(11)$ | $0.00085(12)$ | $0.00247(34)$ |  |
| $\Delta_{N K}$ | $6.4809(16) \times 10^{-6}$ |  |  |  |
| $\Delta_{N}$ | $4.62176(30) \times 10^{-8}$ |  |  |  |
| $\delta_{K}$ | $5.157(37) \times 10^{-6}$ |  |  |  |
| $\delta_{N}$ | $5.680(47) \times 10^{-10}$ |  |  |  |
| $\Phi_{K N}$ | $4.306(84) \times 10^{-9}$ |  |  |  |
| $\Phi_{N K}$ | $2.276(16) \times 10^{-11}$ |  | $-15.1481(57)$ | $0.00^{\mathrm{d}}$ |
| $L_{K}$ | $-2.276(14) \times 10^{-11}$ |  | $0.15852(15)$ |  |
| $\varepsilon_{a a}$ | $0.001740(82)$ | $8.85191(58)$ | $0.01144(74)$ |  |
| $\left(\varepsilon_{b b}+\varepsilon_{c c}\right) / 2$ | $0.0019214(38)$ | $0.24009(10)$ | $0.1063(12)$ |  |
| $\left(\varepsilon_{b b}-\varepsilon_{c c}\right) / 2$ | $-0.0000419(13)$ | $-0.01632(31)$ | $6.56(59) \times 10^{-2}$ |  |
| $\left(\varepsilon_{a b}+\varepsilon_{b a}\right) / 2$ | $-0.000138(11)$ | $0.1667(10)$ |  |  |
| $\Delta_{K N}^{s}$ |  |  |  |  |
| $\Delta_{N}^{s}$ | $-1.14(32) \times 10^{-9}$ |  |  |  |

${ }^{\text {a }}$ Combined fit includes previously recorded millimetre-wave transition data [15].
${ }^{\mathrm{b}}$ Values in parenthesis are $1 \sigma$ standard deviations, in units of the last significant digits.
${ }^{\text {c }}$ Fixed to the $\tilde{X}^{2} A^{\prime}$ state value.
${ }^{\mathrm{d}}$ Fixed to zero.
measured value of $\varepsilon_{a a}$ was found to be nearly $2 \mathrm{~cm}^{-1}$ less than the calculated value. The discrepancy between the measured and calculated value of $\varepsilon_{a a}$ in the $\tilde{A}^{2} A^{\prime}$ state of CaSH was mainly attributed to 'orbital mixing' between
the $\tilde{A}^{2} A^{\prime}$ and $\tilde{C}^{2} A^{\prime}$ states in the non-rotating molecule [6]. This interaction has the effect of lowering the effective orbital angular momentum of the unpaired electron in the $\tilde{A}^{2} A^{\prime}$ state and increasing it in the $\tilde{C}^{2} A^{\prime}$

Table 3. Calculated second-order contributions to the spin-rotation constants of CaSH and SrSH .

|  | CaSH |  |  | SrSH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\tilde{A}^{2} A^{\prime}$ | $\tilde{B}^{2} A^{\prime \prime}$ | $\tilde{C}^{2} A^{\prime}$ | $\tilde{A}^{2} A^{\prime}$ | $\tilde{B}^{2} A^{\prime \prime}$ | $\tilde{C}^{2} A^{\prime}$ |
| $\varepsilon^{\text {(meas) }}$ | 3.44584 | -5.77951 | $0^{\text {a }}$ | 8.85191 | -15.1481 | $0^{\text {a }}$ |
| $\varepsilon_{a a}^{(2)}$ | 5.34 | -5.34 | 0 | 19.4 | -19.4 | 0 |
| $\varepsilon_{\text {bl }}^{\text {ameas) }}$ | 0.025085 | 0.10761 | $-0.05097{ }^{\text {b }}$ | 0.22377 | 0.16996 | $0.06983{ }^{\text {b }}$ |
| $\varepsilon_{b b}^{(2)}$ | 0 | 0.176 | -0.176 | 0 | 0.528 | -0.528 |
| $\varepsilon_{c c}^{\text {meas }}$ | 0.078291 | 0.03259 | $-0.05097^{\text {b }}$ | 0.25641 | 0.14708 | $0.06983{ }^{\text {b }}$ |
| $\varepsilon_{c c}^{(2)}$ | 0.054 | 0 | -0.054 | 0.139 | 0 | -0.139 |

${ }^{\text {a }}$ Fixed to zero in the fit.
${ }^{\mathrm{b}}\left(\varepsilon_{b b}+\varepsilon_{c c}\right) / 2$.
state, which in turn affects the value of $\varepsilon_{a a}$ in the same manner. This phenomenon also appears to be present in the $\tilde{A}^{2} A^{\prime}$ state of SrSH , where the measured value of $\varepsilon_{a a}$ is more than $10 \mathrm{~cm}^{-1}$ less than the calculated value. In contrast, for $\mathrm{CaNH}_{2}$ and $\mathrm{SrNH}_{2}$ the measured values of $\varepsilon_{a a}$ in the $\tilde{A}^{2} B_{2}$ state were found to be in much better agreement with the calculated pure precession values, differing by only 0.043 and $0.018 \mathrm{~cm}^{-1}$, respectively [29, 30]. However, in $\mathrm{CaNH}_{2}$ and $\mathrm{SrNH}_{2}$ this orbital mixing interaction is not possible between the $\tilde{A}^{2} B_{2}$ and $\tilde{C}^{2} A_{1}$ states as they have different symmetries.

Table 3 also contains the calculated second order contributions to the $\varepsilon_{b b}$ and $\varepsilon_{c c}$ spin-rotation constants of CaSH and SrSH . For CaSH , the calculated values of these parameters in the $\tilde{A}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}$, and $\tilde{C}^{2} A^{\prime}$ states are in relatively good agreement with the measured values. The slight differences most likely arise from the assumption of only $p$ atomic orbital character being the dominant contribution to the molecular orbital of the unpaired electron in the excited electronic states. It is certainly possible that d atomic orbital character contributes to the make-up of these molecular orbitals [29].

For SrSH , however, the agreement between the calculated and measured $\varepsilon_{b b}$ and $\varepsilon_{c c}$ constants is not as good. Because of the large values of $\varepsilon_{a a}$ in the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states of SrSH , the spin-components of the $K_{a}=0$ and 1 groups are close in energy in each state. In the $\tilde{A}^{2} A^{\prime}$ state the $K_{a}=1\left(\mathrm{~F}_{1} \quad \Sigma=-1 / 2\right)$ level lies only $\sim 5 \mathrm{~cm}^{-1}$ higher in energy than the spin components of the $K_{a}=0$ level and in the $\tilde{B}^{2} A^{\prime \prime}$ state the separation of the $K_{a}=1\left(\mathrm{~F}_{1} \quad \Sigma=+1 / 2\right)$ level and the $K_{a}=0$ level is even smaller, $\sim 2 \mathrm{~cm}^{-1}$. The matrix elements for the $\left(\varepsilon_{a b}+\varepsilon_{b a}\right) / 2$ parameter mix the $K_{a}=0$ and 1 levels and the selection rule $\Delta \Sigma=0, \pm 1$ causes this interaction to be different for each of the spin components [24]. As a result, the energy positions of each of these spin components will be affected unequally, which in turn changes the measured value of the individual diagonal spin-rotation constants and is largely responsible for their deviation from the calculated values.

The large magnitude of the $\left(\varepsilon_{a b}+\varepsilon_{b a}\right) / 2$ constant in the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states can be interpreted in two different ways: either as a large rotation of the spin axes relative to the inertial axes or as a perturbation. In a molecule with $C_{s}$ symmetry, the inertial a and b axes and the spin axes in the $a-b$ plane can be rotated with respect to each other. In view of the similarity of the electronic structure of CaF and $\mathrm{CaNH}_{2}$ with SrSH [1], a large rotation seems unrealistic. As a result, the interpretation of the large $\left(\varepsilon_{a b}+\varepsilon_{b a}\right) / 2$ parameter as a measure of an accidental internal perturbation between the $K_{a}=0$ and 1 levels in the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states of SrSH is more probable. In this case, the large off-diagonal spinrotation parameter acts as an effective constant that accounts for this perturbation. In fact, the value of $\left(\varepsilon_{a b}+\varepsilon_{b a}\right) / 2$ in the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states is over 1000 times greater than in the ground state. In contrast, for CaSH where the value of $\varepsilon_{a a}$ is smaller, the $K_{a}=0$ and 1 levels lie further apart in energy and the off-diagonal spin-rotation constant is an order of magnitude less in the $\tilde{A}^{2} A^{\prime}$ state as compared to SrSH . In the $\tilde{B}^{2} A^{\prime \prime}$ state of CaSH a value for this parameter could not be determined from the data set observed in the molecular beam experiment [8].

In the $\tilde{C}^{2} A^{\prime}$ state of SrSH , the $\varepsilon_{b b}$ and $\varepsilon_{c c}$ spin-rotation constants (the value of $\left(\varepsilon_{b b}+\varepsilon_{c c}\right) / 2$ is used for both $\varepsilon_{b b}$ and $\varepsilon_{c c}$ ) differ in sign from the calculated value. As mentioned previously, the $\tilde{A}^{2} A^{\prime}$ and $\tilde{C}^{2} A^{\prime}$ states can now interact because they have the same symmetry. This interaction should increase the $\varepsilon_{a a}$ constant in the $\tilde{C}^{2} A^{\prime}$ state from the calculated value of zero to a positive value, shifting the $K_{a}=0$ and 1 levels closer together in energy. As was the case in the $\tilde{A}^{2} A^{\prime}$ state, the close proximity in energy of the $\mathrm{F}_{2} K_{a}=1$ level to the $K_{a}=0$ levels allows them to perturb one another through the off-diagonal spin-rotation constant. In this case, the $\mathrm{F}_{2}$ $K_{a}=0$ level is pushed lower in energy than the $\mathrm{F}_{1} K_{a}=0$ level, which results in a positive $\left(\varepsilon_{b b}+\varepsilon_{c c}\right) / 2$ parameter. As a result, a global fit of the rotational transitions of

Table 4. Second-order corrections to the rotational constants of CaSH and SrSH .

|  | CaSH |  |  | SrSH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\tilde{A}^{2} A^{\prime}$ | $\tilde{B}^{2} A^{\prime \prime}$ | $\tilde{C}^{2} A^{\prime}$ | $\tilde{A}^{2} A^{\prime}$ | $\tilde{B}^{2} A^{\prime \prime}$ | $\tilde{C}^{2} A^{\prime}$ |
| $A^{(2)}$ | 0.7844 | $-0.7844$ | 0 | 0.7075 | -0.7075 | 0 |
| $A$ (meas) | 9.090954 | 10.43552 | $9.693540^{\text {a }}$ | 9.23006 | 9.7334 | $9.7179^{\text {a }}$ |
| $B^{(2)}$ | 0 | +0.00037 | -0.00037 | 0 | +0.00019 | -0.00019 |
| $B$ (meas) | 0.1474767 | 0.143443 | $0.144783{ }^{\text {b }}$ | 0.09932 | 0.09939 | $0.0970991{ }^{\text {b }}$ |
| $C^{(2)}$ | 0.00011 | 0 | -0.00011 | 0.00005 | 0 | -0.00005 |
| $C$ (meas) | 0.1448197 | 0.141141 | $0.144783{ }^{\text {b }}$ | 0.09762 | 0.09445 | $0.0970991{ }^{\text {b }}$ |

the $K_{a}=0$ and $K_{a}=1$ levels would most likely not be possible for the $\tilde{C}^{2} A^{\prime}$ state.

Another possible explanation for the positive value of $\left(\varepsilon_{b b}+\varepsilon_{c c}\right) / 2$ in the $\tilde{C}^{2} A^{\prime}$ state of SrSH is an interaction between this state and one of the excited vibrational levels of the $\tilde{A}^{2} A^{\prime}$ or $\tilde{B}^{2} A^{\prime \prime}$ states. A perturbation of this type was observed in the $K=1$ levels of the $\tilde{B}^{2} A_{1}$ state of $\mathrm{CaCH}_{3}$ [31]. Unfortunately, vibrational energy level information for the excited electronic states of SrSH is scarce. From the low-resolution investigation of SrSH , only a value for the $\mathrm{Sr}-\mathrm{S}$ stretch $\left(\mathrm{v}_{3}\right)$ of $\sim 270 \mathrm{~cm}^{-1}$ was determined for the $\tilde{X}^{2} A^{\prime}, \tilde{A}^{2} A^{\prime}$, and $\tilde{C}^{2} A^{\prime}$ states [6]. Using this value, the $\mathrm{v}_{3}=2$ and 3 vibrational levels in the $\tilde{A}^{2} A^{\prime}$ state are calculated to lie approximately $100 \mathrm{~cm}^{-1}$ below and above the $\tilde{C}^{2} A^{\prime}\left(K_{a}=0\right)$ state. Assuming $v_{3}=270 \mathrm{~cm}^{-1}$ for the $\tilde{B}^{2} A^{\prime \prime}$ state, $v_{3}=1$ lies $\sim 50 \mathrm{~cm}^{-1}$ higher in energy than the $\tilde{C}^{2} A^{\prime}\left(K_{a}=0\right)$ state. In addition, any quanta of the $\mathrm{Sr}-\mathrm{S}$ stretch in the $\tilde{B}^{2} A^{\prime \prime}$ state would have the wrong symmetry to interact with the $\tilde{C}^{2} A^{\prime}$ state. Theoretical calculations on the $\tilde{X}^{2} A^{\prime}$ state of SrSH have given a value of $\sim 335 \mathrm{~cm}^{-1}$ for the bending mode $\left(v_{2}\right)$ [9]. Even assuming this value for the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states, no combination of $\nu_{2}$ and $\nu_{3}$ lies sufficiently close in energy to affect the $\tilde{C}^{2} A^{\prime}\left(K_{a}=0\right)$ state. As a result, this explanation is most likely not responsible for the change in sign of $\left(\varepsilon_{b b}+\varepsilon_{c c}\right) / 2$.

Second-order contributions to the rotational constants in the excited states of CaSH and SrSH are also possible [6, 29, 32]. These contributions have the general form [29]:

$$
\begin{equation*}
B_{\alpha \alpha}^{(2)}=\sum_{n \neq 0} \frac{4 B_{\alpha}^{2}\left\langle\psi_{0}\right| \hat{\ell}_{\alpha}\left|\psi_{n}\right\rangle^{2}}{E_{0}^{0}-E_{n}^{0}} \tag{2}
\end{equation*}
$$

Using the unique perturber approximation, equation (2) can be simplified. Expressions for the second-order contributions to each of the rotational constants of the three low-lying excited electronic states of $\mathrm{CaNH}_{2}$ have been derived [29]. As has been previously discussed for

CaSH [6], a strong Coriolis interaction exists between the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states exists that significantly lowers and raises the $A$ rotational constant in these states, respectively. Second-order contributions to the rotational constants must be taken into consideration in order to derive accurate structural parameters. The second-order contributions to the rotational constants in the $\tilde{A}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}$, and $\tilde{C}^{2} A^{\prime}$ states of CaSH and SrSH are tabulated in table 4 , along with the experimentally determined values for comparison. For CaSH and SrSH , the second-order corrections to the $B$ and $C$ rotational constants comprise less than $0.3 \%$ and $0.5 \%$ of the total measured value, respectively. For SrSH , similar to CaSH , large second-order contributions to the $A$ rotational constant exist in the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states.

By removing the second order contributions to the rotational constants of the excited states of SrSH and CaSH , geometric parameters in these states can be calculated. The $r_{0}$ bond lengths (in $\underset{\sim}{A} \underset{\sim}{\AA}$ ) and bond angle (in degrees) for the $\tilde{A}^{2} A^{\prime}, \tilde{B}^{2} A^{\prime \prime}$, and $\tilde{C}^{2} A^{\prime}$ states of CaSH and SrSH , along with those of the $\tilde{X}^{2} A^{\prime}$ state [11, 14], are tabulated in table 5. These parameters were calculated using the moment of inertia equations for a bent triatomic molecule [33]. Because only one isotopologue of CaSH and SrSH was studied in this work, the $r_{0}$ ( $\mathrm{S}-\mathrm{H}$ ) bond length was held fixed to the ground state value in each excited state. Additionally for the $\tilde{C}^{2} A^{\prime}$ states, the $(\mathrm{M}-\mathrm{S}-\mathrm{H})$ bond angle was held fixed to the ground state value. As a result the calculated geometric parameters in each excited state are exact solutions to the moment of inertia equations. For both CaSH and SrSH , the $r_{0}(\underset{\sim}{\mathrm{M}}-\mathrm{S})$ bond length is found to decrease in the $\tilde{A}^{2} A^{\prime}$ and $\tilde{B}^{2} A^{\prime \prime}$ states as compared to the $\tilde{X}^{2} A^{\prime}$ state value. A similar situation is found in the $\tilde{A}^{2} \Pi$ state of other linear calcium and strontium containing radicals [34]. This behaviour is thought to be due to the polarization of the unpaired electron away from the ligand, which in turn allows for an increase in the electrostatic interaction between the metal cation and anionic ligand. In the $\tilde{C}^{2} A^{\prime}$ states, the $r_{0}(\mathrm{M}-\mathrm{S})$ bond

Table 5. Structural parameters for CaSH and SrSH .

|  | CaSH |  |  |  | SrSH |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\tilde{X}^{2} A^{\prime}$ | $\tilde{A}^{2} A^{\prime}$ | $\tilde{B}^{2} A^{\prime \prime}$ | $\tilde{C}^{2} A^{\prime}$ | $\tilde{X}^{2} A^{\prime}$ | $\tilde{A}^{2} A^{\prime}$ | $\tilde{B}^{2} A^{\prime \prime}$ | $\tilde{C}^{2} A^{\prime}$ |
| $r_{0}(\mathrm{M}-\mathrm{S})(\mathrm{A})$ | 2.564 | 2.517 | 2.550 | 2.562 | 2.706 | 2.665 | 2.686 | 2.720 |
| $r_{0}(\mathrm{~S}-\mathrm{H})(\mathrm{A})$ | 1.357 | $1.357^{\text {a }}$ | $1.357^{\text {a }}$ | $1.357^{\text {a }}$ | 1.359 | $1.359^{\text {a }}$ | $1.359^{\text {a }}$ | $1.359^{\text {a }}$ |
| $\theta(\mathrm{M}-\mathrm{S}-\mathrm{H})\left(^{\circ}\right.$ ) | 91.0 | 89.1 | 89.1 | $91.0^{\text {a }}$ | 91.0 | 89.1 | 89.1 | $91.0^{\text {a }}$ |

${ }^{\text {a }}$ Fixed to the $\tilde{X}^{2} A^{\prime}$ state value.
lengths remain essentially unchanged from the ground state value. Caution of course must be used in interpreting these structural parameters considering the assumptions involved in their derivation. Highresolution spectra of isotopologues of these species would be useful in determining these structural parameters more precisely.

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## Supplementary Material

Table S1. Measured Data for the $A 2 A^{\prime}-X 2 A^{\prime}, B 2 A^{\prime \prime}-X 2 A^{\prime}$, and $C 2 A^{\prime}-X 2 A^{\prime}$ transitions of SrSH and the $C 2 A^{\prime}-X 2 A^{\prime}$ transition of CaSH .
$J=J$
$\mathrm{GAM}=N-K a+K c$
$\mathrm{F}=$ spin component $1=\mathrm{F} 1$ or $2=\mathrm{F} 2$
$K a=K a$
OBS $=$ observed transition frequency in wavenumbers
$\mathrm{OMC}=$ observed transition frequency minus calculated transition frequency in wavenumbers


Table S1. Continued.

| $J$ | GAM | F | Ka | $J$ | GAM F | F K | Ka | OBS | OMC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7.5 | 0 | 1 | 1 | 7.5 |  | 1 |  | 14281.2735 | 0.0002 |
| 8.5 | 0 | 1 | 1 | 8.5 | 01 | 1 |  | 14281.4187 | 0.0052 |
| 9.5 | 0 | 1 | 1 | 9.5 | 01 | 1 |  | 14281.5613 | 0.0014 |
| 10.5 | 0 | 1 | 1 | 10.5 | 01 | 1 |  | 14281.7113 | -0.0011 |
| 12.5 | 0 | 1 | 1 | 12.5 | 0 | 1 | 0 | 14282.0332 | -0.0025 |
| 1.5 | 0 | 1 | 1 | 0.5 | 02 | 2 |  | 14280.5651 | -0.0019 |
| 2.5 | 0 | 1 | 1 | 1.5 | 0 | 2 |  | 14280.6659 | -0.0054 |
| 3.5 | 0 | 1 | 1 | 2.5 | 0 | 2 | 0 | 14280.7843 | 0.0024 |
| 4.5 | 0 | 1 | 1 | 3.5 | 0 | 2 |  | 14280.8947 | -0.0042 |
| 5.5 | 0 | 1 | 1 | 4.5 | 02 | 2 |  | 14281.0226 | 0.0003 |
| 6.5 | 0 | 1 | 1 | 5.5 | 02 | 2 |  | 14281.1481 | -0.0038 |
| 7.5 | 0 | 1 | 1 | 6.5 | 02 | 2 |  | 14281.2853 | -0.0025 |
| 8.5 | 0 | 1 | 1 | 7.5 | 0 | 2 |  | 14281.4328 | 0.0030 |
| 9.5 | 0 | 1 | 1 | 8.5 | 0 | 2 |  | 14281.5800 | 0.0019 |
| 10.5 | 0 | 1 | 1 | 9.5 | 02 | 2 |  | 14281.7336 | 0.0011 |
| 12.5 | 0 | 1 | 1 | 11.5 | 0 | 2 |  | 14282.0616 | 0.0019 |
| 0.5 | 1 | 1 | 1 | 1.5 | 0 | 2 | 0 | 14279.8983 | -0.0001 |
| 1.5 | 0 | 1 | 1 | 2.5 | 02 | 2 |  | 14279.6104 | -0.0041 |
| 2.5 | 0 | 1 | 1 | 3.5 | 0 | 2 |  | 14279.3375 | 0.0006 |
| 3.5 | 0 | 1 | 1 | 4.5 | 0 | 2 | 0 | 14279.0670 | 0.0012 |
| 4.5 | 0 | 1 | 1 | 5.5 | 0 | 2 |  | 14278.7980 | -0.0031 |
| 5.5 | 0 | 1 | 1 | 6.5 | 02 | 2 |  | 14278.5380 | -0.0046 |
| 6.5 | 0 | 1 | 1 | 7.5 | 0 | 2 | 0 | 14278.2872 | -0.0033 |
| 7.5 | 0 | 1 | 1 | 8.5 | 02 | 2 |  | 14278.0435 | -0.0012 |
| 8.5 | 0 | 1 | 1 | 9.5 | 0 | 2 |  | 14277.8121 | 0.0070 |
| 9.5 | 0 | 1 | 1 | 10.5 | 02 | 2 |  | 14277.5786 | 0.0069 |
| 10.5 | 0 | 1 |  | 11.5 | 0 | 2 |  | 14277.3399 | -0.0045 |
| 1.5 |  | 2 | 1 | 2.5 | 0 | 1 |  | 14288.8545 | 0.0035 |
| 2.5 | 0 | 2 | 1 | 3.5 | 01 | 1 |  | 14288.7721 | 0.0018 |
| 3.5 |  | 2 | 1 | 4.5 | 0 | 1 |  | 14288.7007 | 0.0048 |
| 4.5 |  | 2 |  | 5.5 | 0 | 1 |  | 14288.6220 | -0.0057 |
| 5.5 |  | 2 | 1 | 6.5 | 0 | 1 |  | 14288.5624 | -0.0034 |
| 6.5 |  | 2 | 1 | 7.5 | 01 | 1 |  | 14288.5088 | -0.0013 |
| 7.5 |  | 2 | 1 | 8.5 | 0 | 1 |  | 14288.4621 | 0.0015 |
| 8.5 |  | 2 | 1 | 9.5 | 0 | 1 |  | 14288.4191 | 0.0017 |
| 9.5 |  | 2 |  | 10.5 | 01 | 1 |  | 14288.3846 | 0.0042 |
| 10.5 |  | 2 | 1 | 11.5 | 0 | 1 |  | 14288.3527 | 0.0030 |
| 11.5 |  | 2 | 1 | 12.5 | 0 | 1 |  | 14288.3206 | -0.0046 |
| 12.5 | 0 | 2 | 1 | 13.5 | 01 | 1 |  | 14288.3134 | 0.0064 |
| 13.5 |  | 2 | 1 | 14.5 | 01 | 1 |  | 14288.2887 | -0.0063 |
| 14.5 |  | 2 | 1 | 15.5 | 0 | 1 |  | 14288.2887 | -0.0006 |
| 15.5 |  | 2 | 1 | 16.5 | 01 | 1 |  | 14288.2887 | -0.0012 |
| 1.5 |  | 2 | 1 | 1.5 | 0 | 2 |  | 14288.8545 | -0.0013 |
| 2.5 |  | 2 | 1 | 2.5 | 0 | 2 |  | 14288.7792 | 0.0022 |
| 3.5 |  | 2 | 1 | 3.5 | 0 | 2 |  | 14288.7093 | 0.0048 |
| 4.5 |  | 2 | 1 | 4.5 | 0 | 2 |  | 14288.6319 | -0.0064 |
| 5.5 |  | 2 | 1 | 5.5 | 0 | 2 |  | 14288.5753 | -0.0030 |
| 6.5 |  | 2 | 1 | 6.5 |  | 2 |  | 14288.5223 | -0.0022 |
| 7.5 | 0 | 2 | 1 | 7.5 | 0 | 2 |  | 14288.4794 | 0.0024 |
| 8.5 |  | 2 | 1 | 8.5 | 0 | 2 |  | 14288.4375 | 0.0018 |
| 9.5 |  | 2 |  | 9.5 |  | 2 |  | 14288.4031 | 0.0025 |
| 10.5 | 0 | 2 | 1 | 10.5 | 0 | 2 |  | 14288.3772 | 0.0054 |
| 11.5 | 0 | 2 | 1 | 11.5 | 02 | 2 |  | 14288.3527 | 0.0035 |
| 12.5 |  | 2 |  | 12.5 | 0 | 2 |  | 14288.3305 | -0.0024 |
| 13.5 | 0 | 2 | 1 | 13.5 | 0 | 2 | 0 | 14288.3206 | -0.0023 |

Table S1. Continued.

| $J$ | GAM | F | Ka J | GAM F | F Ka | Ka OBS | OMC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 14.5 | 0 | 2 | 114.5 | 02 | 20 | 014288.3206 | 0.0015 |
| 15.5 | 0 | 2 | 115.5 | 02 | 20 | 014288.3206 | -0.0010 |
| 1.5 | 0 | 2 | 10.5 | 0 | 0 | 014289.4265 | 0.0009 |
| 2.5 | 0 | 2 | 11.5 | 0 | 0 | 014289.7241 | -0.0026 |
| 3.5 | 0 | 2 | 2.5 | 0 | 0 | 014290.0292 | -0.0049 |
| 4.5 | 0 | 2 | 13.5 | 0 | 0 | 014290.3496 | 0.0019 |
| 5.5 | 0 | 2 | 4.5 | 0 | 0 | 014290.6651 | -0.0024 |
| 6.5 | 0 | 2 | 15.5 | 0 | 0 | 014290.9922 | -0.0014 |
| 7.5 | 0 | 2 | 16.5 | 0 | 0 | 014291.3231 | -0.0027 |
| 8.5 | 0 | 2 | 17.5 | 0 | 0 | 014291.6577 | -0.0066 |
| 9.5 | 0 | 2 | 8.5 | 0 | 0 | 014292.0070 | -0.0021 |
| 10.5 | 0 | 2 | 19.5 | 0 |  | 014292.3650 | 0.0050 |
| 11.5 | 0 | 2 | 110.5 | 0 | 0 | 014292.7217 | 0.0045 |
| 1.5 | 1 | 2 | 11.5 | 0 | 0 | 014289.2358 | 0.0020 |
| 2.5 | 1 | 2 | 12.5 | 0 |  | 014289.3416 | -0.0025 |
| 3.5 | 1 | 2 | 3.5 | 0 | 0 | 014289.4634 | 0.0027 |
| 4.5 | 1 | 2 | 14.5 | 0 | 0 | 014289.5824 | -0.0013 |
| 5.5 | 1 | 2 | 15.5 | 0 |  | 014289.7151 | 0.0020 |
| 6.5 | 1 | 2 | 16.5 | 0 | 0 | 014289.8508 | 0.0018 |
| 7.5 | 1 | 2 | 17.5 | 0 | 0 | 014289.9959 | 0.0047 |
| 8.5 | 1 | 2 | 18.5 | 0 | 0 | 014290.1388 | -0.0012 |
| 9.5 | 1 | 2 | 19.5 | 0 | 0 | 014290.2961 | 0.0009 |
| 10.5 | 1 | 2 | 110.5 | 0 | 0 | 014290.4572 | 0.0002 |
| 11.5 | 1 | 2 | 111.5 | 0 | 0 | 014290.6269 | 0.0016 |
| 12.5 | 1 | 2 | 112.5 | 01 | 0 | 014290.8052 | 0.0049 |
| 13.5 | 1 | 2 | 113.5 | 0 | 0 | 014290.9824 | 0.0006 |
| 1.5 | 1 | 2 | 10.5 | 02 | 0 | 014289.2358 | -0.0009 |
| 2.5 | 1 | 2 | 11.5 | 02 | 0 | 014289.3416 | -0.0073 |
| 3.5 | 1 | 2 | 12.5 | 02 | 0 | 014289.4634 | -0.0041 |
| 4.5 | 1 | 2 | 13.5 | 02 |  | 014289.5900 | -0.0024 |
| 5.5 | 1 | 2 | 14.5 | 02 | 0 | 014289.7241 | 0.0004 |
| 6.5 | 1 | 2 | 15.5 | 02 | 0 | 014289.8631 | 0.0016 |
| 7.5 |  | 2 | 16.5 | 02 |  | 014290.0058 | 0.0001 |
| 8.5 | 1 | 2 | 17.5 | 02 | 0 | 014290.1571 | 0.0008 |
| 9.5 | 1 | 2 | 18.5 | 02 | 0 | 014290.3159 | 0.0024 |
| 10.5 | 1 | 2 | 19.5 | 02 | 0 | 014290.4781 | 0.0009 |
| 11.5 | 1 | 2 | 110.5 | 02 | 20 | 014290.6479 | 0.0005 |
| 12.5 | 1 | 2 | 111.5 | 02 | 0 | 014290.8254 | 0.0011 |
| 13.5 |  | 2 | 112.5 | 02 |  | 014291.0039 | -0.0039 |
| 1.5 | 1 | 2 | 12.5 | 02 | 0 | 014288.2801 | -0.0040 |
| 0.5 | 0 | 1 | 01.5 | 0 | 0 | 014275.5022 | 0.0008 |
| 1.5 | 0 | 1 | $0 \quad 2.5$ | 0 | 0 | 014275.4360 | 0.0011 |
| 2.5 | 0 | 1 | $0 \quad 3.5$ | 0 | 0 | 014275.3759 | 0.0025 |
| 3.5 | 0 | 1 | 04.5 | 0 | 0 | 014275.3202 | 0.0033 |
| 4.5 | 0 | 1 | 05.5 | 0 | 0 | 014275.2661 | 0.0006 |
| 5.5 | 0 | 1 | 06.5 | 0 | 0 | 014275.2193 | 0.0003 |
| 6.5 | 0 | 1 | 07.5 | 0 | 0 | 014275.1752 | -0.0025 |
| 7.5 | 0 | 1 | 08.5 | 0 | 0 | 014275.1392 | -0.0021 |
| 8.5 | 0 | 1 | 09.5 | 0 | 0 | 014275.1064 | -0.0035 |
| 9.5 | 0 | 1 | 010.5 | 0 |  | 014275.0841 | 0.0005 |
| 10.5 | 0 | 1 | 011.5 | 0 | 0 | 014275.0596 | -0.0028 |
| 11.5 | 0 | 1 | 012.5 | 01 | 0 | 014275.0473 | 0.0011 |
| 12.5 | 0 | 1 | 013.5 | 0 |  | 014275.0350 | -0.0001 |
| 0.5 | 0 | 1 | 00.5 | 02 | 20 | 014275.5022 | -0.0021 |
| 1.5 | 0 | 1 | $0 \quad 1.5$ | 02 | 20 | 014275.4360 | -0.0037 |

Table S1. Continued.

| $J$ | GAM | F | Ka | K J | GAM F | F Ka |  | OBS | OMC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.5 | 0 | ) 1 | 0 | 2.5 |  | 2 |  | 14275.3821 | 0.0020 |
| 3.5 | 0 | 1 | 0 | 03.5 | 0 | 2 | 0 | 14275.3273 | 0.0017 |
| 4.5 | 0 | ) 1 | 0 | 4.5 | 0 | 2 |  | 14275.2784 | 0.0024 |
| 5.5 | 0 | ) 1 |  | 5.5 |  | 2 |  | 14275.2317 | 0.0002 |
| 6.5 | 0 | 1 | 0 | 6.5 | 0 | 2 |  | 14275.1923 | 0.0002 |
| 7.5 | 0 | ) 1 | 0 | 7.5 | 0 | 2 |  | 14275.1555 | -0.0021 |
| 8.5 | 0 | ) 1 |  | 8.5 |  | 2 |  | 14275.1259 | -0.0023 |
| 9.5 | 0 | 1 | 0 | 9.5 |  | 2 |  | 14275.1064 | 0.0026 |
| 10.5 | 0 | ) 1 |  | 010.5 | 0 | 2 |  | 14275.0841 | -0.0004 |
| 11.5 | 0 | ) 1 |  | 011.5 |  | 2 |  | 14275.0711 | 0.0009 |
| 12.5 | 0 | 1 |  | 12.5 |  | 2 |  | 14275.0596 | -0.0014 |
| 13.5 | 0 | 1 |  | 013.5 | 02 | 2 |  | 14275.0596 | 0.0027 |
| 1.5 | 0 | 02 |  | 0.5 | 0 | 2 |  | 14275.7262 | -0.0051 |
| 2.5 | 0 | 02 |  | 1.5 |  | 2 |  | 14275.8171 | -0.0011 |
| 3.5 | 0 | 02 |  | 2.5 |  | 2 |  | 14275.9082 | -0.0019 |
| 4.5 | 0 | 02 |  | 3.5 | 0 | 2 |  | 14276.0091 | 0.0020 |
| 5.5 | 0 | 02 |  | 4.5 | 0 | 2 |  | 14276.1052 | -0.0041 |
| 6.5 | 0 | 02 |  | 5.5 |  | 2 |  | 14276.2206 | 0.0039 |
| 7.5 | 0 | 02 |  | 6.5 | 0 | 2 |  | 14276.3290 | -0.0003 |
| 8.5 | 0 | 02 |  | 7.5 | 02 | 2 |  | 14276.4422 | -0.0049 |
| 9.5 | 0 | 02 |  | 8.5 |  | 2 |  | 14276.5774 | 0.0072 |
| 10.5 | 0 | 02 |  | 9.5 | 0 | 2 |  | 14276.6980 | -0.0006 |
| 11.5 | 0 | 02 |  | 010.5 | 0 | 2 |  | 14276.8332 | 0.0008 |
| 12.5 | 0 | 02 |  | 011.5 |  | 2 |  | 14276.9759 | 0.0044 |
| 13.5 | 0 | 02 |  | 012.5 | 0 | 2 |  | 14277.1088 | -0.0072 |
| 14.5 | 0 | 02 |  | 013.5 | 02 | 2 |  | 14277.2687 | 0.0028 |
| 16.5 | 0 | 02 |  | 015.5 | 0 | 2 |  | 14277.5786 | -0.0036 |
| 0.5 | 0 | 02 |  | 0.5 | 0 | , |  | 14275.6498 | 0.0011 |
| 1.5 | 0 | 02 |  | 1.5 | 0 | 1 |  | 14275.7262 | -0.0023 |
| 2.5 | 0 | 02 |  | 2.5 | 0 | 1 |  | 14275.8171 | 0.0038 |
| 3.5 | 0 | 02 |  | 3.5 | 0 | 1 |  | 14275.9082 | 0.0049 |
| 4.5 | 0 | 02 |  | 4.5 | 0 | 1 |  | 14275.9982 | -0.0003 |
| 5.5 | 0 | 02 |  | 5.5 | 0 | 10 |  | 14276.0986 | -0.0002 |
| 6.5 | 0 | 02 |  | 6.5 | 0 | 10 |  | 14276.2060 | 0.0018 |
| 7.5 | 0 | 02 |  | 7.5 | 0 | 10 |  | 14276.3143 | -0.0006 |
| 8.5 | 0 | 02 |  | 8.5 | 0 | 1 |  | 14276.4274 | -0.0034 |
| 9.5 | 0 | 02 |  | 9.5 |  | 10 |  | 14276.5554 | 0.0034 |
| 10.5 | 0 | 02 |  | 010.5 | 0 | 10 |  | 14276.6807 | 0.0022 |
| 11.5 | 0 | 02 |  | 011.5 | 0 | 1 |  | 14276.8112 | 0.0009 |
| 12.5 | 0 | 02 |  | 012.5 | 0 | 1 |  | 14276.9464 | -0.0011 |
| 13.5 | 0 | 02 |  | 013.5 | 0 | 1 |  | 14277.0867 | -0.0033 |
| 14.5 |  | 02 |  | 014.5 | 0 | 1 |  | 14277.2329 | -0.0051 |
| 16.5 | 0 | 02 |  | 016.5 | 01 | 1 |  | 14277.5563 | 0.0058 |
| SrSH |  |  |  | B2A ${ }^{\prime \prime}$ | "-X2A ${ }^{\prime}$ |  |  |  |  |
| 1.5 |  | 01 |  | 1.5 | 0 | 1 |  | 14811.6946 | -0.0006 |
| 2.5 |  | 01 |  | 2.5 | 0 | 1 |  | 14811.7967 | -0.0019 |
| 3.5 |  | 0 |  | 3.5 | 0 |  |  | 14811.9061 | 0.0006 |
| 4.5 | 0 | 01 | 1 | 4.5 | 0 | 1 |  | 14812.0189 | 0.0030 |
| 5.5 | 0 | 01 |  | 5.5 | 0 | 1 |  | 14812.1345 | 0.0046 |
| 6.5 |  | 01 |  | 6.5 | 0 | 1 |  | 14812.2493 | 0.0020 |
| 7.5 |  | 0 |  | 7.5 | 0 | 1 |  | 14812.3724 | 0.0042 |
| 8.5 |  | 01 |  | 8.5 | 01 | 1 |  | 14812.4953 | 0.0028 |
| 9.5 |  | 01 |  | 9.5 | 0 | 1 |  | 14812.6290 | 0.0088 |
| 10.5 |  | 01 |  | 110.5 | 01 | 1 |  | 14812.7568 | 0.0056 |
| 11.5 |  | 0 |  | 111.5 | 01 | 1 | 0 | 14812.8903 | 0.0048 |

Table S1. Continued.

| $J$ | GAM | F |  | $J$ | GAM |  | Ka | a OBS | OMC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 12.5 | 0 | 1 | 1 | 12.5 |  | 01 |  | 014813.0169 | -0.0062 |
| 1.5 | 0 | 1 | 1 | 2.5 |  | 02 |  | 014810.7426 | -0.0029 |
| 2.5 | 0 | 1 | 1 | 3.5 |  | 02 | 0 | 014810.4695 | 0.0005 |
| 3.5 | 0 | 1 | 1 | 4.5 |  | 02 | 0 | 014810.1946 | -0.0015 |
| 4.5 | 0 | 1 | 1 | 5.5 |  | 02 | 0 | 014809.9267 | 0.0000 |
| 5.5 | 0 | 1 | 1 | 6.5 |  | 02 | 0 | 014809.6598 | -0.0010 |
| 6.5 | 0 | 1 | 1 | 7.5 |  | 02 | 0 | 014809.3988 | 0.0004 |
| 7.5 | 0 | 1 | 1 | 8.5 |  | 02 | 0 | 014809.1418 | 0.0023 |
| 8.5 | 0 | 1 | 1 | 9.5 |  | 02 | 0 | 014808.8858 | 0.0018 |
| 1.5 | 0 | 1 | 1 | 0.5 |  | 02 | 0 | 014811.6946 | -0.0035 |
| 2.5 | 0 | 1 | 1 | 1.5 |  |  | 0 | 014811.7967 | -0.0067 |
| 3.5 | 0 | 1 | 1 | 2.5 |  | 02 | 0 | 014811.9061 | -0.0061 |
| 4.5 | 0 | 1 | 1 | 3.5 |  | 02 | 0 | 014812.0230 | -0.0016 |
| 5.5 | 0 | 1 | 1 | 4.5 |  | 02 | 0 | 014812.1416 | 0.0011 |
| 6.5 | 0 | 1 | 1 | 5.5 |  | 02 | 0 | 014812.2617 | 0.0019 |
| 7.5 | 0 | 1 | 1 | 6.5 |  | 02 | 0 | 014812.3859 | 0.0033 |
| 8.5 | 0 | 1 | 1 | 7.5 |  | 02 | 0 | 014812.5138 | 0.0050 |
| 9.5 | 0 | 1 | 1 | 8.5 |  | 02 | 0 | 014812.6463 | 0.0079 |
| 10.5 | 0 | 1 | 1 | 9.5 |  | 02 | 0 | 014812.7770 | 0.0056 |
| 11.5 | 0 | 1 |  | 10.5 |  | 02 | 0 | 014812.9156 | 0.0080 |
| 12.5 | 0 | 1 | 1 | 11.5 |  | 02 | 0 | 014813.0394 | -0.0077 |
| 1.5 | 1 | 1 | 1 | 0.5 |  | 0 | 0 | 014811.8884 | 0.0014 |
| 2.5 | 1 | 1 | 1 | 1.5 |  | 0 | 0 | 014812.1817 | 0.0004 |
| 3.5 | 1 | 1 | 1 | 2.5 |  | 0 | 0 | 014812.4781 | -0.0011 |
| 4.5 | 1 | 1 | 1 | 3.5 |  | 0 | 0 | 014812.7770 | -0.0035 |
| 5.5 | 1 | 1 | 1 | 4.5 |  | 0 | 0 | 014813.0882 | 0.0029 |
| 6.5 | 1 | 1 | 1 | 5.5 |  | 0 | 0 | 014813.3908 | -0.0028 |
| 7.5 | 1 | 1 | 1 | 6.5 |  | 0 |  | 014813.7081 | 0.0028 |
| 8.5 | 1 | 1 | 1 | 7.5 |  | 0 |  | 014814.0194 | -0.0010 |
| 9.5 | 1 | 1 | 1 | 8.5 |  | 0 | 0 | 014814.3403 | 0.0015 |
| 10.5 | 1 | 1 | 1 | 9.5 |  | 0 |  | 014814.6638 | 0.0033 |
| 1.5 | 1 | 1 | 1 | 1.5 |  | 02 |  | 014811.3119 | -0.0053 |
| 2.5 | 1 | 1 | 1 | 2.5 |  | 02 | 0 | 014811.2252 | -0.0065 |
| 3.5 | 1 | 1 | 1 | 3.5 |  | 02 | 0 | 014811.1448 | -0.0048 |
| 4.5 | 1 | 1 | 1 | 4.5 |  | 02 |  | 014811.0648 | -0.0063 |
| 5.5 | 1 | 1 | 1 | 5.5 |  | 02 | 0 | 014810.9962 | 0.0001 |
| 6.5 | 1 | 1 | 1 | 6.5 |  | 02 | 0 | 014810.9234 | -0.0011 |
| 7.5 | 1 | 1 | 1 | 7.5 |  | 02 |  | 014810.8520 | -0.0044 |
| 8.5 | 1 | 1 | 1 | 8.5 |  |  |  | 014810.7868 | -0.0049 |
| 9.5 | 1 | 1 | 1 | 9.5 |  | 02 |  | 014810.7277 | -0.0027 |
| 10.5 | 1 | 1 |  | 10.5 |  | 02 |  | 014810.6712 | -0.0011 |
| 11.5 | 1 | 1 |  | 11.5 |  |  |  | 014810.6134 | -0.0041 |
| 12.5 |  | 1 |  | 12.5 |  | 02 |  | 014810.5667 | 0.0008 |
| 13.5 | 1 | 1 |  | 13.5 |  | 02 | 0 | 014810.5163 | -0.0011 |
| 14.5 | 1 | 1 |  | 14.5 |  |  |  | 014810.4695 | -0.0024 |
| 15.5 |  | 1 |  | 15.5 |  | 02 |  | 014810.4312 | 0.0018 |
| 1.5 | 1 | 1 | 1 | 2.5 |  | 0 | 0 | 014811.3119 | -0.0005 |
| 2.5 | 1 | 1 | 1 | 3.5 |  | 0 |  | 014811.2252 | 0.0003 |
| 3.5 |  | 1 |  | 4.5 |  | 0 |  | 014811.1448 | 0.0038 |
| 4.5 | 1 | 1 | 1 | 5.5 |  | 0 | 0 | 014811.0648 | 0.0043 |
| 5.5 | 1 | 1 | 1 | 6.5 |  | 0 | 0 | 014810.9894 | 0.0058 |
| 6.5 |  | 1 |  | 7.5 |  | 0 |  | 014810.9099 | -0.0002 |
| 7.5 | 1 | 1 | 1 | 8.5 |  | 0 | 0 | 014810.8360 | -0.0041 |
| 8.5 | 1 | 1 | 1 | 9.5 |  | 0 | 0 | 014810.7721 | -0.0014 |

Table S1. Continued.

| $J$ | GAM F | $K a$ | $J$ | GAM F | $K a$ | a OBS | OMC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9.5 | 11 | 1 | 10.5 | 01 |  | 14810.7093 | -0.0009 |
| 10.5 | 11 | 1 | 11.5 | 01 | 0 | ) 14810.6466 | -0.0036 |
| 11.5 | 1 | 1 | 12.5 | 0 | 0 | ) 14810.5975 | 0.0040 |
| 12.5 | 1 | 1 | 13.5 | 01 | 0 | 14810.5409 | 0.0010 |
| 13.5 | 1 | 1 | 14.5 | 01 | 0 | 14810.4894 | -0.0001 |
| 14.5 | 11 | 1 | 15.5 | 01 | 0 | ) 14810.4417 | -0.0005 |
| 15.5 | 1 | 1 | 16.5 | 0 | 0 | 14810.3939 | -0.0039 |
| 1.5 | 02 | 1 | 0.5 | 01 | 0 | ) 14827.1661 | -0.0033 |
| 3.5 | 02 | 1 | 2.5 | 0 | 0 | ) 14827.7671 | 0.0020 |
| 4.5 | 02 | 1 | 3.5 | 01 | 0 | 14828.0717 | 0.0041 |
| 5.5 | 02 | 1 | 4.5 | 01 | 0 | ) 14828.3699 | -0.0033 |
| 6.5 | 02 | 1 | 5.5 | 01 | 0 | ) 14828.6823 | 0.0004 |
| 0.5 | 12 | 1 | 0.5 | 02 | 0 | ) 14826.6811 | 0.0016 |
| 1.5 | 02 | 1 | 1.5 | 02 | 0 | 14826.5986 | -0.0010 |
| 2.5 | 02 | 1 | 2.5 | 02 | 0 | ) 14826.5138 | -0.0022 |
| 3.5 | 02 | 1 | 3.5 | 02 | 0 | ) 14826.4359 | 0.0004 |
| 4.5 | 02 | 1 | 4.5 | 02 | 0 | ) 14826.3600 | 0.0018 |
| 5.5 | 02 | 1 | 5.5 | 02 | 0 | ) 14826.2887 | 0.0048 |
| 6.5 | 02 | 1 | 6.5 | 02 | 0 | ) 14826.2161 | 0.0032 |
| 7.5 | 02 | 1 | 7.5 | 02 | 0 | ) 14826.1485 | 0.0035 |
| 8.5 | 02 | 1 | 8.5 | 02 | 0 | ) 14826.0816 | 0.0012 |
| 9.5 | 02 | 1 | 9.5 | 02 | 0 | ) 14826.0199 | 0.0008 |
| 10.5 | 02 | 1 | 10.5 | 02 | 0 | ) 14825.9603 | -0.0008 |
| 11.5 | 02 | 1 | 11.5 | 02 | 0 | ) 14825.9037 | -0.0028 |
| 12.5 | 02 | 1 | 12.5 | 02 | 0 | 14825.8561 | 0.0008 |
| 13.5 | 02 | 1 | 13.5 | 02 | 0 | ) 14825.8052 | -0.0025 |
| 14.5 | 02 | 1 | 14.5 | 02 | 0 | 14825.7573 | -0.0062 |
| 15.5 | 02 | 1 | 15.5 | 02 | 0 | ) 14825.7271 | 0.0041 |
| 16.5 | 02 | 1 | 16.5 | 02 | 0 | 14825.6823 | -0.0038 |
| 17.5 | 02 | 1 | 17.5 | 02 | 0 | ) 14825.6577 | 0.0048 |
| 0.5 | 12 | 1 | 1.5 | 01 |  | ) 14826.6811 | 0.0045 |
| 1.5 | 02 | 1 | 2.5 | 01 | 0 | ) 14826.5986 | 0.0038 |
| 2.5 | 02 | 1 | 3.5 | 01 |  | ) 14826.5138 | 0.0045 |
| 3.5 | 02 | 1 | 4.5 | 01 | 0 | 14826.4313 | 0.0044 |
| 4.5 | 02 | 1 | 5.5 | 01 | 0 | ) 14826.3502 | 0.0026 |
| 5.5 | 02 | 1 | 6.5 | 0 | 0 | 14826.2739 | 0.0024 |
| 6.5 | 02 | 1 | 7.5 | 01 | 0 | 14826.1999 | 0.0014 |
| 7.5 | 02 | 1 | 8.5 | 0 | 0 | 14826.1313 | 0.0026 |
| 8.5 | 02 | 1 | 9.5 | 01 | 0 | ) 14826.0639 | 0.0017 |
| 9.5 | 02 | 1 | 10.5 | 01 |  | ) 14826.0003 | 0.0014 |
| 10.5 | 02 | 1 | 11.5 | 01 | 0 | 14825.9418 | 0.0028 |
| 11.5 | 02 | 1 | 12.5 | 01 |  | ) 14825.8828 | 0.0003 |
| 12.5 | 02 | 1 | 13.5 | 01 | 0 | ) 14825.8237 | -0.0057 |
| 13.5 | 02 | 1 | 14.5 | 01 |  | 14825.7745 | $-0.0053$ |
| 14.5 | 02 | 1 | 15.5 | 01 | 0 | 14825.7271 | -0.0066 |
| 15.5 | 02 | 1 | 16.5 | 01 |  | ) 14825.6858 | -0.0055 |
| 16.5 | 02 | 1 | 17.5 | 01 | 0 | 14825.6577 | 0.0052 |
| 0.5 | 02 | , | 1.5 | 02 |  | 14826.2995 | -0.0059 |
| 1.5 | 12 | 1 | 2.5 | 02 |  | 14826.0199 | 0.0054 |
| 2.5 | 12 | 1 | 3.5 | 02 |  | ) 14825.7271 | -0.0062 |
| 3.5 | 12 | 1 | 4.5 | 02 |  | ) 14825.4500 | -0.0051 |
| 0.5 | 02 | 1 | 0.5 | 01 |  | ) 14826.8668 | -0.0084 |
| 1.5 |  | 1 | 1.5 | 01 |  | ) 14826.9652 | 0.0011 |
| 2.5 | 12 | 1 | 2.5 | 01 |  | 14827.0636 | 0.0008 |

Table S1. Continued.
$\left.\begin{array}{rrrrrrrrrr}\hline J & \text { GAM } & \mathrm{F} & K a & J & \text { GAM } & \mathrm{F} & K a & \text { OBS } & \text { OMC } \\ \hline 3.5 & 1 & 2 & 1 & 3.5 & 0 & 1 & 0 & 14827.1661 & 0.0017 \\ 4.5 & 1 & 2 & 1 & 4.5 & & 0 & 1 & 0 & 14827.2727 \\ 5.5 & 1 & 2 & 1 & 5.5 & & 0 & 1 & 0 & 14827.3760\end{array}\right)-0.0036$

Table S1. Continued.

| $J$ | GAM F | $K a$ | $J$ | GAM F | $K a$ | a OBS | OMC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.5 | 02 | 0 | 2.5 | 0 | 0 | 14809.8800 | -0.0001 |
| 3.5 | 02 | 0 | 3.5 | 01 | 0 | 14810.0005 | 0.0010 |
| 4.5 | 02 | 0 | 4.5 | 0 | 0 | 14810.1234 | 0.0023 |
| 5.5 | 02 | 0 | 5.5 | 0 | 0 | ) 14810.2468 | 0.0020 |
| 6.5 | 02 | 0 | 6.5 | 0 | 0 | ) 14810.3711 | 0.0005 |
| 7.5 | 02 | 0 | 7.5 | 0 | 0 | 14810.4987 | 0.0002 |
| 8.5 | 02 | 0 | 8.5 | 0 | 0 | 14810.6307 | 0.0022 |
| 10.5 | 02 | 0 | 10.5 | 0 | 0 | ) 14810.8987 | 0.0039 |
| 1.5 | 01 | 0 | 0.5 | 0 | 0 | ) 14809.8800 | -0.0043 |
| 2.5 | 01 | 0 | 1.5 | 0 | 0 | ) 14810.1558 | -0.0017 |
| 3.5 | 01 | 0 | 2.5 | 0 | 0 | ) 14810.4312 | -0.0017 |
| 4.5 | 0 | 0 | 3.5 | 0 | 0 | ) 14810.7093 | -0.0012 |
| 5.5 | 01 | 0 | 4.5 | 01 | 0 | ) 14810.9894 | -0.0010 |
| 6.5 | 0 | 0 | 5.5 | 0 | 0 | ) 14811.2739 | 0.0014 |
| 7.5 | 01 | 0 | 6.5 | 01 | 0 | ) 14811.5556 | -0.0013 |
| 8.5 | 0 | 0 | 7.5 | 0 | 0 | ) 14811.8409 | -0.0026 |
| 9.5 | 01 | 0 | 8.5 | 01 | 0 | ) 14812.1345 | 0.0019 |
| 10.5 | 01 | 0 | 9.5 | 0 | 0 | ) 14812.4253 | 0.0014 |
| 11.5 | 01 | 0 | 10.5 | 01 | 0 | ) 14812.7229 | 0.0053 |
| 0.5 | 01 | 0 | 1.5 | 01 | 0 | ) 14809.4235 | 0.0031 |
| 1.5 | 01 | 0 | 2.5 | 01 | 0 | ) 14809.3128 | 0.0032 |
| 2.5 | 01 | 0 | 3.5 | 01 | 0 | 14809.2033 | 0.0022 |
| 3.5 | 0 | 0 | 4.5 | 01 | 0 | 14809.1012 | 0.0065 |
| 4.5 | 01 | 0 | 5.5 | 01 | 0 | ) 14808.9893 | -0.0012 |
| 5.5 | 0 | 0 | 6.5 | 0 | 0 | ) 14808.8858 | -0.0028 |
| 0.5 | 01 | 0 | 0.5 | 02 | 0 | ) 14809.4235 | 0.0002 |
| 1.5 | 01 | 0 | 1.5 | 02 | 0 | ) 14809.3128 | -0.0016 |
| 2.5 | 01 | 0 | 2.5 | 02 | 0 | ) 14809.2033 | -0.0045 |
| 3.5 | 01 | 0 | 3.5 | 02 | 0 | ) 14809.1012 | -0.0021 |
| 4.5 | 01 | 0 | 4.5 | 02 | 0 | ) 14809.0016 | 0.0005 |
| 5.5 | 01 | 0 | 5.5 | 02 | 0 | 14808.8994 | -0.0017 |
| SrSH |  |  | $C 2 A$ | $X 2 A^{\prime}$ |  |  |  |
| 1.5 | 01 | 0 | 0.5 | 01 | 0 | 15003.3724 | -0.0035 |
| 2.5 | 01 | 0 | 1.5 | 0 | 0 | ) 15003.6018 | -0.0056 |
| 3.5 | 01 | 0 | 2.5 | 01 |  | ) 15003.8424 | 0.0003 |
| 4.5 | 01 | 0 | 3.5 | 0 | 0 | 15004.0796 | -0.0006 |
| 5.5 | 01 | 0 | 4.5 | 01 | 0 | 15004.3175 | -0.0041 |
| 6.5 | 01 | 0 | 5.5 | 01 |  | ) 15004.5666 | 0.0003 |
| 7.5 | 01 | 0 | 6.5 | 01 | 0 | ) 15004.8155 | 0.0012 |
| 8.5 | 01 | 0 | 7.5 | 01 |  | 15005.0646 | -0.0010 |
| 9.5 | 01 | 0 | 8.5 | 01 | 0 | 15005.3219 | 0.0016 |
| 10.5 | 01 | 0 | 9.5 | 01 |  | ) 15005.5793 | 0.0010 |
| 11.5 | 01 | 0 | 10.5 | 01 | 0 | ) 15005.8424 | 0.0028 |
| 12.5 | 01 | 0 | 11.5 | 01 |  | 15006.1106 | 0.0062 |
| 13.5 | 01 | 0 | 12.5 | 0 | 0 | 15006.3820 | 0.0095 |
| 0.5 | 01 | 0 | 1.5 | 01 |  | 15002.9555 | 0.0005 |
| 1.5 | 01 | 0 | 2.5 | 01 | 0 | ) 15002.8045 | 0.0032 |
| 2.5 | 01 | 0 | 3.5 | 01 |  | ) 15002.6532 | 0.0022 |
| 3.5 | 01 | 0 | 4.5 | 01 | 0 | 15002.5077 | 0.0037 |
| 4.5 | 01 | 0 | 5.5 | 01 |  | ) 15002.3595 | -0.0008 |
| 5.5 | 01 | 0 | 6.5 | 01 |  | 15002.2169 | -0.0030 |
| 6.5 | 01 | 0 | 7.5 | 01 |  | ) 15002.0796 | -0.0032 |
| 7.5 | 01 | 0 | 8.5 | 01 |  | ) 15001.9431 | -0.0060 |
| 8.5 | 01 | 0 | 9.5 | 01 |  | 15001.8171 | -0.0016 |

(continued)

Table S1. Continued.

| $J$ | GAM | F | Ka | $J$ | GAM |  |  | $a \mathrm{OBS}$ | OMC |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9.5 | 0 | 1 | 0 | 10.5 | 0 | 1 | 0 | 015001.6895 | -0.0021 |
| 10.5 | 0 | 1 | 0 | 11.5 | 0 | 1 |  | 015001.5682 | 0.0002 |
| 1.5 | 0 | 2 | 0 | 0.5 | 0 | 2 |  | 015003.4357 | 0.0000 |
| 2.5 | 0 | 2 | 0 | 1.5 | 0 | 2 |  | 015003.6018 | -0.0007 |
| 3.5 | 0 | 2 | 0 | 2.5 | 0 | 2 |  | 015003.7737 | 0.0010 |
| 4.5 | 0 | 2 | 0 | 3.5 | 0 | 2 |  | 015003.9459 | -0.0003 |
| 5.5 | 0 | 2 | 0 | 4.5 | 0 | 2 |  | 015004.1188 | -0.0041 |
| 6.5 | 0 | 2 | 0 | 5.5 | 0 | 2 |  | 015004.2980 | -0.0050 |
| 7.5 | 0 | 2 | 0 | 6.5 | 0 | 2 |  | 015004.4883 | 0.0019 |
| 8.5 | 0 | 2 | 0 | 7.5 | 0 | 2 |  | 015004.6729 | -0.0003 |
| 9.5 | 0 | 2 | 0 | 8.5 | 0 | 2 |  | 015004.8575 | -0.0058 |
| 10.5 | 0 | 2 | 0 | 9.5 | 0 | 2 |  | 015005.0646 | 0.0079 |
| 0.5 | 0 | 2 | 0 | 1.5 | 0 | 2 |  | 015002.7036 | 0.0022 |
| 1.5 | 0 | 2 | 0 | 2.5 | 0 | 2 |  | 015002.4870 | 0.0039 |
| 2.5 | 0 | 2 | 0 | 3.5 | 0 | 2 | 0 | 015002.2699 | 0.0017 |
| 3.5 | 0 | 2 | 0 | 4.5 | 0 | 2 |  | 015002.0602 | 0.0036 |
| 4.5 | 0 | 2 | 0 | 5.5 | 0 | 2 |  | 015001.8507 | 0.0024 |
| 5.5 | 0 | 2 | 0 | 6.5 | 0 | 2 |  | 015001.6466 | 0.0033 |
| 6.5 | 0 | 2 | 0 | 7.5 | 0 | 2 |  | 015001.4451 | 0.0035 |
| 7.5 | 0 | 2 | 0 | 8.5 | 0 | 2 |  | 015001.2464 | 0.0030 |
| 8.5 | 0 | 2 | 0 | 9.5 | 0 | 2 | 0 | 015001.0477 | -0.0007 |
| 9.5 | 0 | 2 |  | 10.5 | 0 | 2 |  | 015000.8519 | -0.0049 |
| 10.5 | 0 | 2 | 0 | 11.5 | 0 | 2 |  | 015000.6616 | -0.0070 |
| 11.5 | 0 | 2 | 0 | 12.5 | 0 | 2 |  | 015000.4770 | -0.0068 |
| 0.5 | 0 | 1 | 0 | 0.5 | 0 | 2 |  | 015002.9555 | -0.0024 |
| 1.5 | 0 | 1 | 0 | 1.5 | 0 | 2 |  | 015002.8045 | -0.0016 |
| 2.5 | 0 | 1 | 0 | 2.5 | 0 | 2 |  | 015002.6532 | -0.0045 |
| 3.5 | 0 | 1 | 0 | 3.5 | 0 | 2 |  | 015002.5077 | -0.0049 |
| 4.5 | 0 | 1 | 0 | 4.5 | 0 | 2 |  | 015002.3680 | -0.0028 |
| 5.5 | 0 | 1 | 0 | 5.5 | 0 | 2 |  | 015002.2320 | -0.0004 |
| 6.5 | 0 | 1 | 0 | 6.5 | 0 | 2 |  | 015002.0937 | -0.0035 |
| 7.5 | 0 | 1 | 0 | 7.5 | 0 | 2 |  | 015001.9610 | -0.0044 |
| 8.5 | 0 | 1 | 0 | 8.5 | 0 | 2 |  | 015001.8341 | -0.0028 |
| 9.5 | 0 | 1 | 0 | 9.5 | 0 | 2 |  | 015001.7110 | -0.0008 |
| 10.5 | 0 | 1 | 0 | 10.5 | 0 | 2 |  | 015001.5895 | -0.0006 |
| 0.5 | 0 | 2 | 0 | 0.5 | 0 | 1 |  | 015003.2712 | 0.0000 |
| 1.5 | 0 | 2 | 0 | 1.5 | 0 | 1 |  | 015003.4357 | 0.0029 |
| 2.5 | 0 | 2 | 0 | 2.5 | 0 | 1 |  | 015003.6018 | 0.0041 |
| 3.5 | 0 | 2 | 0 | 3.5 | 0 | 1 |  | 015003.7737 | 0.0077 |
| 4.5 | 0 | 2 | 0 | 4.5 | 0 | 1 |  | 015003.9459 | 0.0084 |
| 5.5 | 0 | 2 | 0 | 5.5 | 0 | 1 |  | 015004.1188 | 0.0064 |
| 6.5 | 0 | 2 | 0 | 6.5 | 0 | 1 |  | 015004.2980 | 0.0075 |
| 7.5 | 0 | 2 | 0 | 7.5 | 0 | 1 |  | 015004.4730 | 0.0010 |
| 8.5 | 0 | 2 | 0 | 8.5 | 0 | 1 |  | 015004.6514 | -0.0055 |
| 9.5 | 0 | 2 | 0 | 9.5 | 0 | 1 |  | 015004.8411 | -0.0039 |
| CaSH |  |  |  | C2A | $A^{\prime}-X 2 A^{\prime}$ |  |  |  |  |
| 1.5 | 0 | 1 | 0 | 0.5 | 0 | 1 |  | 016075.3918 | -0.0011 |
| 2.5 | 0 | 1 | 0 | 1.5 | 0 | 1 |  | 016075.6661 | 0.0017 |
| 3.5 | 0 | 1 |  | 2.5 | 0 | 1 |  | 016075.9487 | 0.0048 |
| 4.5 | 0 | 1 | 0 | 3.5 | 0 | 1 |  | 016076.2363 | 0.0047 |
| 5.5 |  | 1 | 0 | 4.5 | 0 | 1 |  | 016076.5274 | 0.0001 |
| 6.5 | 0 |  |  | 5.5 | 0 | 1 |  | 016076.8296 | -0.0016 |
| 7.5 | 0 | 1 | 0 | 6.5 | 0 | 1 |  | 016077.1429 | -0.0003 |
| 8.5 | 0 | 1 | 0 | 7.5 | 0 | 1 | 0 | 0 16077.4620 | -0.0013 |

Table S1. Continued.

| $J$ | GAM | F | Ka | $J$ | GAM |  | F | Ka | OBS | OMC |  |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 9.5 | 0 | 1 | 0 | 8.5 |  | 0 | 1 | 0 | 16077.7920 | 0.0005 |  |
| 10.5 | 0 | 1 | 0 | 9.5 |  | 0 | 1 | 0 | 16078.1329 | 0.0049 |  |
| 0.5 | 0 | 1 | 0 | 1.5 |  | 0 | 1 | 0 | 16074.8462 | -0.0005 |  |
| 1.5 | 0 | 1 | 0 | 2.5 |  | 0 | 1 | 0 | 16074.5469 | -0.0002 |  |
| 2.5 | 0 | 1 | 0 | 3.5 |  | 0 | 1 | 0 | 16074.2560 | 0.0004 |  |
| 3.5 | 0 | 1 | 0 | 4.5 |  | 0 | 1 | 0 | 16073.9766 | 0.0044 |  |
| 4.5 | 0 | 1 | 0 | 5.5 |  | 0 | 1 | 0 | 16073.6951 | -0.0018 |  |
| 5.5 | 0 | 1 | 0 | 6.5 |  | 0 | 1 | 0 | 16073.4279 | -0.0019 |  |
| 6.5 | 0 | 1 | 0 | 7.5 |  | 0 | 1 | 0 | 16073.1695 | -0.0013 |  |
| 7.5 | 0 | 1 | 0 | 8.5 |  | 0 | 1 | 0 | 16072.9220 | 0.0021 |  |
| 8.5 | 0 | 1 | 0 | 9.5 |  | 0 | 1 | 0 | 16072.6757 | -0.0016 |  |
| 1.5 | 0 | 2 | 0 | 0.5 |  | 0 | 2 | 0 | 16075.7920 | -0.0019 |  |
| 2.5 | 0 | 2 | 0 | 1.5 |  | 0 | 2 | 0 | 16076.1273 | 0.0015 |  |
| 3.5 | 0 | 2 | 0 | 2.5 |  | 0 | 2 | 0 | 16076.4629 | -0.0029 |  |
| 4.5 | 0 | 2 | 0 | 3.5 |  | 0 | 2 | 0 | 16076.8143 | 0.0004 |  |
| 5.5 | 0 | 2 | 0 | 4.5 |  | 0 | 2 | 0 | 16077.1737 | 0.0035 |  |
| 6.5 | 0 | 2 | 0 | 5.5 |  | 0 | 2 | 0 | 16077.5375 | 0.0030 |  |
| 7.5 | 0 | 2 | 0 | 6.5 |  | 0 | 2 | 0 | 16077.9055 | -0.0015 |  |
| 8.5 | 0 | 2 | 0 | 7.5 |  | 0 | 2 | 0 | 16078.2837 | -0.0040 |  |
| 0.5 | 0 | 2 | 0 | 1.5 |  | 0 | 2 | 0 | 16074.6253 | -0.0017 |  |
| 1.5 | 0 | 2 | 0 | 2.5 |  | 0 | 2 | 0 | 16074.3874 | -0.0005 |  |
| 2.5 | 0 | 2 | 0 | 3.5 |  | 0 | 2 | 0 | 16074.1608 | 0.0039 |  |
| 3.5 | 0 | 2 | 0 | 4.5 |  | 0 | 2 | 0 | 16073.9346 | 0.0006 |  |
| 4.5 | 0 | 2 | 0 | 5.5 |  | 0 | 2 | 0 | 16073.7197 | 0.0005 |  |
| 5.5 | 0 | 2 | 0 | 6.5 |  | 0 | 2 | 0 | 16073.5122 | -0.0004 |  |
| 6.5 | 0 | 2 | 0 | 7.5 |  | 0 | 2 | 0 | 16073.3135 | -0.0006 |  |
| 7.5 | 0 | 2 | 0 | 8.5 |  | 0 | 2 | 0 | 16073.1204 | -0.0034 |  |
| 0.5 | 0 | 1 | 0 | 0.5 |  | 0 | 2 | 0 | 16074.8462 | -0.0026 |  |
| 1.5 | 0 | 1 | 0 | 1.5 |  | 0 | 2 | 0 | 16074.5469 | -0.0037 |  |
| 2.5 | 0 | 1 | 0 | 2.5 |  | 0 | 2 | 0 | 16074.2560 | -0.0045 |  |
| 3.5 | 0 | 1 | 0 | 3.5 |  | 0 | 2 | 0 | 16073.9766 | -0.0019 |  |
| 4.5 | 0 | 1 | 0 | 4.5 |  | 0 | 2 | 0 | 16073.6989 | -0.0057 |  |
| 5.5 | 0 | 1 | 0 | 5.5 |  | 0 | 2 | 0 | 16073.4375 | -0.0014 |  |
| 6.5 | 0 | 1 | 0 | 6.5 |  | 0 | 2 | 0 | 16073.1779 | -0.0033 |  |
| 7.5 | 0 | 1 | 0 | 7.5 |  | 0 | 2 | 0 | 16072.9345 | 0.0027 |  |
| 0.5 | 0 | 2 | 0 | 0.5 |  | 0 | 1 | 0 | 16075.4702 | 0.0008 |  |
| 1.5 | 0 | 2 | 0 | 1.5 |  | 0 | 1 | 0 | 16075.7920 | 0.0002 |  |
| 2.5 | 0 | 2 | 0 | 2.5 |  | 0 | 1 | 0 | 16076.1273 | 0.0050 |  |
| 3.5 | 0 | 2 | 0 | 3.5 |  | 0 | 1 | 0 | 16076.4629 | 0.0020 |  |
| 4.5 | 0 | 2 | 0 | 4.5 |  | 0 | 1 | 0 | 16076.8143 | 0.0066 |  |
| 5.5 | 0 | 2 | 0 | 5.5 |  | 0 | 1 | 0 | 16077.1626 | 0.0001 |  |
| 6.5 | 0 | 2 | 0 | 6.5 |  | 0 | 1 | 0 | 16077.5216 | -0.0038 |  |
| 7.5 | 0 | 2 | 0 | 7.5 |  | 0 | 1 | 0 | 16077.8982 | 0.0017 |  |
| 8.5 | 0 | 2 | 0 | 8.5 |  | 0 | 1 | 0 | 16078.2749 | -0.0009 |  |
|  |  |  |  |  |  |  |  |  |  |  |  |


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